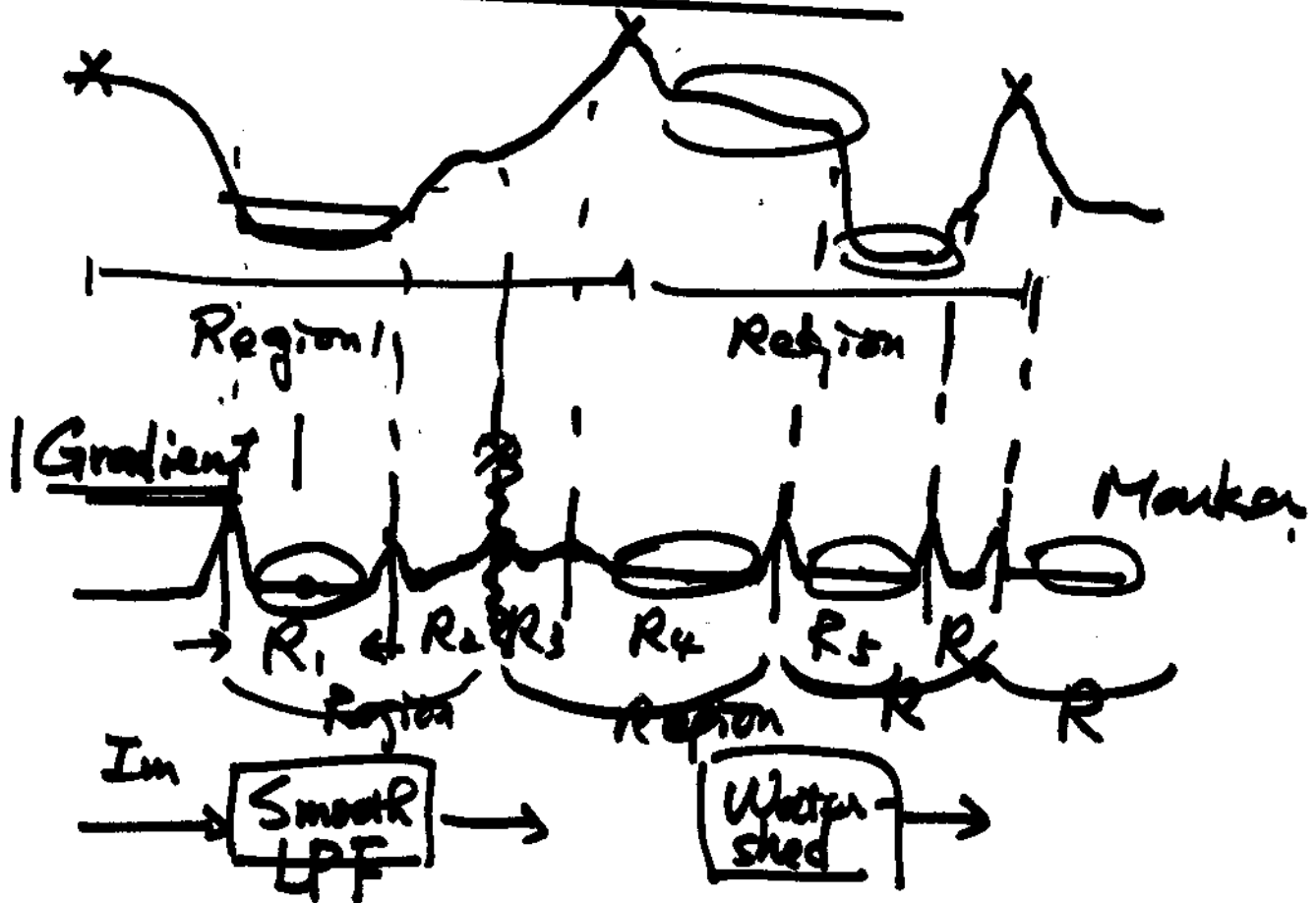


EE 4830 DIP

Loc # 11

Today: Segmentation

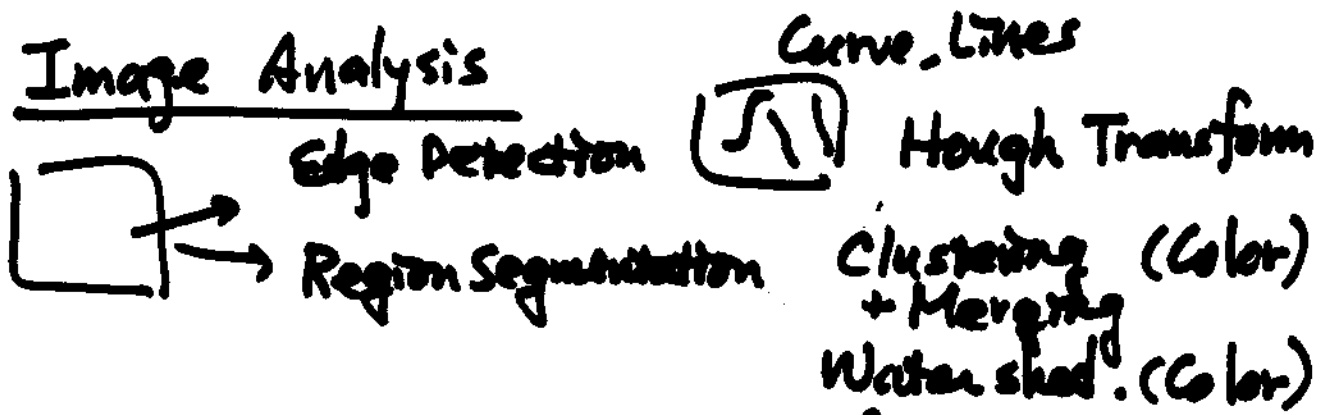
