

# Perceptually-Inspired Music Audio Analysis

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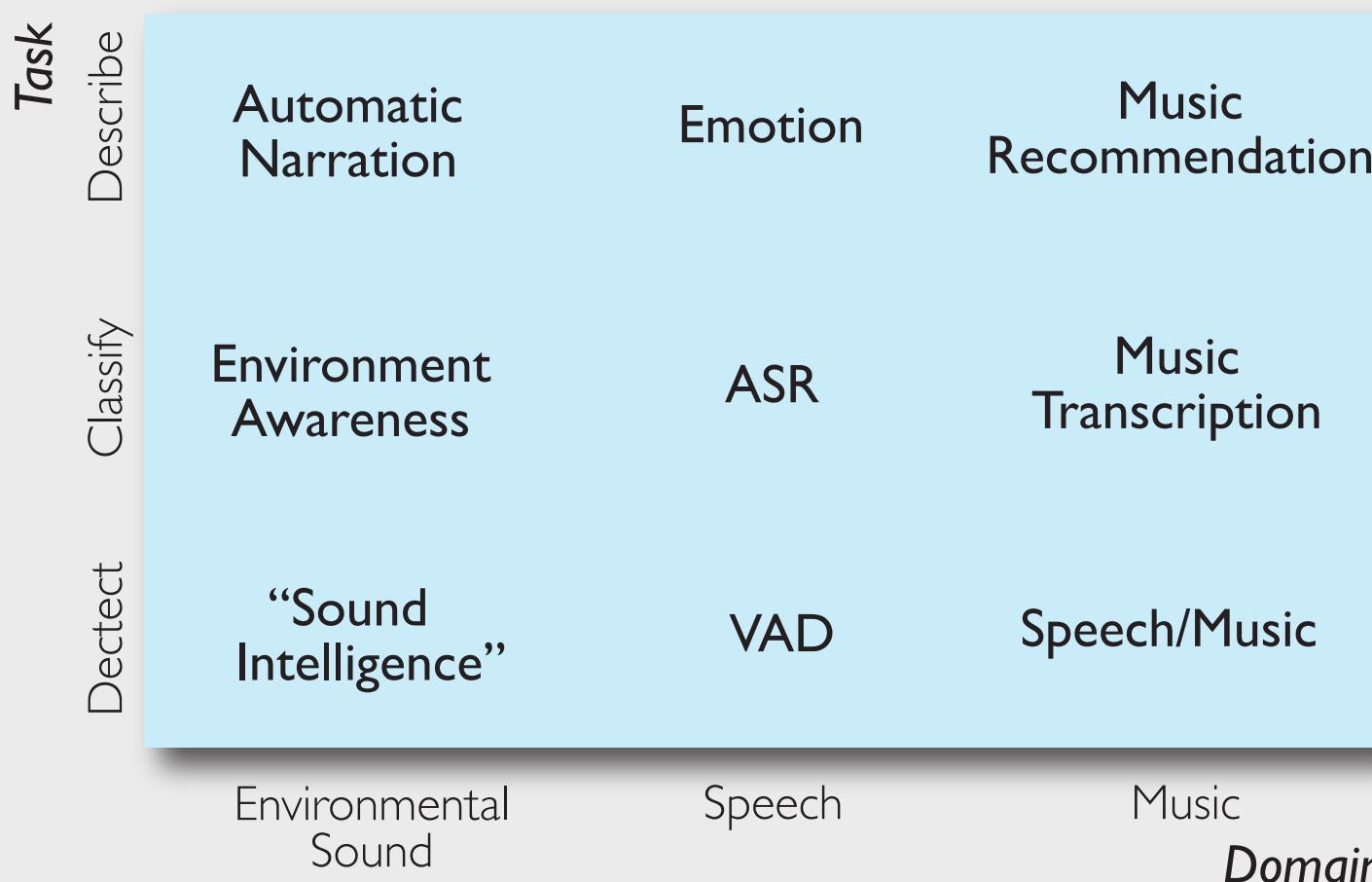
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<http://labrosa.ee.columbia.edu/>

1. Perceptually-Inspired Analysis
2. The Acoustic Structure of Music
3. Music Scene Analysis
4. Large Music Collections
5. Open Issues

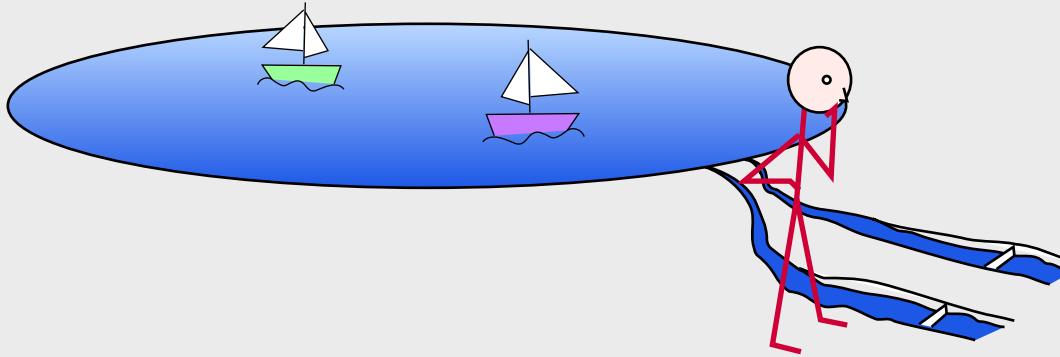
# I. Perceptually-Inspired Analysis

- Machine Listening:  
Extracting **useful information** from sound



# Listening to Mixtures

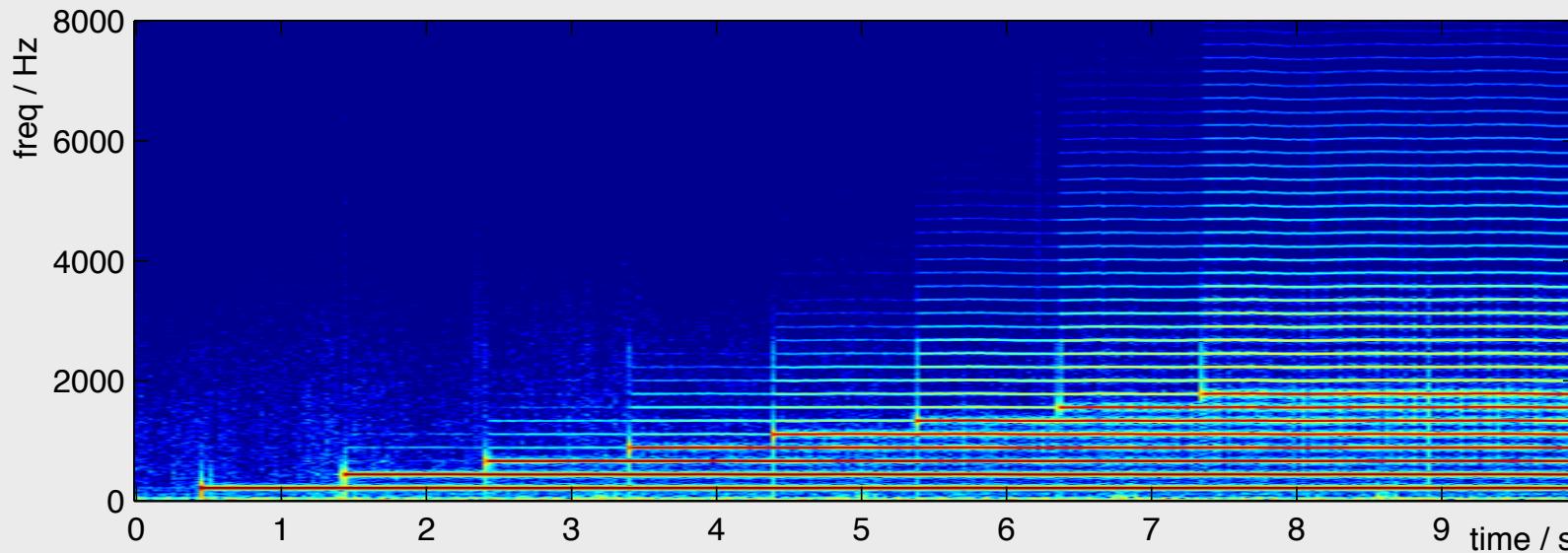
Bregman '90



- The world is **cluttered**  
sound is **transparent**
  - mixtures are inevitable
- Useful information is structured by '**sources**'
  - specific definition of a 'source':  
intentional independence