Chap 10. Morphological Processing



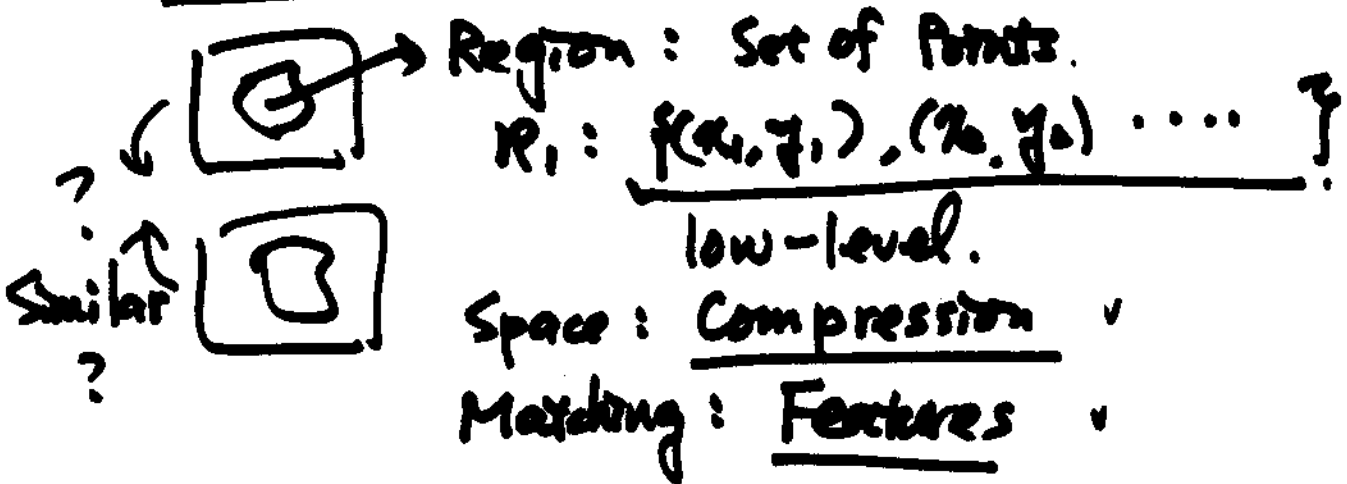
HW#5 Assigned Today
due Apr. 28.

Final Exam May 12 TR. Thursday.

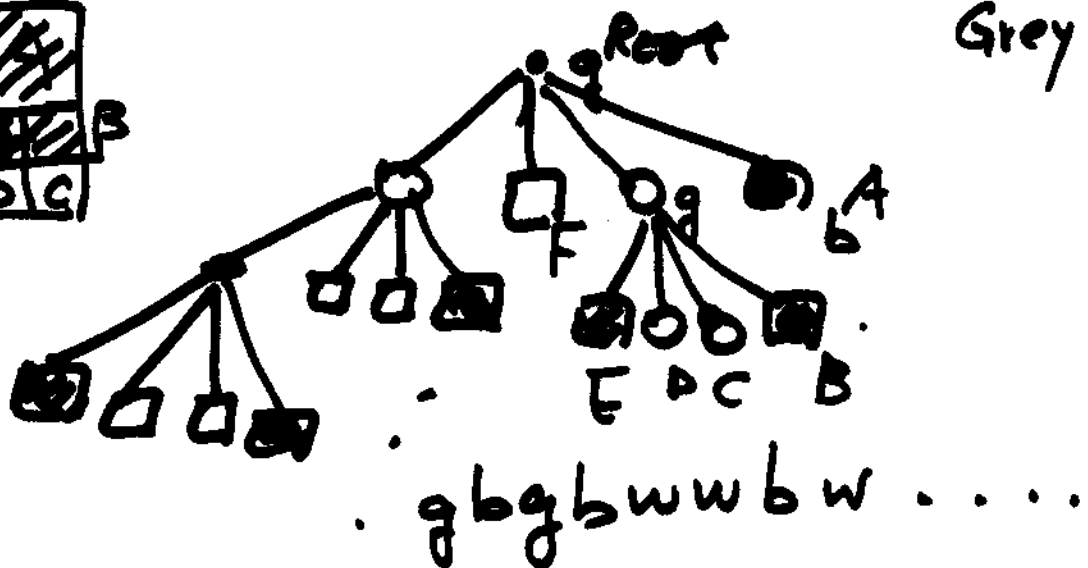
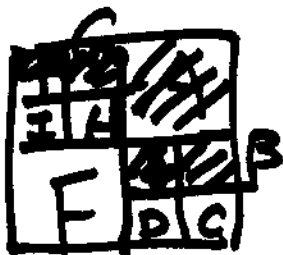
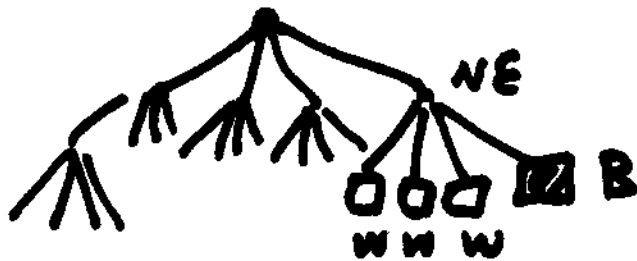
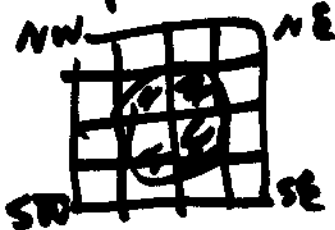
Image Analysis



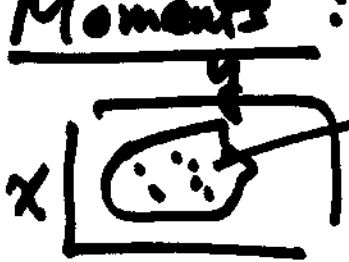
Represent Intermediate Results



Compression: Quad-Tree.