# Scene Analysis

- Detect separate **events**
  - common **onset**
  - common **harmonicity**

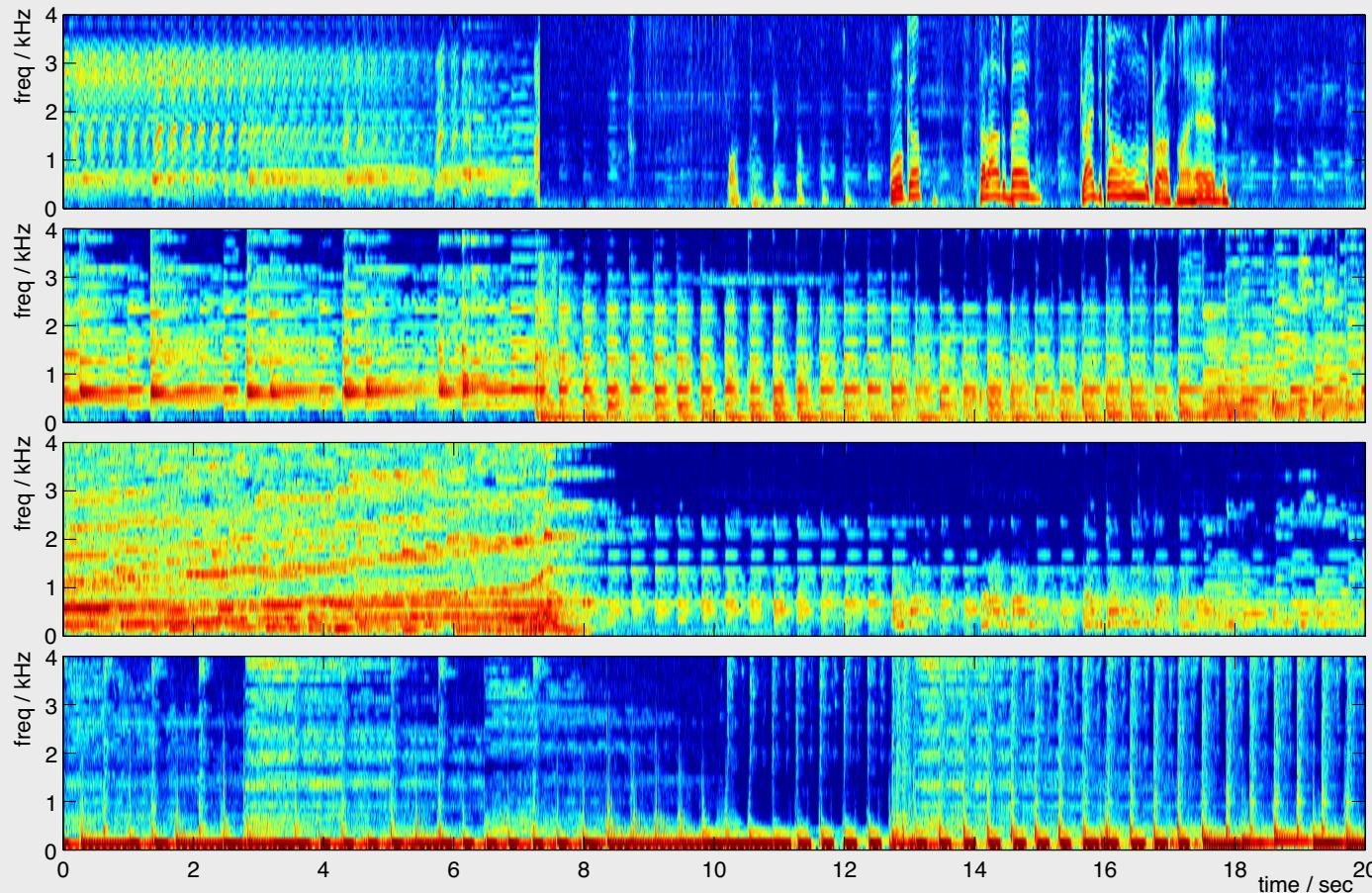


Pierce '83



- instruments & timbre

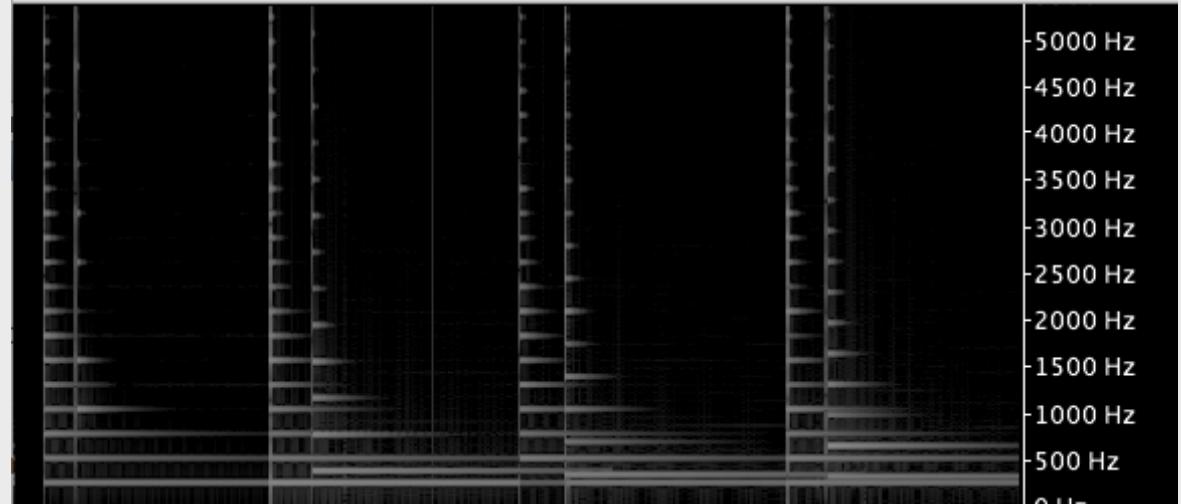
## 2. The Acoustic Structure of Music



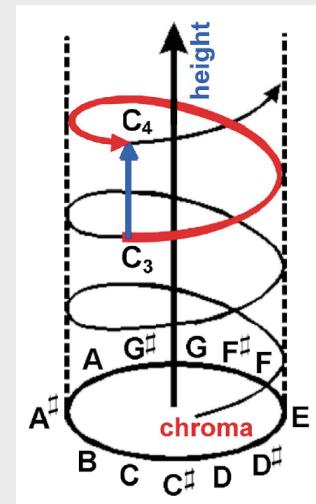
- Pitches, Voices, Rhythm

# Pitch, Harmony, Consonance

- Musical intervals relate to harmonic proximity

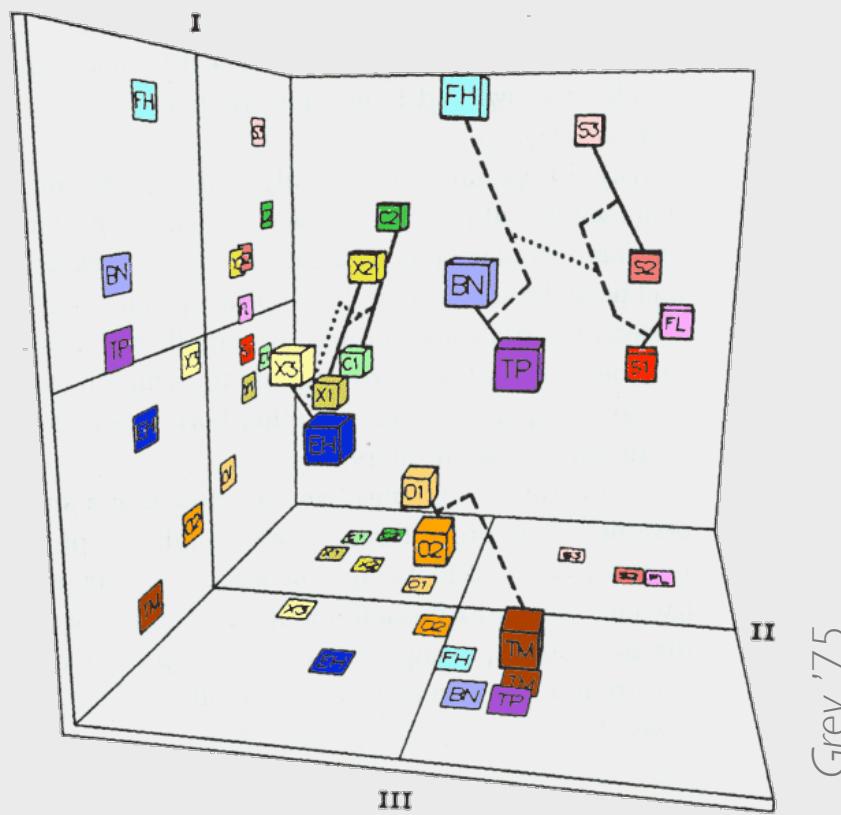


- Pitch Helix



# Timbre

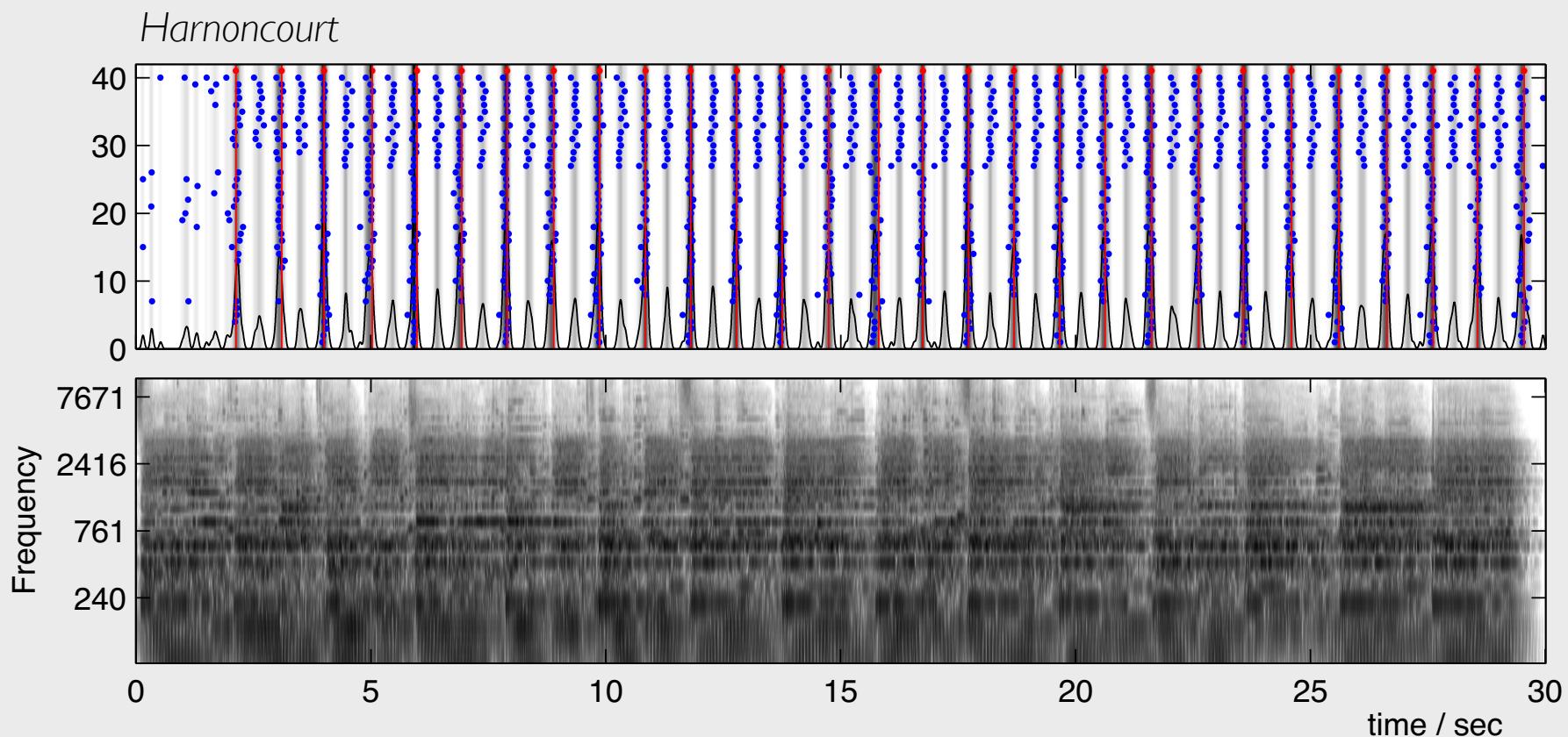
- The property that distinguishes instruments



- spectrum, noise, onset, dynamics, ...

# Rhythm

- Periodic “events” perceived as a **structure**



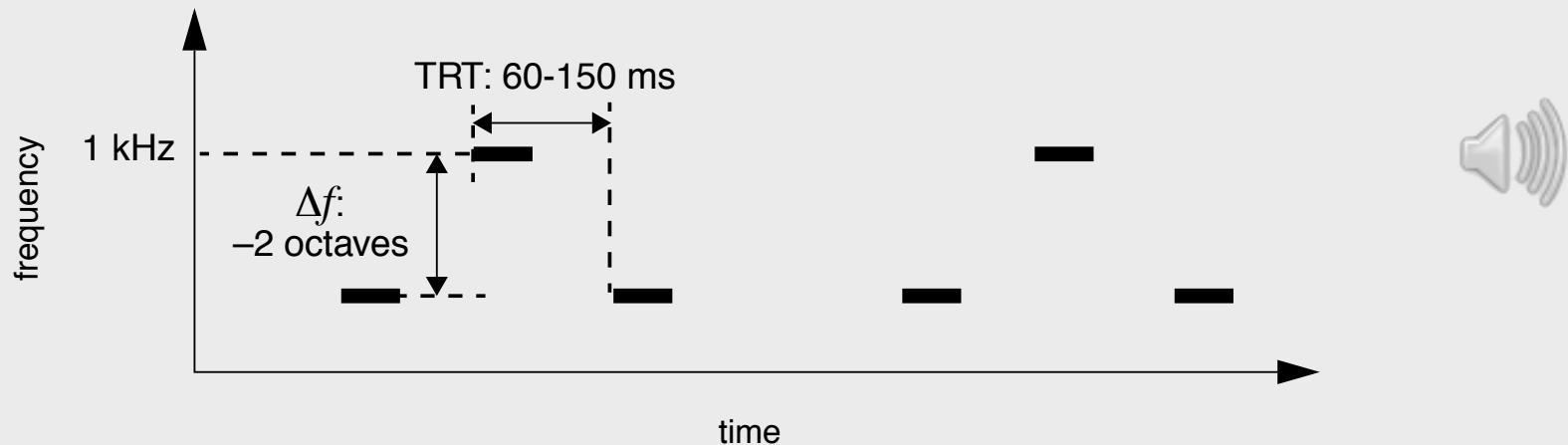
McKinney & Moelants '06

- hierarchy, swing



# Sequences & Streaming

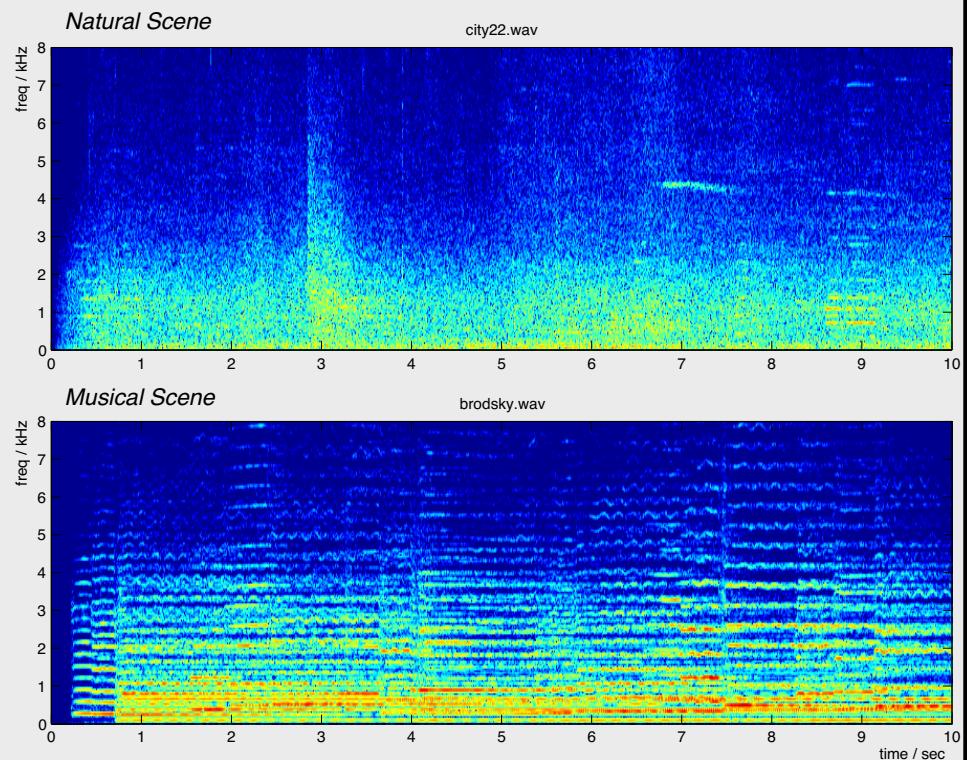
- Perceptual effects of sequences
  - e.g. streaming



- **Music is built of sequences**
  - at many different levels

# Music and Scene Analysis

- Music appears designed to “defeat” auditory scene analysis
  - harmonic relations  
→ overlapped harmonics
  - rhythmic playing  
→ synchronized onsets
  - co-ordinated ensembles  
→ mutual dependence of sources



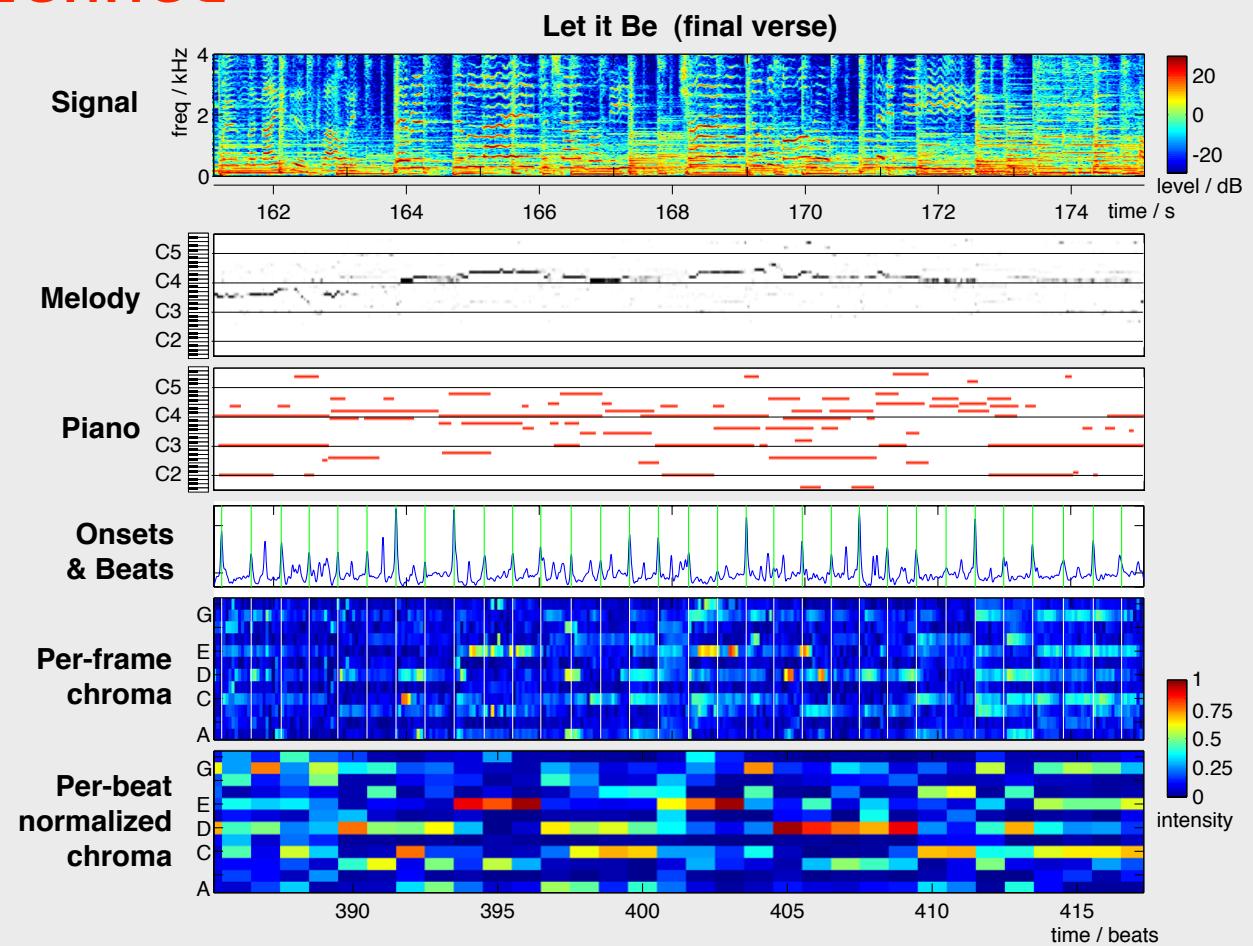
- Maybe that's why we like it!



# 3. Music Scene Analysis

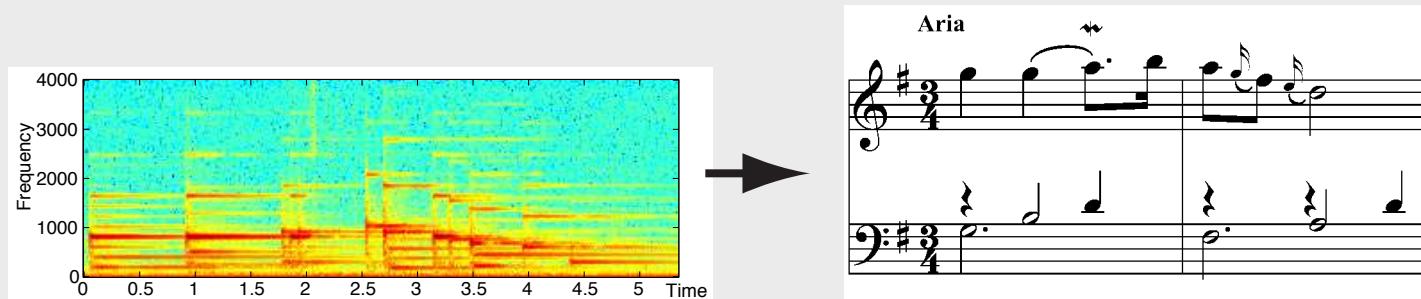
- Interesting music audio analysis tasks are **perceptually defined**

○ what do listeners **hear**?



# Note Transcription

- Goal: Recover the **score** (notes, timing, voices)

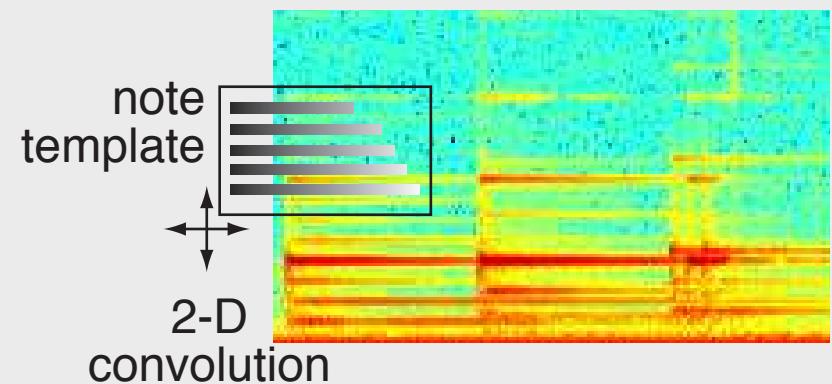


- musicians can (be trained to) do it

- Framework:

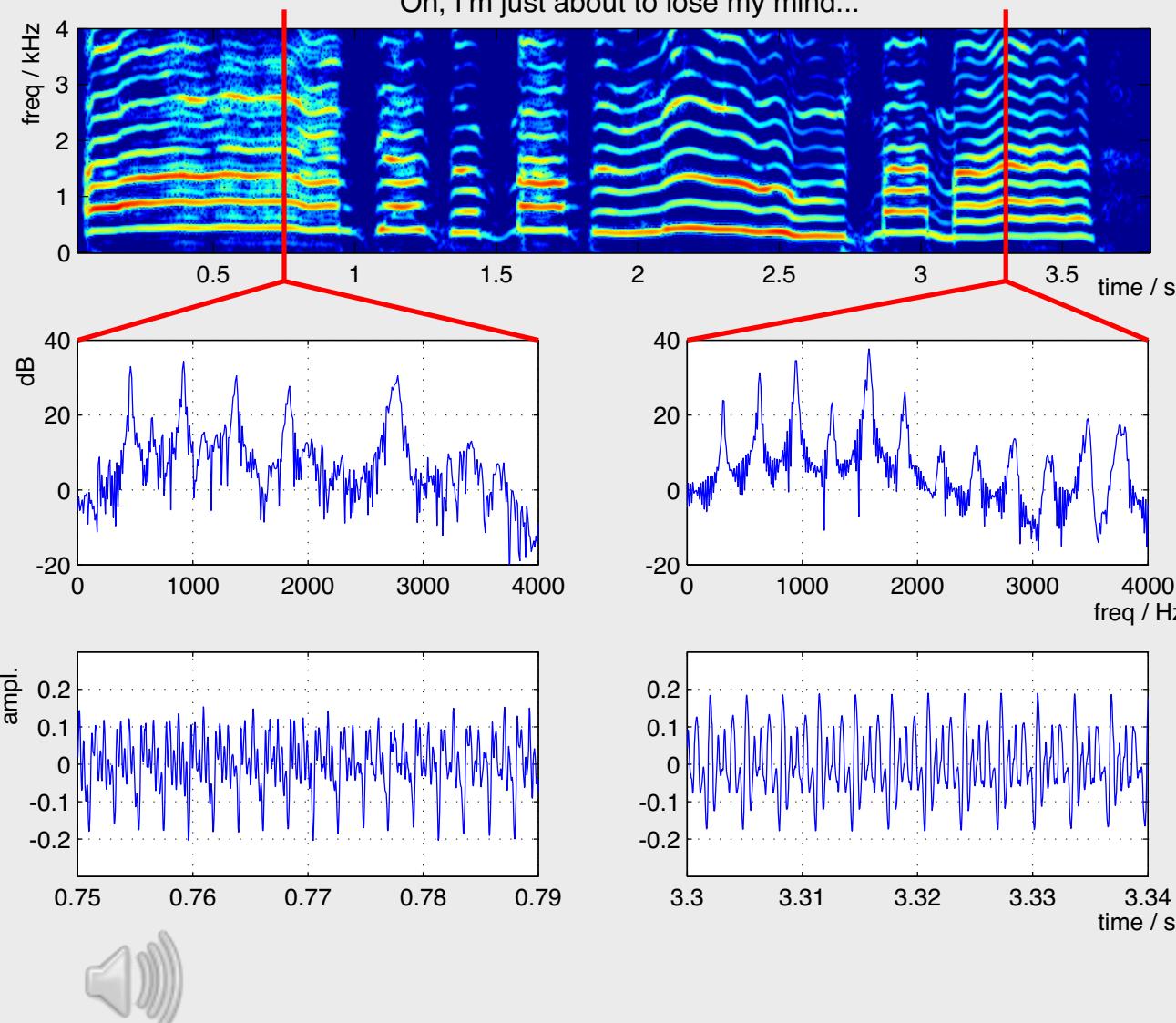
- find the best-matching **synthesis** parameters?

Note events  $\{t_k, p_k, i_k\}$   $\xrightarrow{\text{synthesis}}$  ? Observations  $X[k,n]$

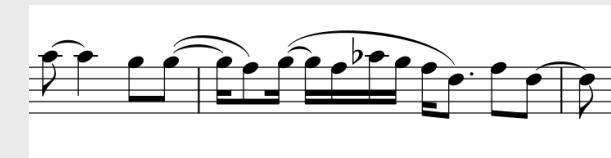


# Note Transcription Problems

“Oh, I’m just about to lose my mind...”

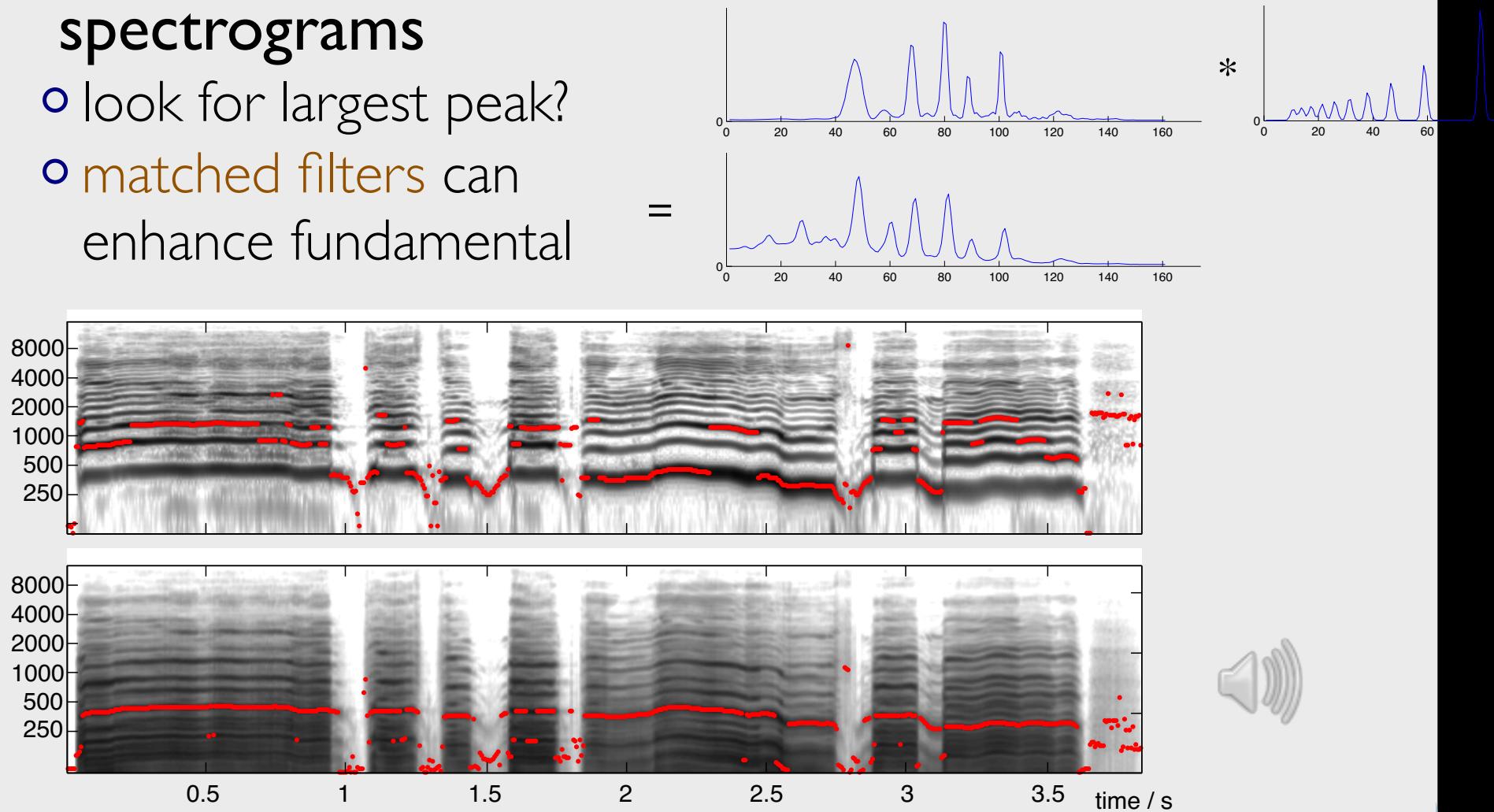


- noise / multiple  $f_0$ s
- Voice Activity Detection
- unclear  $f_0$
- note segmentation



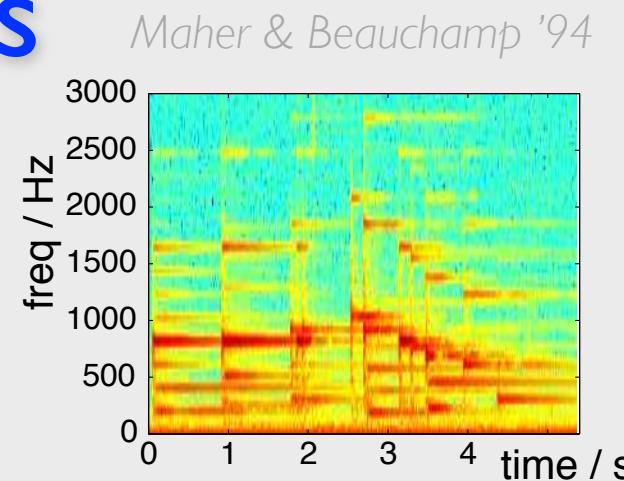
# Pitch Templates

- Harmonic series as patterns on log-frequency spectrograms
  - look for largest peak?
  - matched filters can enhance fundamental

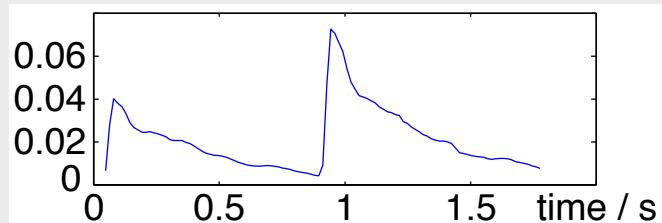


# Sinusoid Tracks

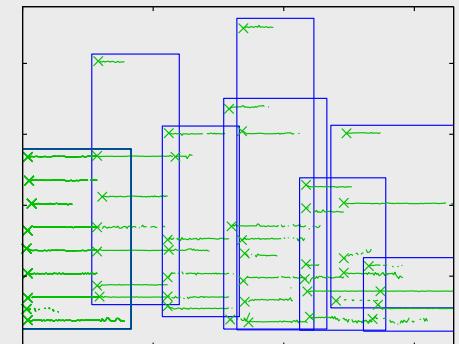
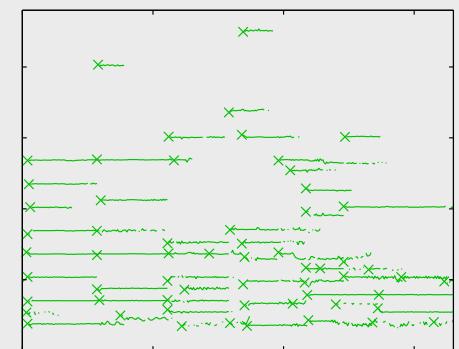
- Notes generate multiple harmonics in **sinusoid analysis**
  - find pitches by grouping them?



- Problems
  - when to “break tracks”



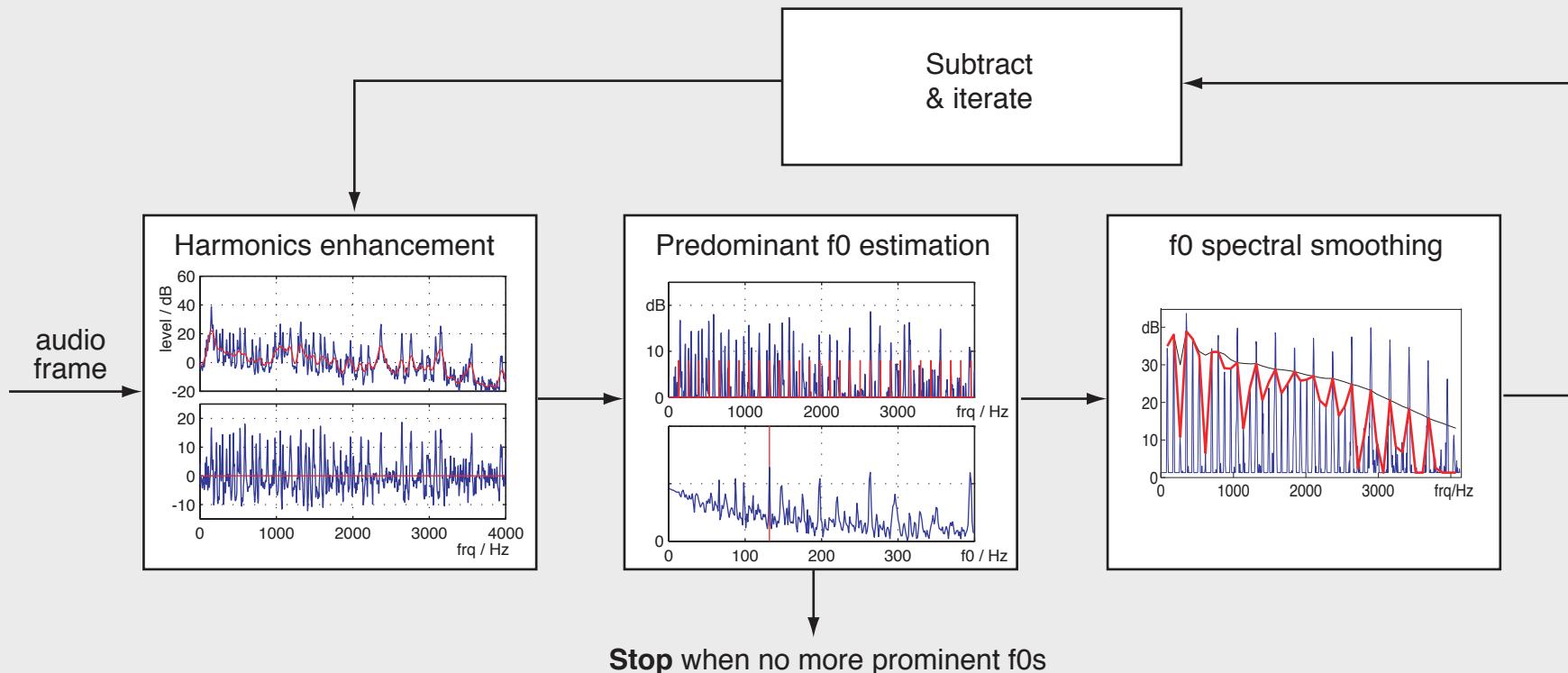
- how to group (harmonicity, onset)



# Iterative Removal

Klapuri '01, '06

- At each frame:
  - estimate dominant  $f_0$  by checking for harmonics
  - cancel it from spectrum
  - repeat until no  $f_0$  is prominent



# Probabilistic Model

Goto '97, '00

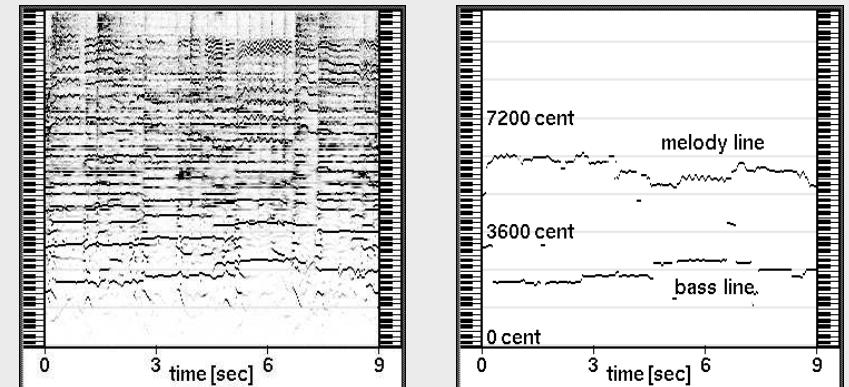
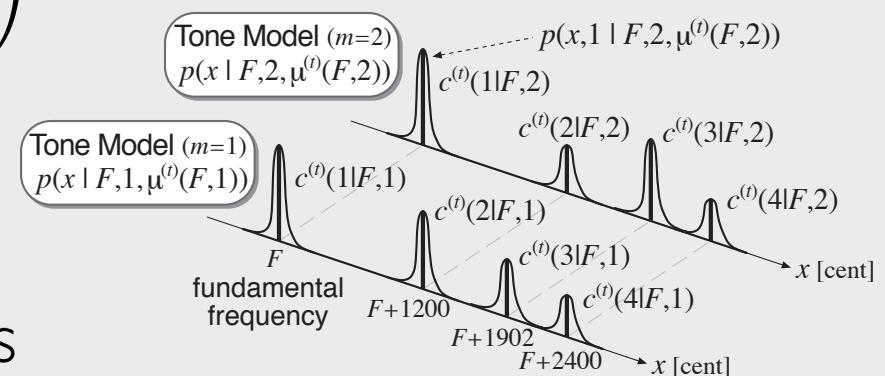
- Generative model:

$$p(x(f)) = \int \left( \sum_m w(F, m) p(x(f) | F, m) \right) dF$$

- spectrum  
= weighted combination  
of tone models at specific  $f_0$ s

- ‘knowledge’ in models  
& prior distributions for  $f_0$

- Is it  
perceptually relevant?



# Trained Pitch Classifier

- Exchange signal models for data
  - transcription as pure classification problem

Poliner & Ellis '05,'06,'07

**Training data and features:**

- MIDI, multi-track recordings, playback piano, & resampled audio (less than 28 mins of train audio).
- Normalized magnitude STFT.