Moments:


$$f(x, y) = \begin{cases} 1 & \text{if } (x, y) \in R \\ 0 & \text{if } (x, y) \notin R \end{cases}$$

$(p+q)$ -th order moments

$$m_{pq} = \sum_R \sum f(x, y) x^p y^q$$

$$m_{10} = \frac{\sum \sum f(x, y) x}{\# \text{ pixels in } R}$$

$$\# \text{ pixels} = \sum \sum f(x, y) = m_{00}$$

$$\left. \begin{aligned} \frac{m_{10}}{m_{00}} &= \bar{x} \\ \frac{m_{01}}{m_{00}} &= \bar{y} \end{aligned} \right\} \text{Centroid of } R$$

Central Moments

$$\mu_{pq} = \sum_R \sum f(x, y) (x - \bar{x})^p (y - \bar{y})^q$$



$$\mu_{20} = \sum \sum f(x, y) (x - \bar{x})^2$$

$$\mu_{02} = \text{Var in } y \text{ dim}$$



camera zoom input
cause ~~some~~ scale change

Q: how will moments
 μ_{pg} change?

$$\begin{matrix} \mu_{10} & \mu_{01} \\ \approx \bar{x} & \bar{y} \\ \mu_{20} & \mu_{02} \end{matrix}$$

HW 5: $f(x, y) \Rightarrow f(\alpha x, \alpha y)$
 μ_{pg} ?

Find a feature that's invariant
to scale change.

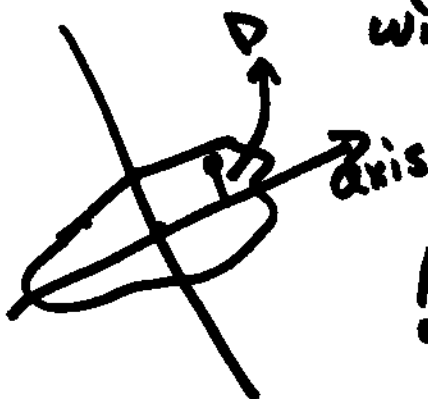
$$\mu_{pg} / (\mu_{00})^{p+g+2/2}$$

scale-
invariant
moments.



$\theta = ?$ Orientation of
the region.

the angle of the axis
with the least moments of
inertia

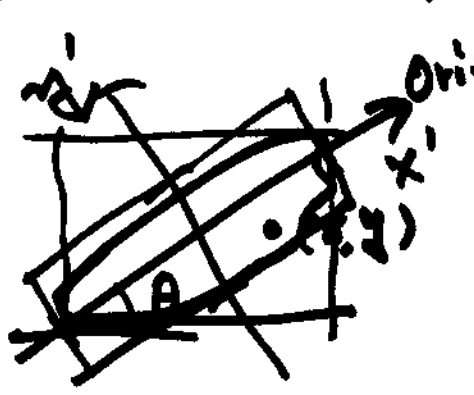


D : distance to the axis

$$\min \left(\sum_R \sum D^2 \right) \Rightarrow$$

$$\theta_{\text{min. moment inertia}} = \frac{1}{2} \tan^{-1} \left[\frac{2 \mu_{11}}{\mu_{20} - \mu_{02}} \right]$$

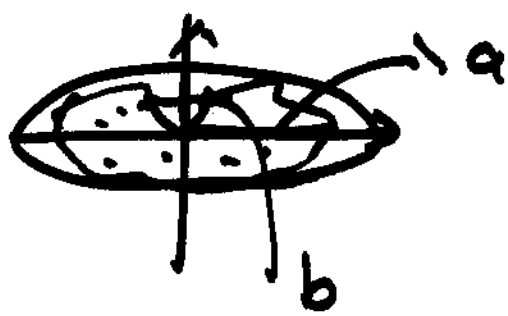
μ_{20} large $\mu_{02} \downarrow$ $\theta \downarrow$
 $\mu_{20} \downarrow$ $\mu_{02} \uparrow$ $\theta \uparrow$
 $\mu_{11} \uparrow$ $\theta = \pi/4$
 $\theta = \pi/4$



- * Minimal Bounding Rectangle ?
- * Best-Fit Ellipse ?
- * Minimal Ellipse ?