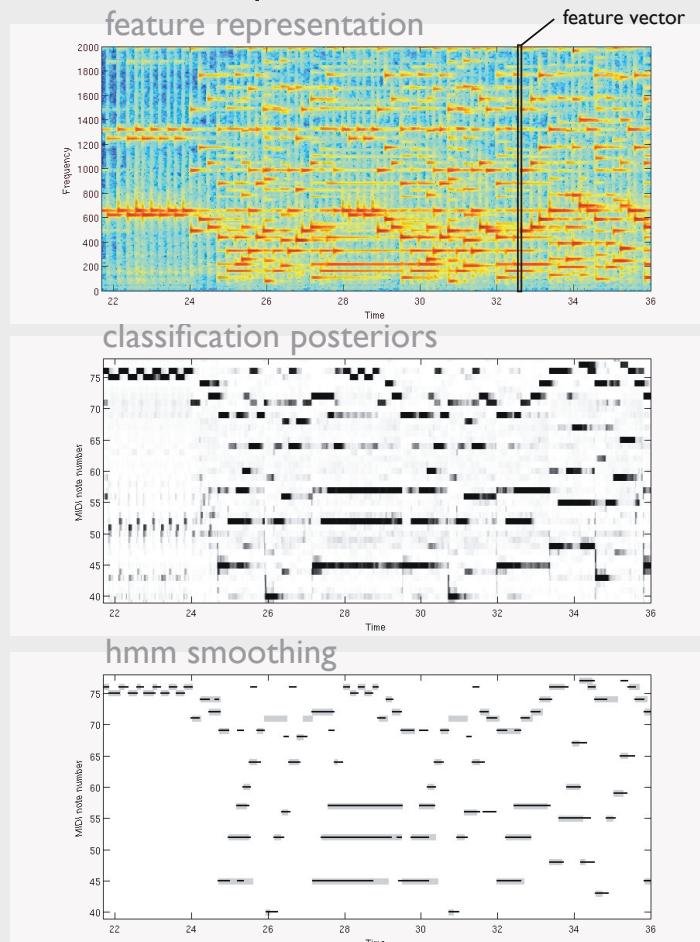
**Classification:**

- N-binary SVMs (one for ea. note).
- Independent frame-level classification on 10 ms grid.
- Dist. to class bndy as posterior.



**Temporal Smoothing:**

- Two state (on/off) independent HMM for ea. note. Parameters learned from training data.
- Find Viterbi sequence for ea. note.



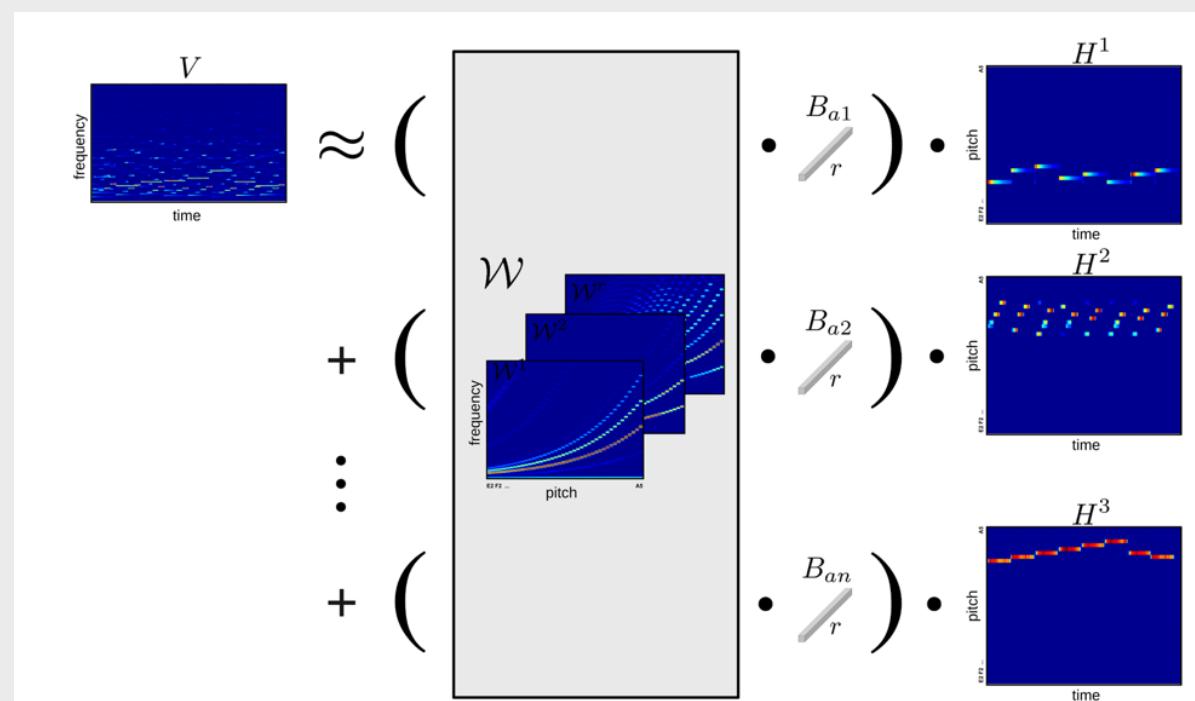
# Instrument Modeling

- Use NMF to model spectrum as **templates** + **activation**

Grindlay & Ellis '09, '11

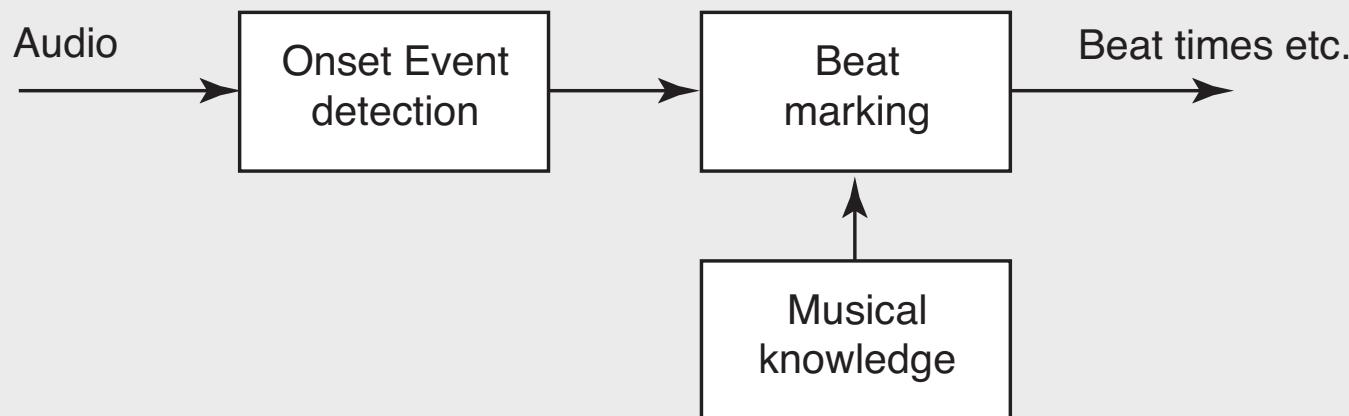
$$\mathbf{X} = \mathbf{W} \cdot \mathbf{H}$$

- Eigeninstrument bases constrain instrument spectra



# Rhythm Tracking

- Rhythm/Beat tracking has 2 main components:
  - front end: extract ‘events’ from audio
  - back end: find plausible beat sequence to match



- Other outputs

- tempo
- time signature
- metrical level(s)

# Onset Detection

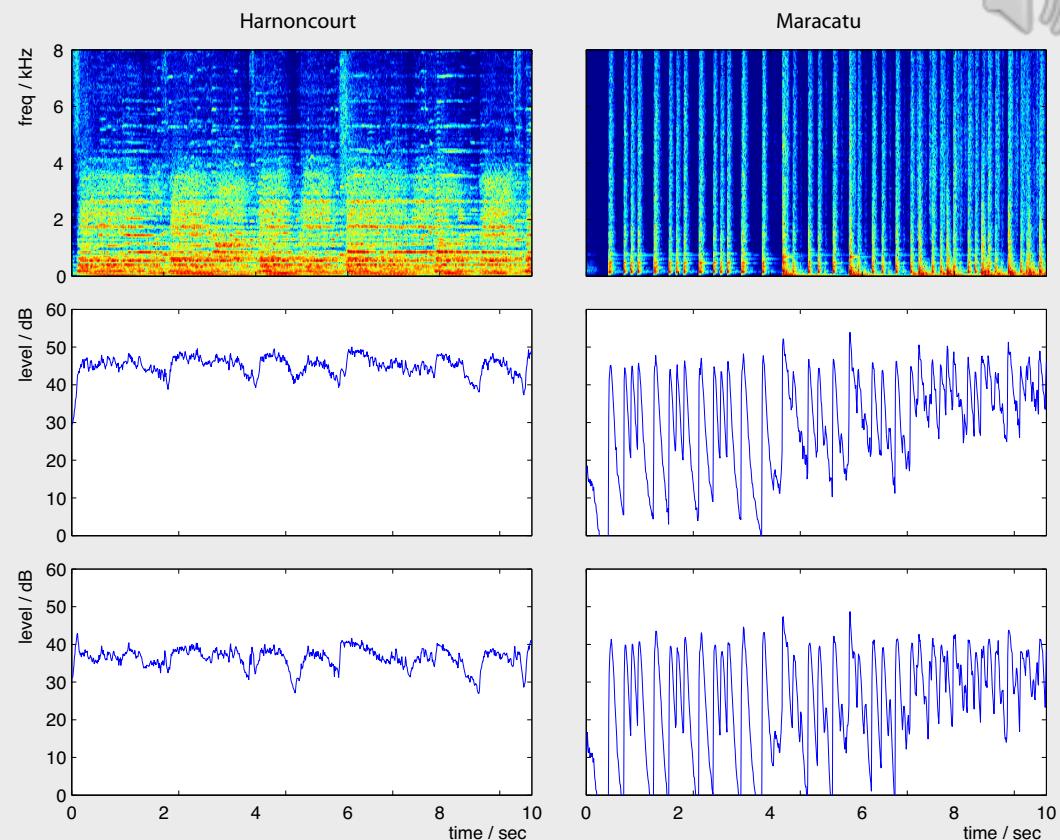
- Simplest thing is **energy envelope**

◦ emphasis on high frequencies?

$$\sum_f |X(f, t)|$$

$$\sum_f f \cdot |X(f, t)|$$

$$e(n_0) = \sum_{n=-W/2}^{W/2} w[n] |x(n + n_0)|^2$$



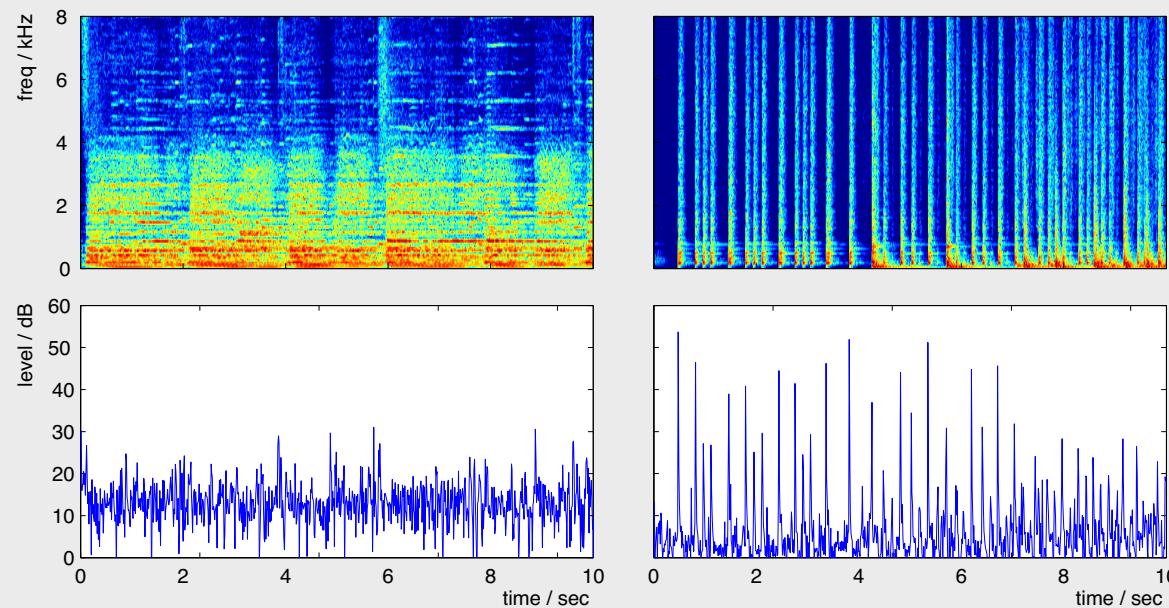
# Multiband Derivatives

Puckette et. al '98

- Sometimes energy just “shifts”
  - calculate & sum onset in **multiple bands**
  - use **ratio** instead of difference - normalize energy

$$o(t) = \sum_f W(f) \max(0, \frac{|X(f, t)|}{|X(f, t - 1)|} - 1)$$

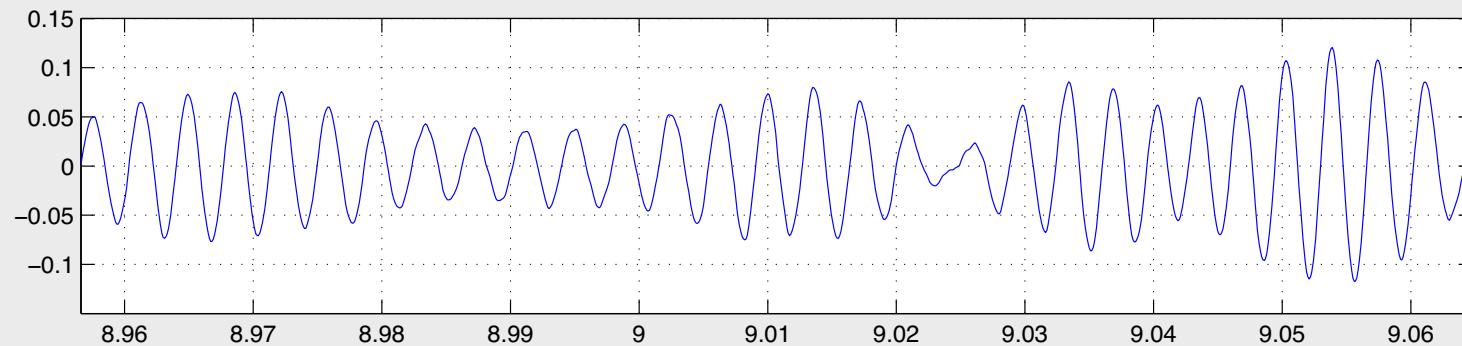
**bonk~**



# Phase Deviation

Bello et al. '05

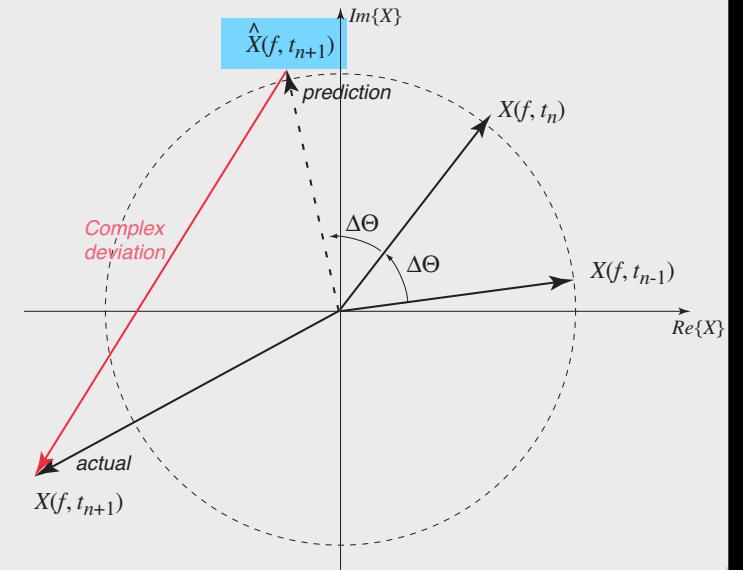
- When amplitudes don't change much, **phase discontinuity** may signal new note



- Can detect by comparing actual phase with **extrapolation** from past

$$\hat{X}(f, t_{n+1}) = X(f, t_n) \frac{X(f, t_n)}{X(f, t_{n-1})}$$

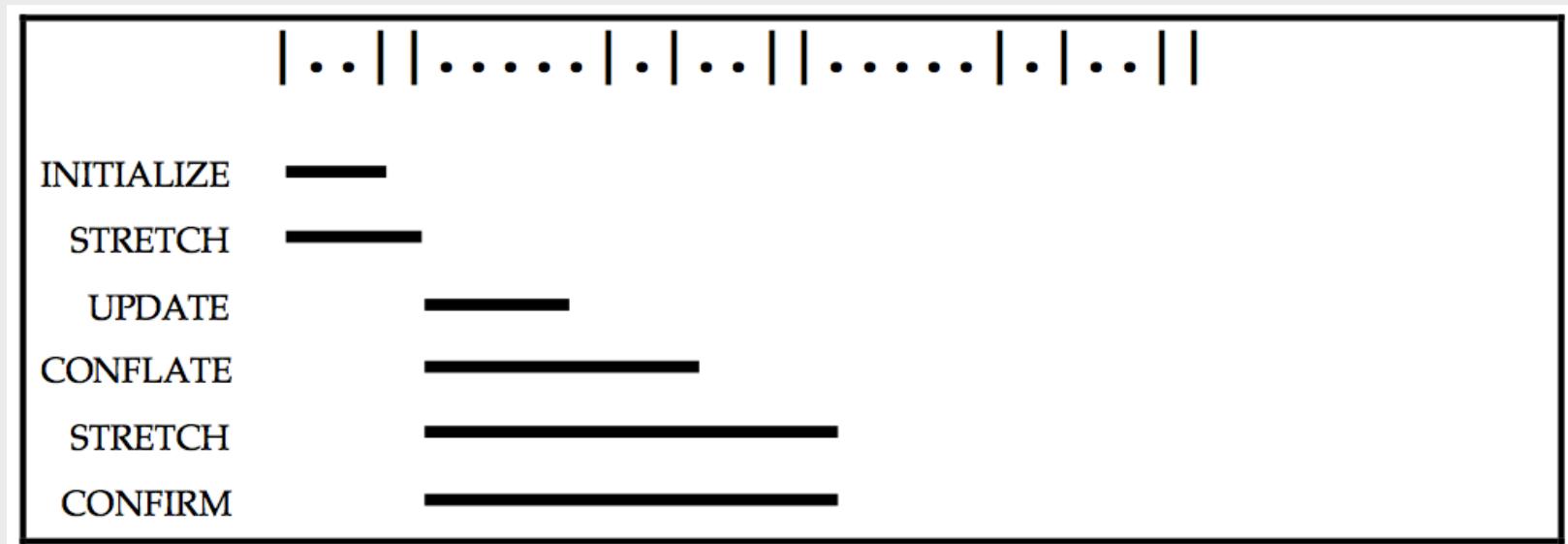
- combine with **amplitude...**



# Rhythm Tracking

Desain & Honing 1999

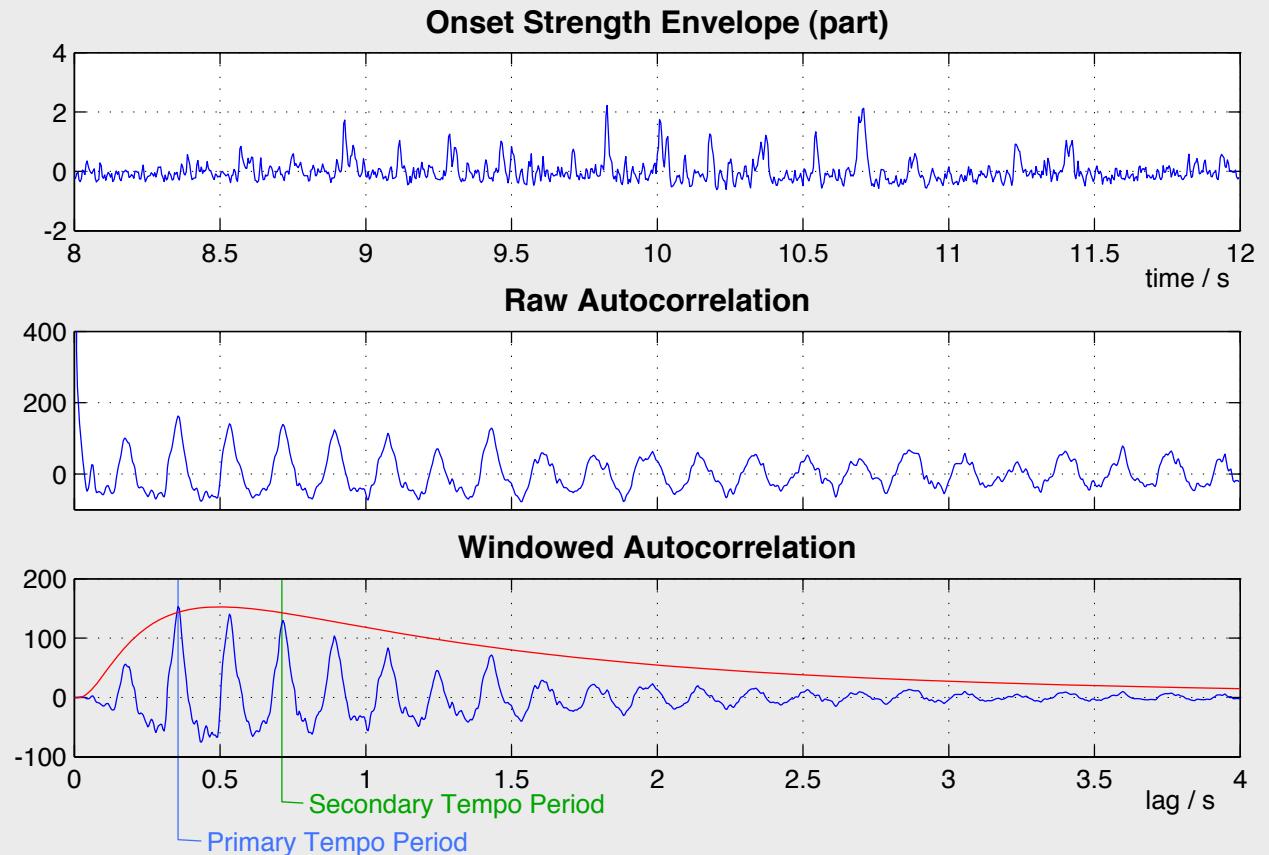
- Earliest systems were rule based
  - based on musicology Longuet-Higgins and Lee, 1982
  - inspired by linguistic grammars - Chomsky



- **input**: event sequence (MIDI)
- **output**: quarter notes, downbeats

# Tempo Estimation

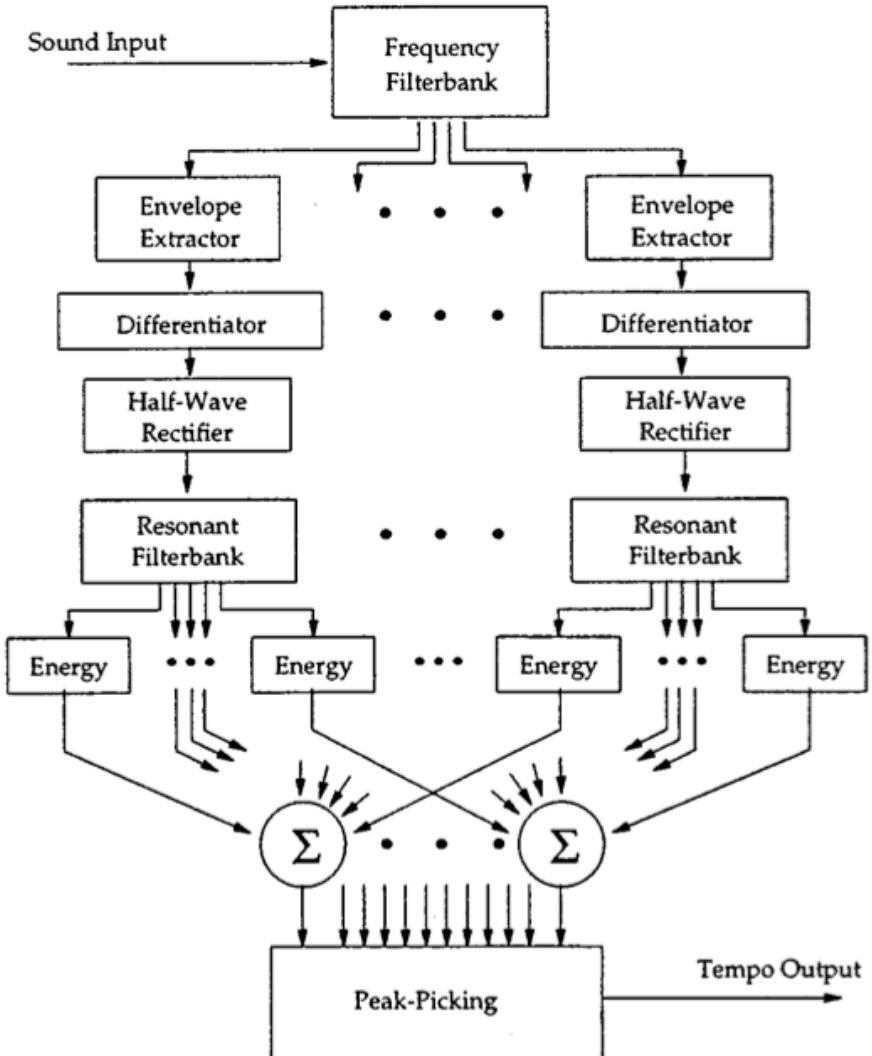
- Perception of **beat** comes from regular spacing
  - .. the kind of thing we detect with **autocorrelation**
- Pick peak in **onset envelope** **autocorrelation**
  - after applying “human preference” window
  - check for **subbeat**



# Resonators for Beat Tracking

- How to address:
  - build-up of rhythmic evidence
  - “ghost events”
  - (audio input)
- Reminiscent of a **comb filter**...
  - resonant filterbank of
$$y(t) = \alpha y(t - T) + (1 - \alpha)x(t)$$
for all possible  $T$

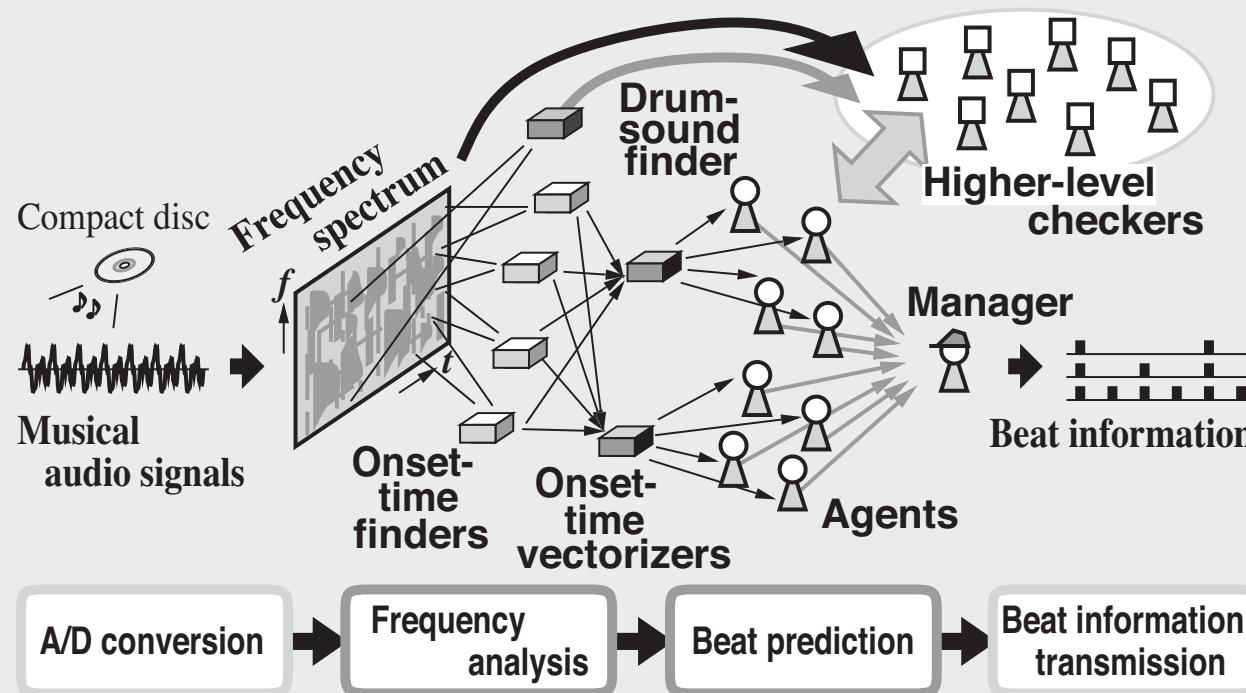
Scheirer '98



# Multi-Hypothesis Systems

Goto & Muraoka 1994  
Goto 2001  
Dixon 2001

- Beat is ambiguous
  - develop several alternatives



- inputs: music audio
- outputs: beat times, downbeats, BD/SD patterns...

# Objective Function Optimization

Ellis 2007

- Re-cast beat tracking as **optimization**:  
Find beat times  $\{t_i\}$  to maximize

$$C(\{t_i\}) = \sum_{i=1}^N O(t_i) + \alpha \sum_{i=2}^N F(t_i - t_{i-1}, \tau_p)$$

- $O(t)$  is **onset strength** function
- $F(\Delta t, \tau)$  is **tempo consistency** score e.g.

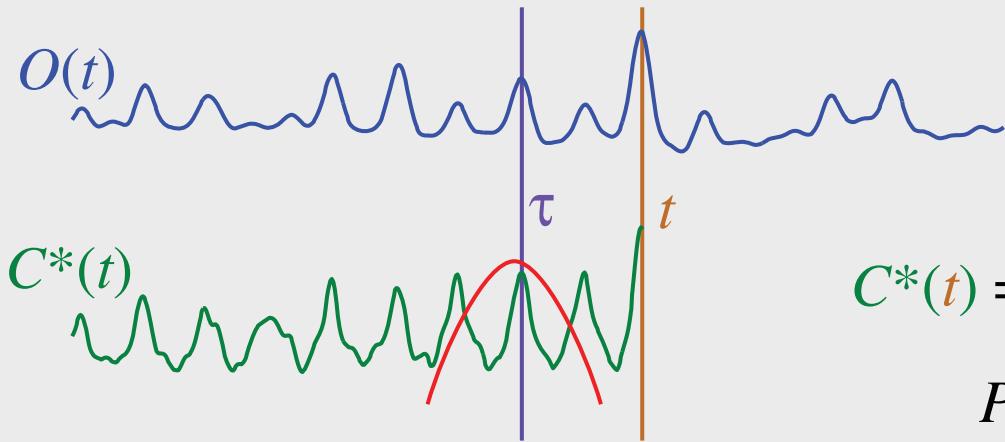
$$F(\Delta t, \tau) = - \left( \log \frac{\Delta t}{\tau} \right)^2$$

- (needs tempo for  $\tau$ )

- Looks like an **exponential search** over all  $\{t_i\}$ 
  - ... but Dynamic Programming saves us

# Beat Tracking by DP

- To optimize  $C(\{t_i\}) = \sum_{i=1}^N O(t_i) + \alpha \sum_{i=2}^N F(t_i - t_{i-1}, \tau_p)$ 
  - define  $C^*(t)$  as best score up to time  $t$
  - then build up recursively (with traceback  $P(t)$ )



$$C^*(t) = O(t) + \max_{\tau} \{\alpha F(t - \tau, \tau_p) + C^*(\tau)\}$$

$$P(t) = \operatorname{argmax}_{\tau} \{\alpha F(t - \tau, \tau_p) + C^*(\tau)\}$$