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

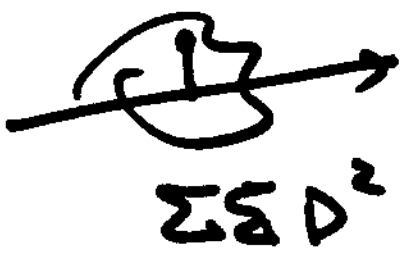
Find max, min in x', y'



Moments of Inertia Ellipse:

$$I_{\text{min}} = \frac{\pi}{4} a b^3$$

$$I_{\text{max}} = \frac{\pi}{4} a^3 b$$



Skeleton Extraction



$$f(m,n) = \begin{cases} 1 & \text{if } R \\ 0 & \text{if } \bar{R} \end{cases}$$

Structure
OCR



Mean Axis Transform

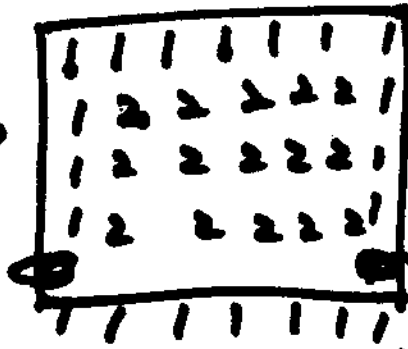
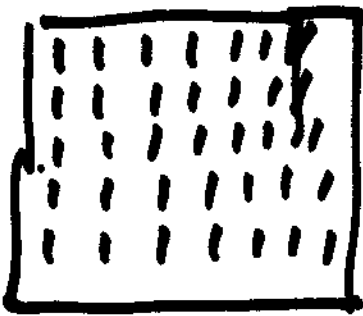
$$f_0(m,n) \equiv \underline{f(m,n)}$$

$$\Rightarrow f_k(m,n) = \underline{f_0(m,n)} + \min_{i,j \in N(m,n)} (f_{k-1}(i,j))$$

$f_0(m,n)$

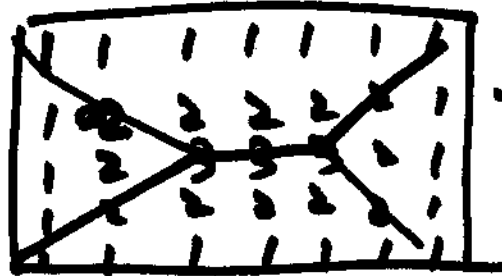
$f_1(m,n)$

N : neighborhood of m,n "4"



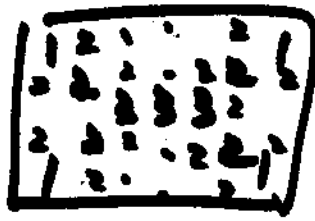
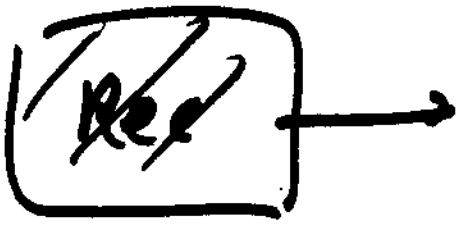
$f_2(m,n)$

f_3

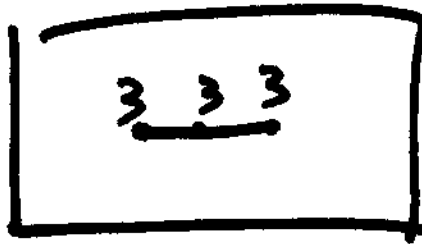
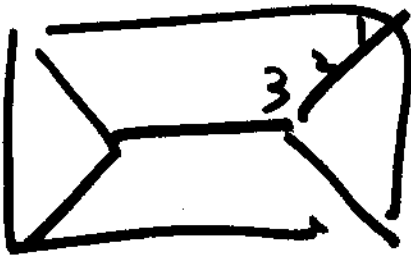
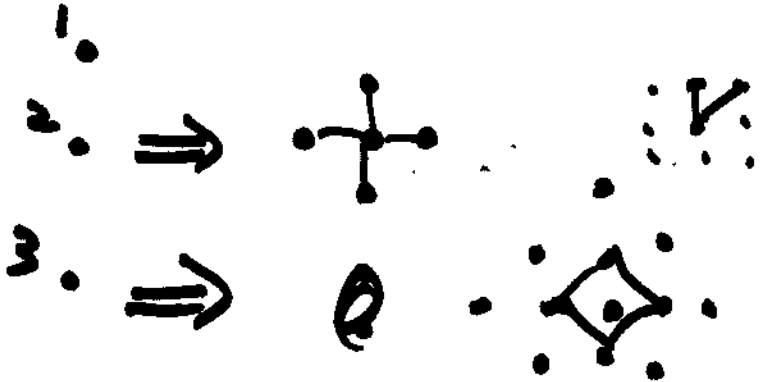
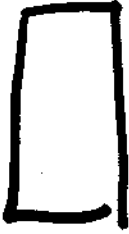