- final beat sequence  $\{t_i\}$  is best  $C^*$  + back-trace

# beatsimple

- Beat tracking in 15 lines of Matlab

```
function beats = beatsimple(localscore, period, alpha)
% beats = beatsimple(localscore, period, alpha)
% Core of the DP-based beat tracker
% <localscore> is the onset strength envelope
% <period> is the target tempo period (in samples)
% <alpha> is weight applied to transition cost
% <beats> returns the chosen beat sample times.
% 2007-06-19 Dan Ellis dpwe@ee.columbia.edu

% backlink(time) is best predecessor for this point
% cumscore(time) is total cumulated score to this point
backlink = -ones(1,length(localscore));
cumscore = localscore;

% Search range for previous beat
prange = round(-2*period):-round(period/2);
% Log-gaussian window over that range
txcost= (-alpha*abs((log(prange/-period)).^2));

for i = max(-prange + 1):length(localscore)

    timerange = i + prange;

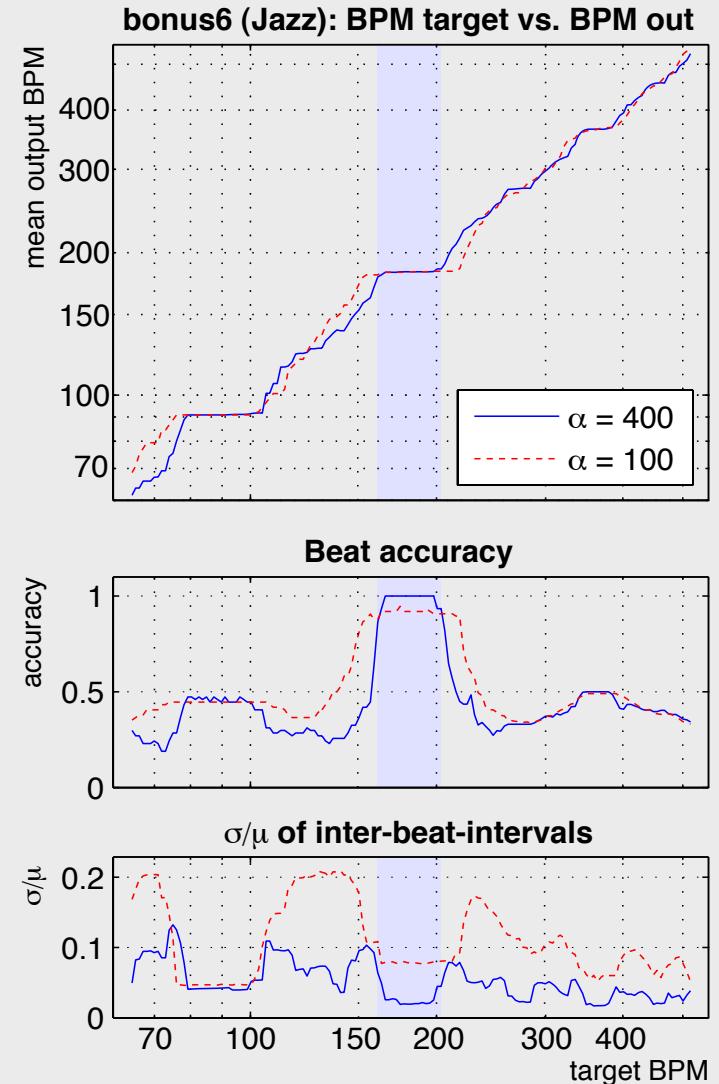
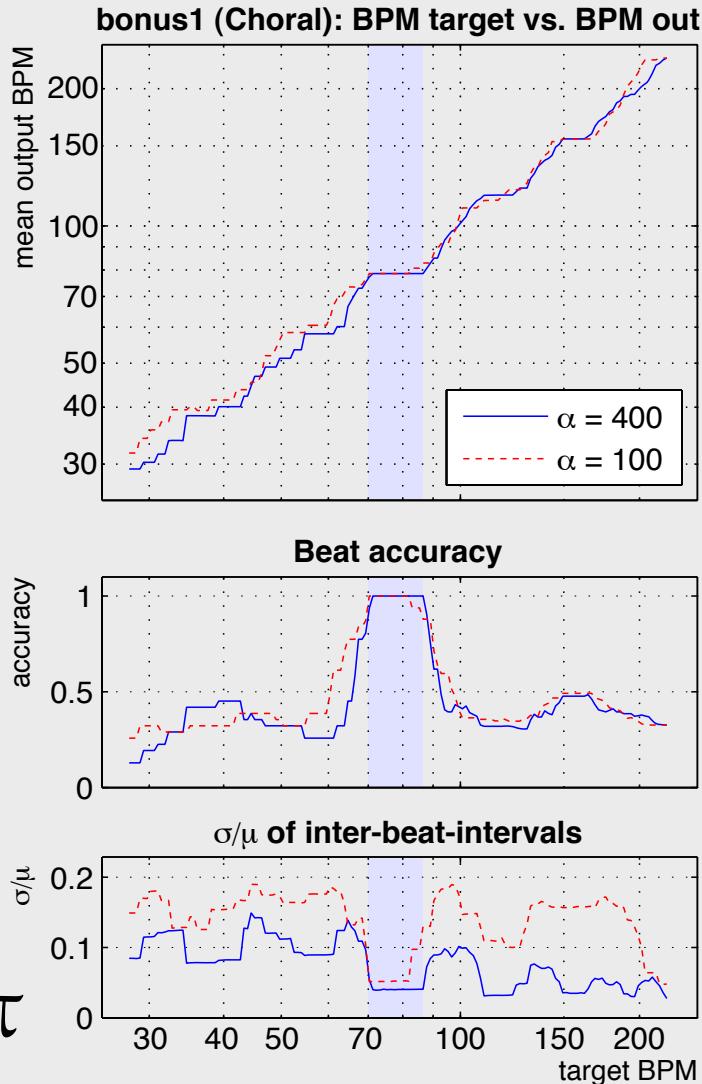
    % Search over all possible predecessors
    % and apply transition weighting
    scorecands = txcost + cumscore(timerange);
    % Find best predecessor beat
    [vv,xx] = max(scorecands);
    % Add on local score
    cumscore(i) = vv + localscore(i);
    % Store backtrace
    backlink(i) = timerange(xx);

end

% Start backtrace from best cumulated score
[vv,beats] = max(cumscore);
% .. then find all its predecessors
while backlink(beats(1)) > 0
    beats = [backlink(beats(1)),beats];
end
```

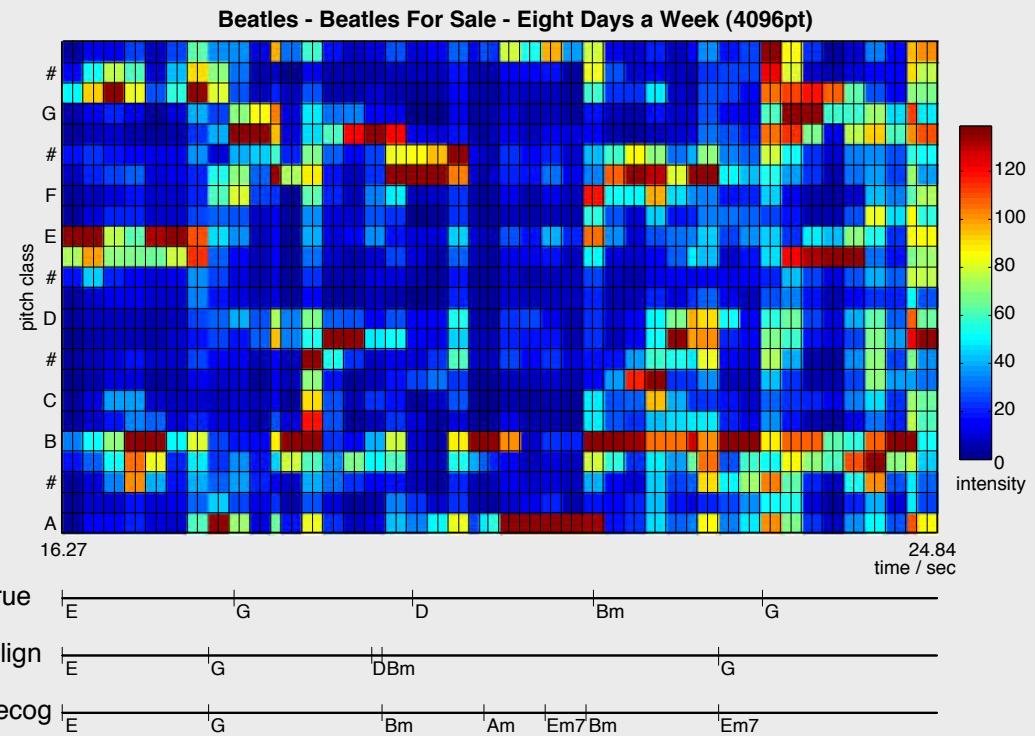
# Results

- Verify against human tapping data
  - vary tradeoff weight  $\alpha$
  - vary tempo estimate  $\tau$



# Chord Recognition

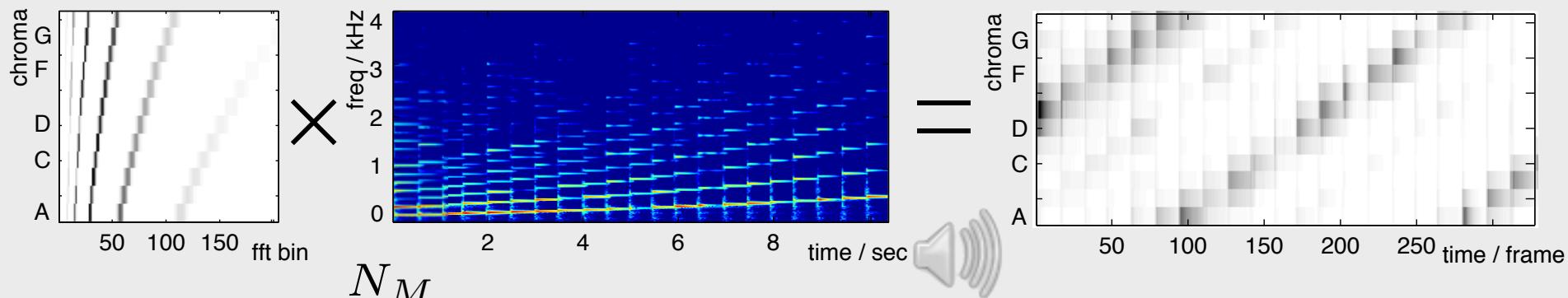
- Do people hear simultaneous notes or do they learn the sound of chords?
  - music limits the likely combinations
  - chords have a definite “color”
- Recognize chords instead of notes?
  - labeled data available
  - analogous to speech recognition



# Chord Features: Chroma

Fujishima 1999

- Idea: Project all energy onto **12 semitones** regardless of **octave**
  - maintains main “musical” distinction
  - **invariant** to musical equivalence
  - no need to worry about **harmonics?**



$$C(b) = \sum_{k=0}^{N_M} B(12 \log_2(k/k_0) - b) W(k) |X[k]|$$

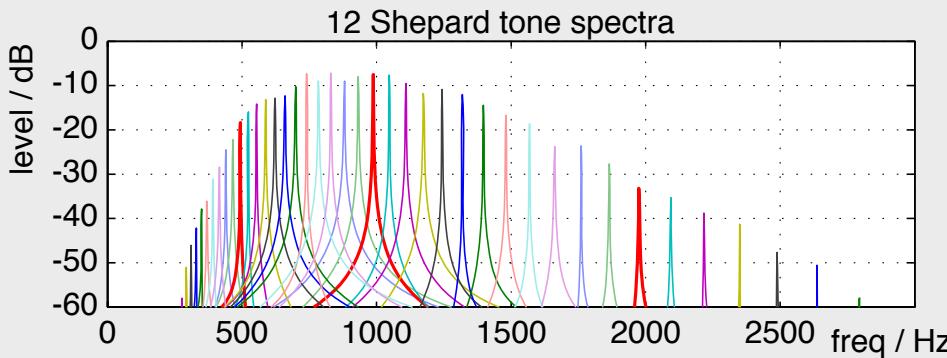
- $W(k)$  is weighting,  $B(b)$  selects every  $\sim \text{mod } 12$

# Chroma Resynthesis

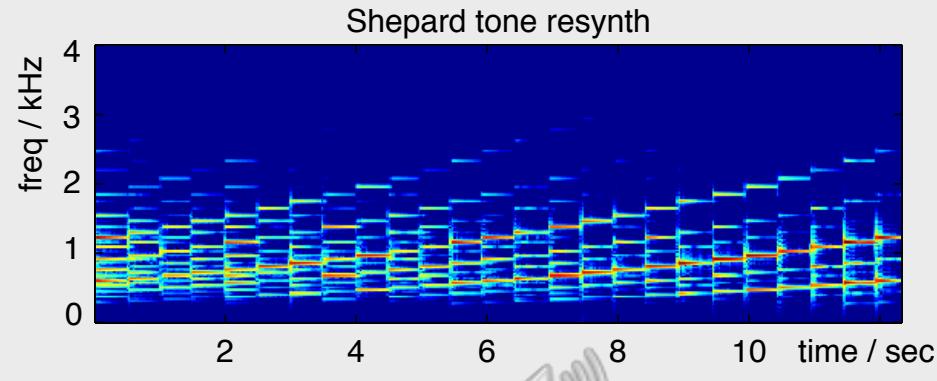
Ellis & Poliner 2007

- Chroma describes the notes in an octave
  - ... but not the octave
- Can resynthesize by presenting all octaves
  - ... with a smooth envelope
  - “Shepard tones” - octave is ambiguous

$$y_b(t) = \sum_{o=1}^M W(o + \frac{b}{12}) \cos 2^{o+\frac{b}{12}} w_0 t$$

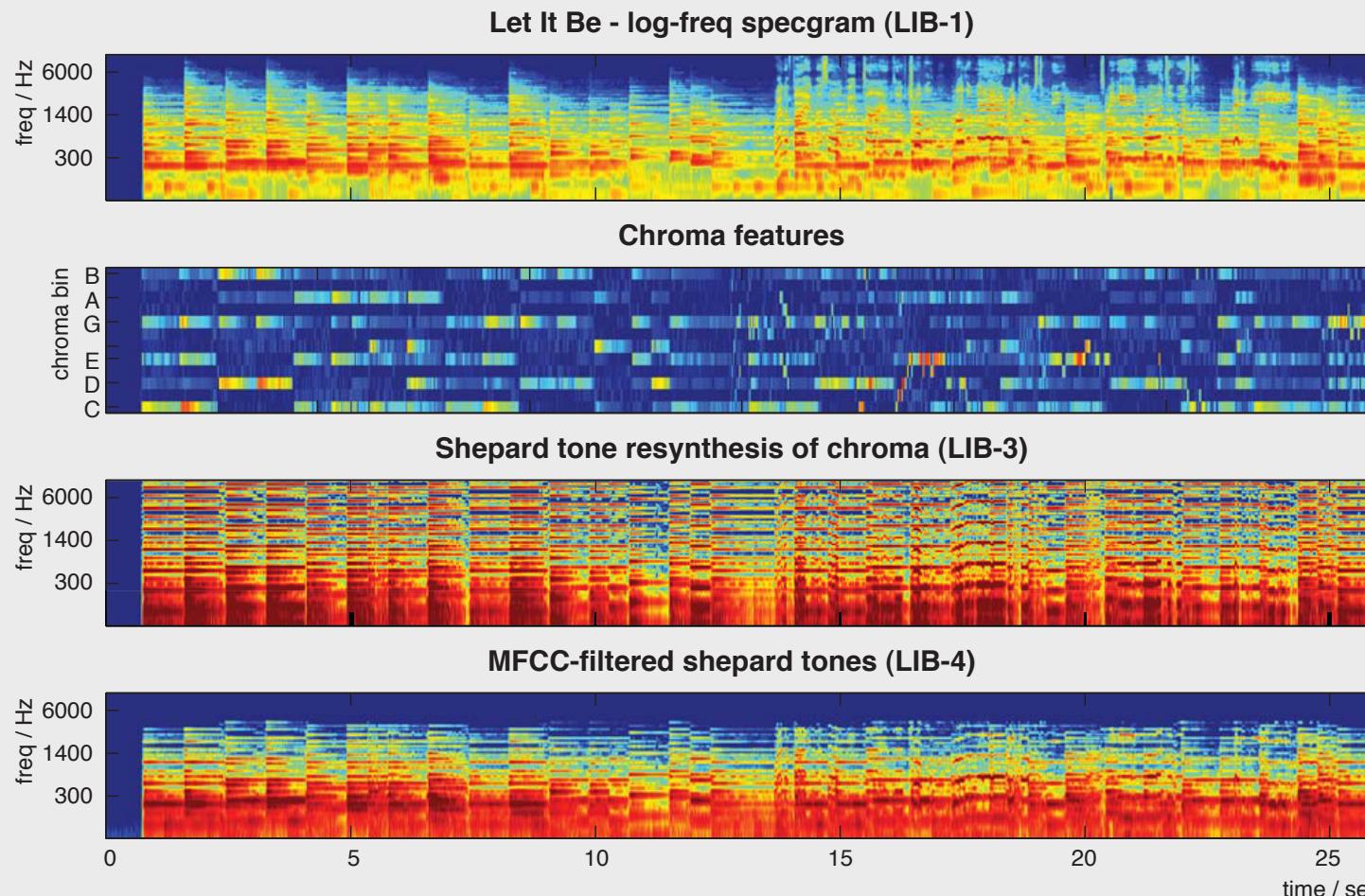


- endless sequence illusion



# Chroma Resynthesis

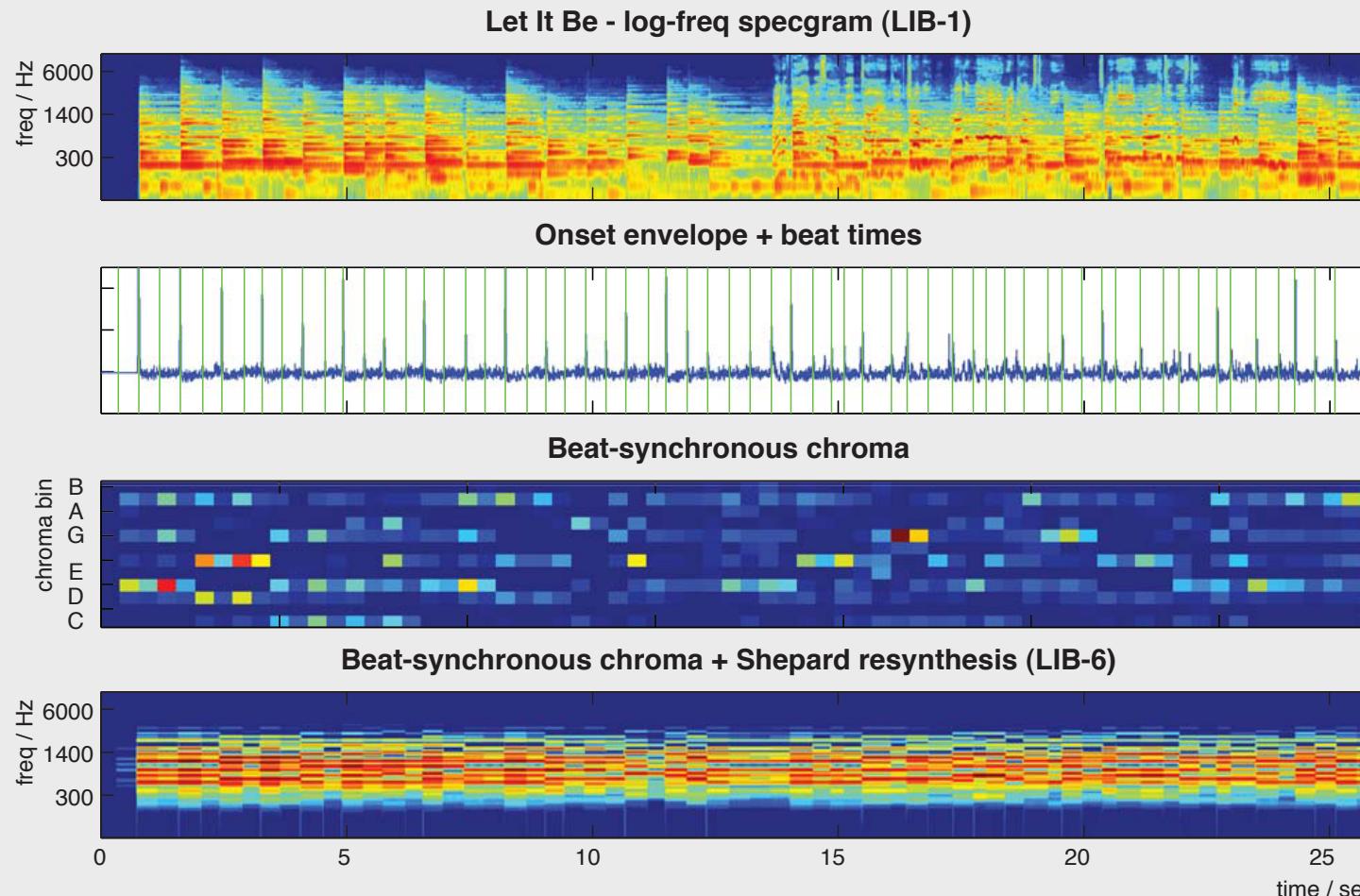
- **Resynthesis** illustrates what has been captured
  - can combine with **MFCC** features for coarse spectrum



# Beat-Synchronous Chroma

Bartsch & Wakefield '01

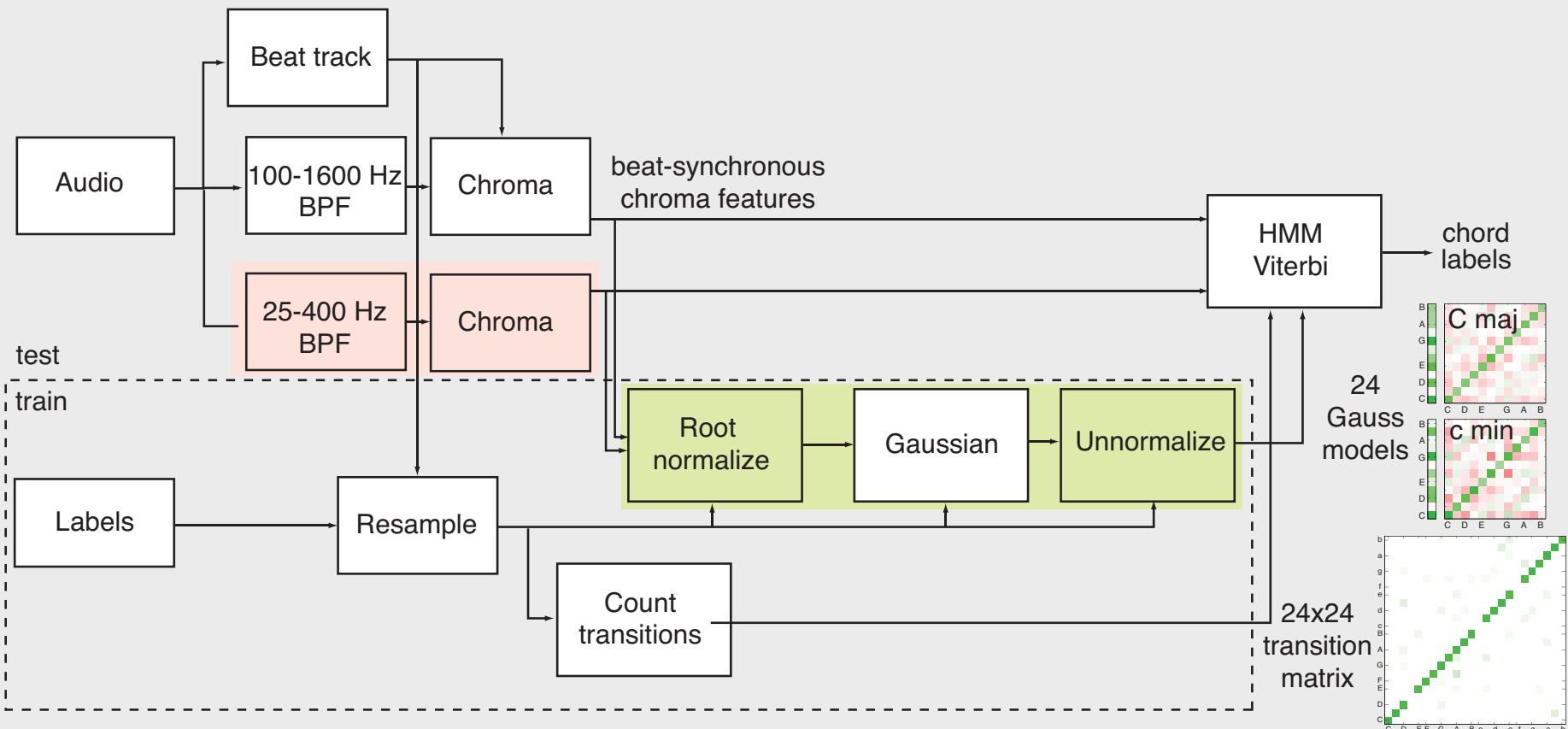
- Store just one chroma frame per beat
  - a compact representation of musical content



# Chord Recognition System

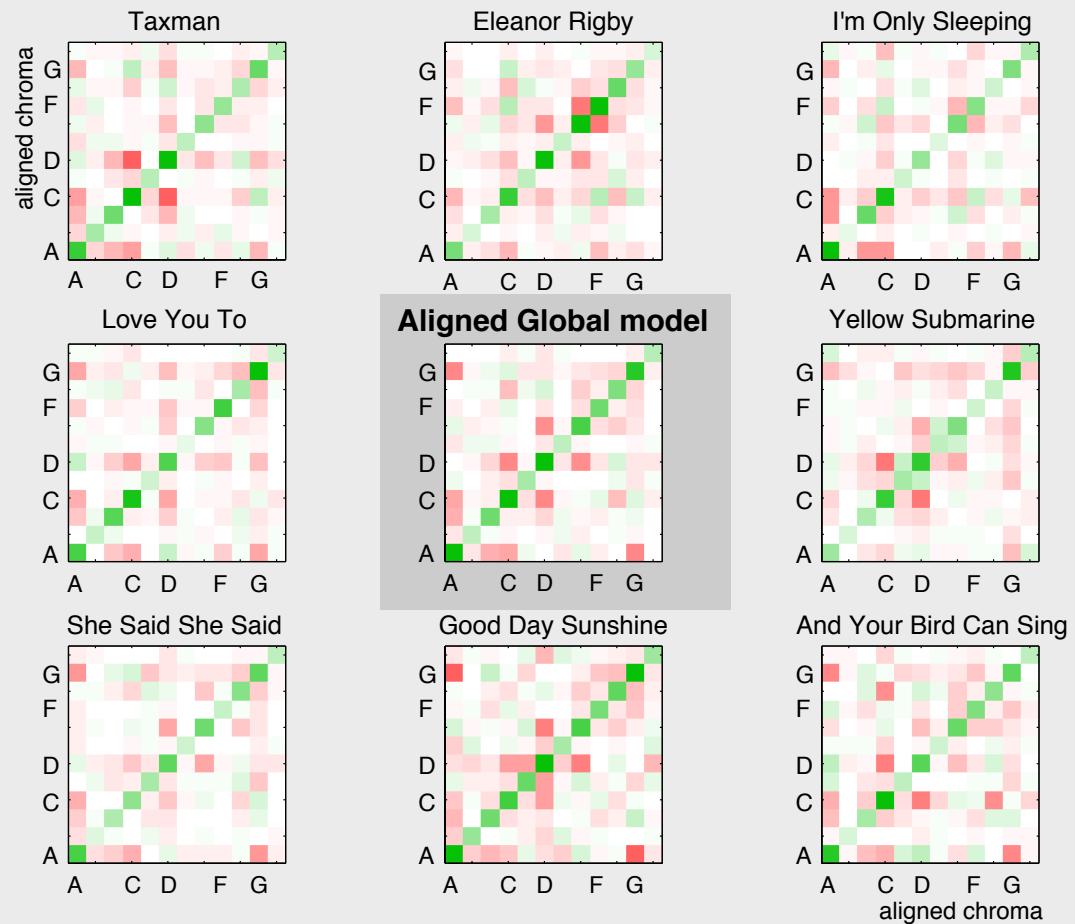
Sheh & Ellis '03

- Analogous to speech recognition
  - Gaussian models of features for each chord
  - Hidden Markov Models for chord transitions



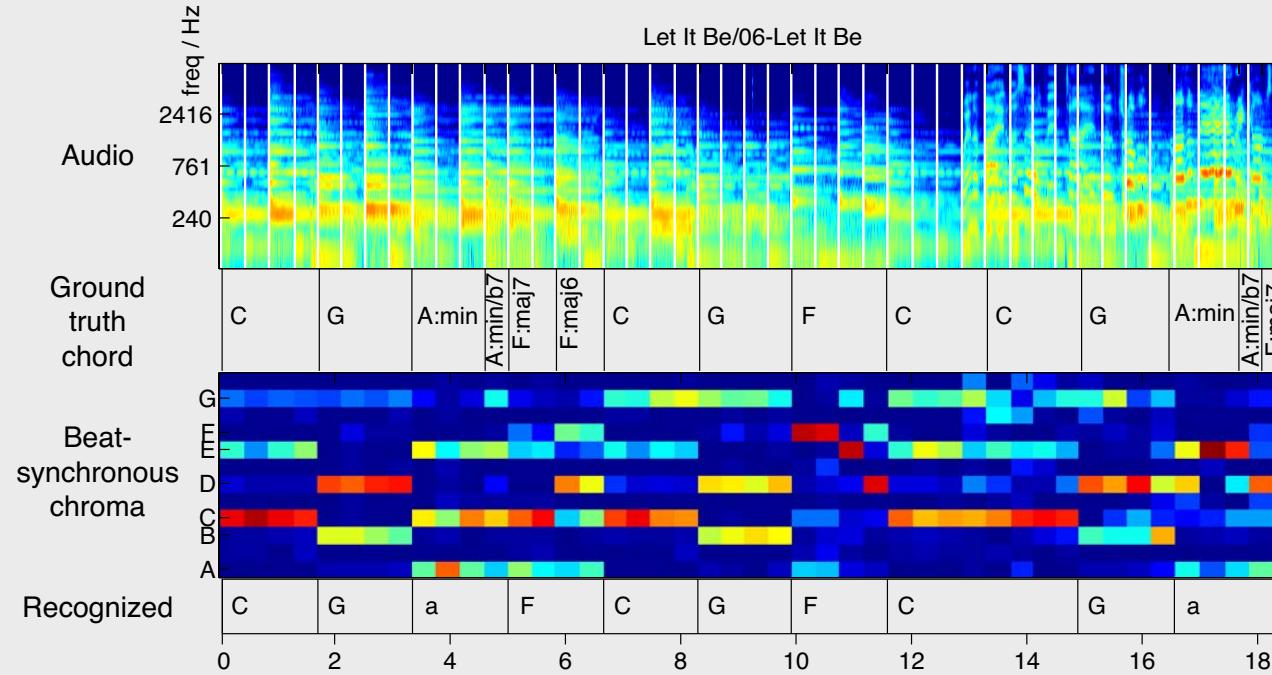
# Key Normalization

- Chord transitions depend on **key** of piece
  - dominant, relative minor, etc...
- Chord transition probabilities should be **key-relative**
  - estimate main key of piece
  - rotate all chroma features
  - learn models



# Chord Recognition

- Often works:



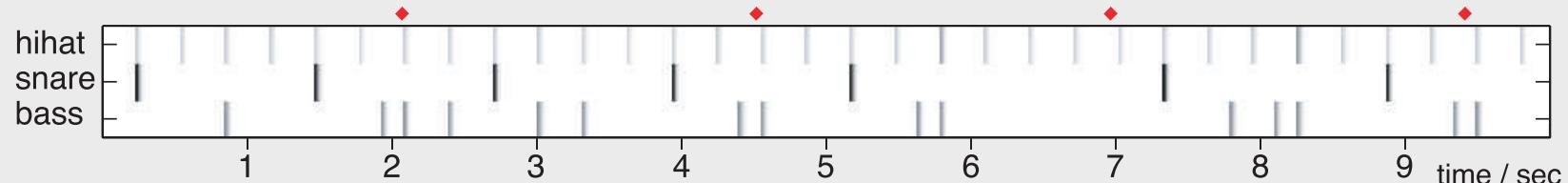
- But not always:

	12 chroma	+bass
indep. models	0.539	0.552
pooled models	0.556	0.578

# Eigenrhythms: Drum Pattern Space

Ellis & Arroyo '04

- Pop songs built on repeating “drum loop”
  - variations on a few bass, snare, hi-hat patterns