Union of all local max pts.

$$f(m,n) \geq f(i,j) \quad i,j \in N(m,n) \\ \Rightarrow f(m,n) \text{ is local max.}$$



⇒ "Reconstruct"
the original
shape.



Morphological Operation

Erosion & Dilation Operators from set theory

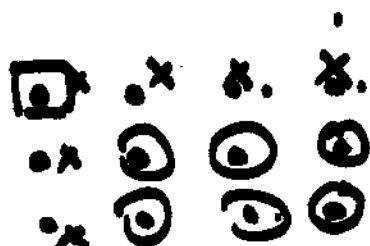


Set of points X

smaller set (structural element): B

Example $B = \cdot \square \rightsquigarrow$ Origin

X

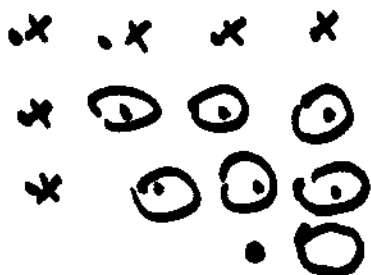


$B = \cdot \square$

Erosion

$$X \ominus B \equiv \{x; B_x \subset X\}$$

X



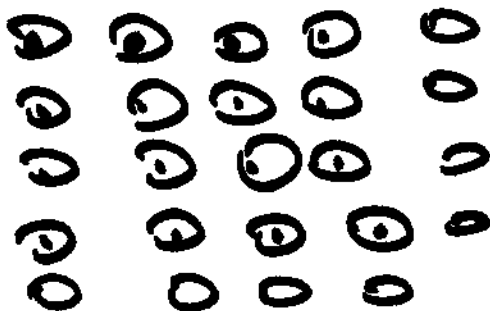
$B = \cdot \square$

$B = \square \cdot$

Dilation

$$X \oplus B \equiv \{x; B_x \cap X \neq \emptyset\}$$

X

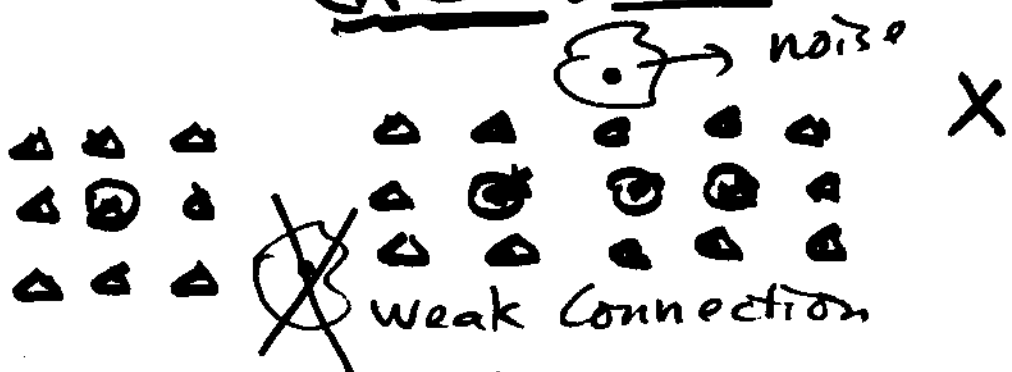


$B = \cdot \square$

Open :

$$X \circ B$$

$$= \underline{(X \ominus B)} \oplus B$$



$$B = \begin{pmatrix} \cdot & \cdot & \cdot \\ \cdot & \square & \cdot \\ \cdot & \cdot & \cdot \end{pmatrix}$$

Close