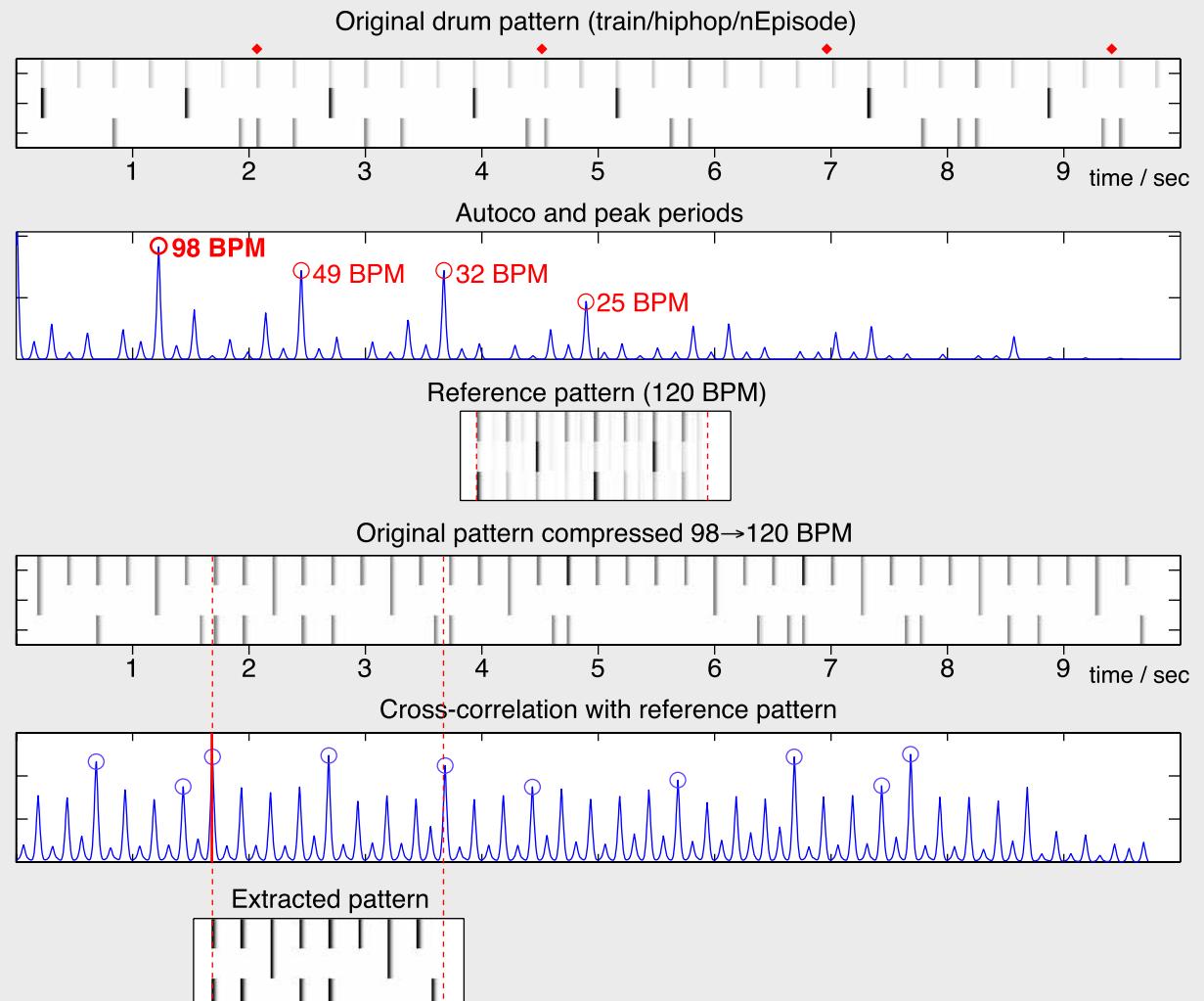
- Eigen-analysis (or ...) to capture variations?
  - by analyzing lots of (MIDI) data, or from audio
- Applications
  - music categorization
  - “beat box” synthesis
  - insight

# Aligning the Data

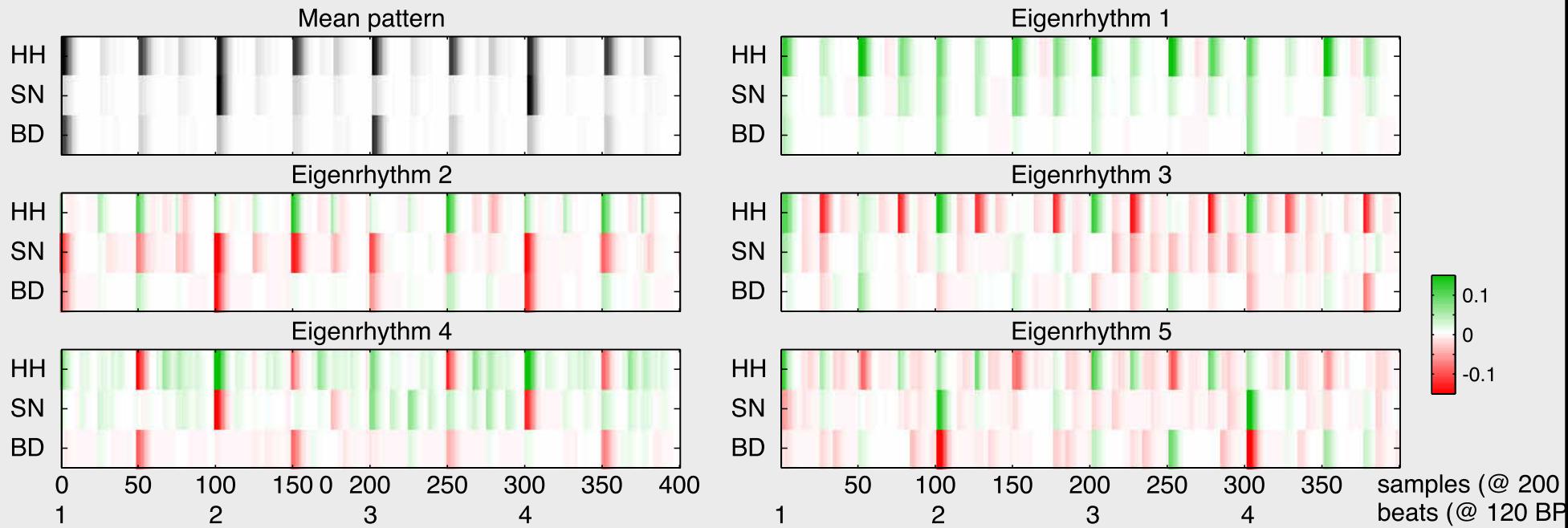
- Need to align patterns prior to modeling...

**tempo** (stretch):  
by inferring BPM &  
normalizing

**downbeat** (shift):  
correlate against  
'mean' template

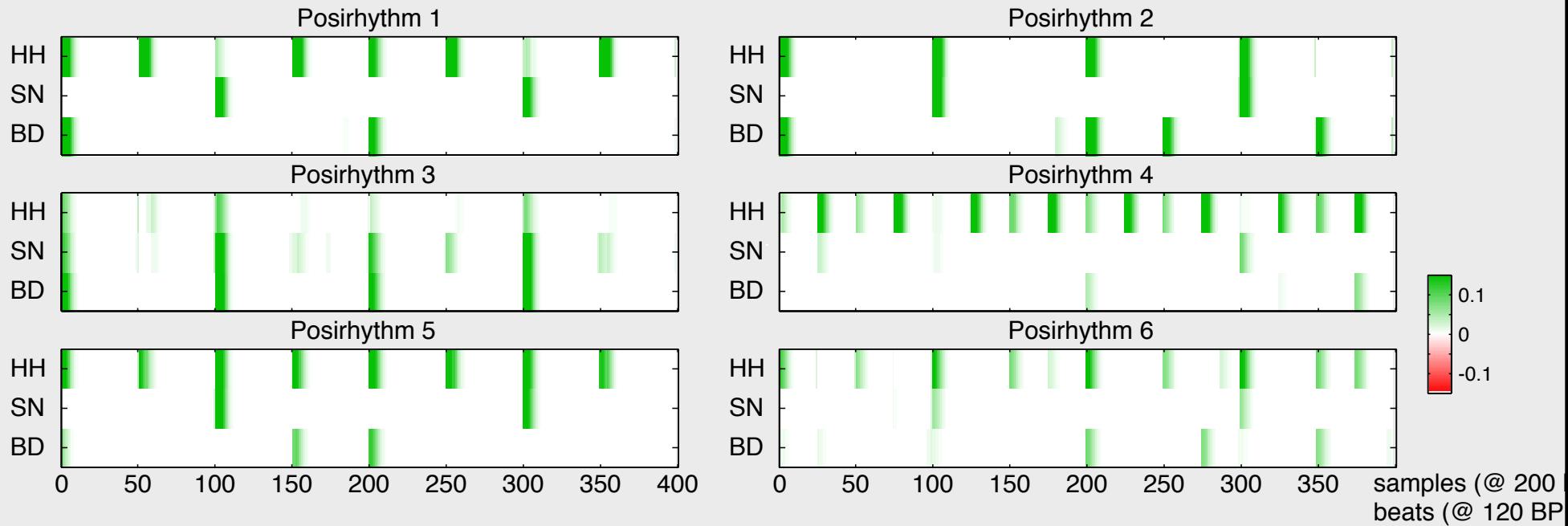


# Eigenrhythms (PCA)



- Need 20+ Eigenvectors for good coverage of 100 training patterns (1200 dims)
- Eigenrhythms both **add** and **subtract**

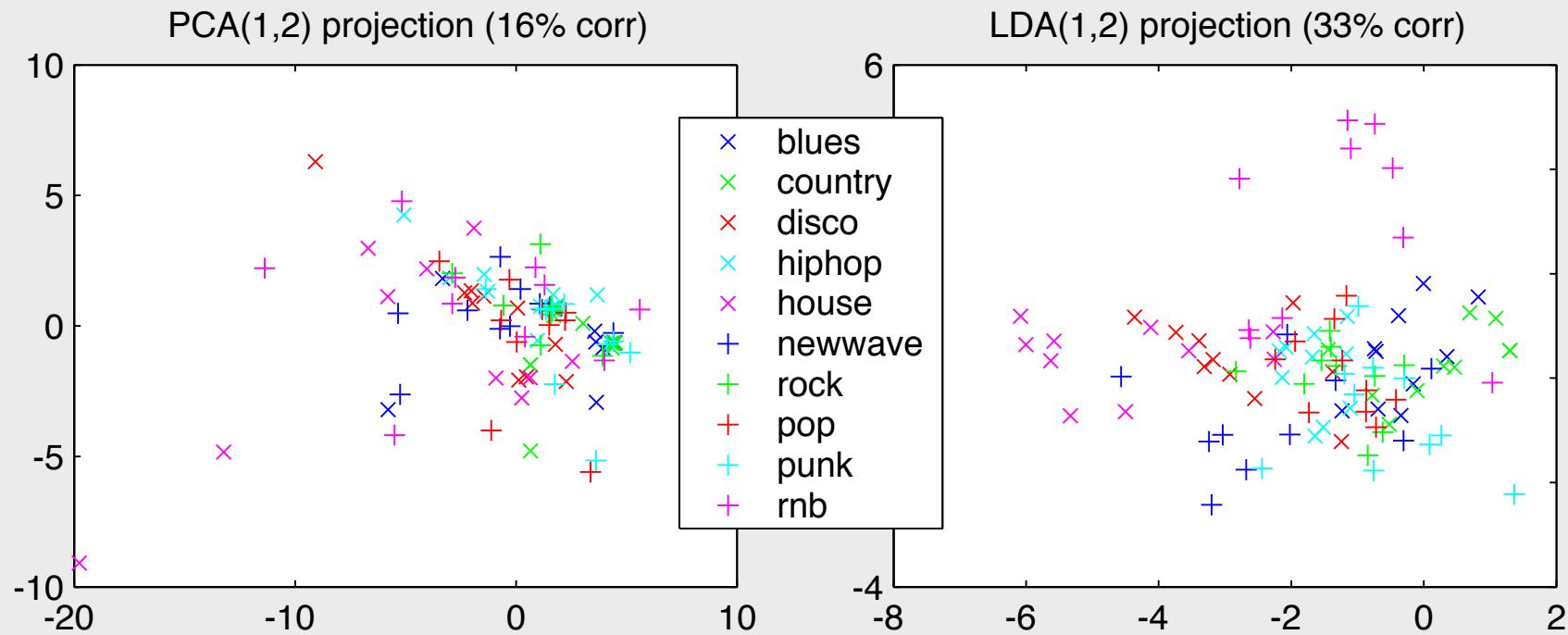
# Posirhythms (NMF)



- Nonnegative: only adds beat-weight
- Capturing some structure...

# Eigenrhythms for Classification

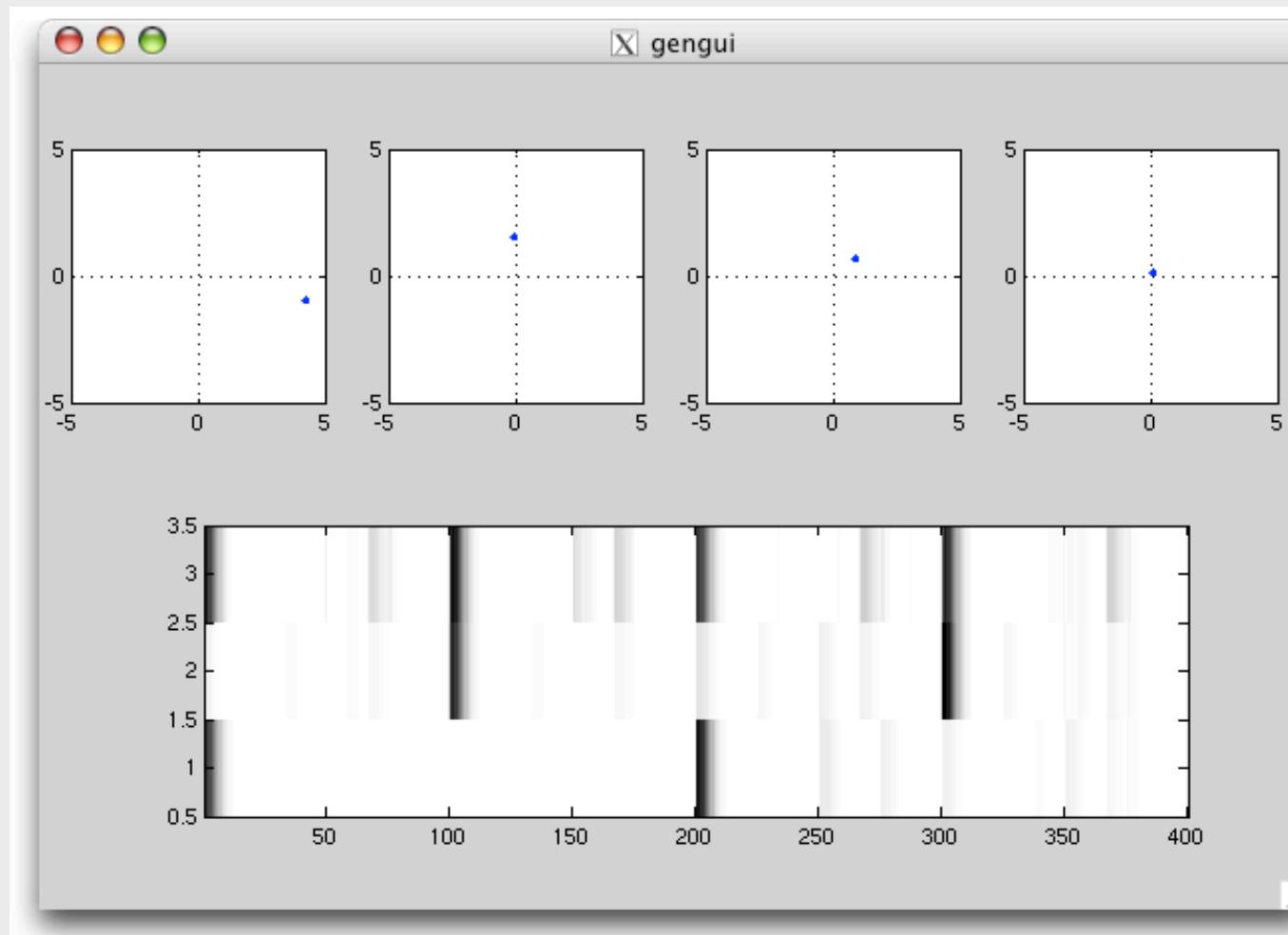
- **Projections** in Eigenspace / LDA space



- **10-way Genre classification (nearest nbr):**
  - PCA3: 20% correct
  - LDA4: 36% correct

# Eigenrhythm BeatBox

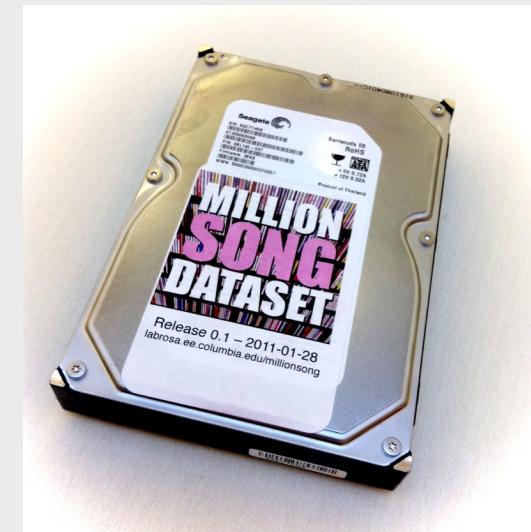
- Resynthesize rhythms from eigen-space



# 4. Large Music Audio Datasets

Bertin-Mahieu et al '11

- Music Information Retrieval (**MIR**) is a vibrant new field
  - many commercial opportunities
- But: music audio is hard to **share**
  - copyright owners have been burned
  - researchers use personal collections...
- Idea: **Million Song Dataset (MSD)**
  - commercial scale
  - available to all
  - many different “facets”
  - <http://labrosa.ee.columbia.edu/millionsong>



# MSD Facets

- Features,  
Lyrics,  
Tags,  
Covers,  
Listeners ...



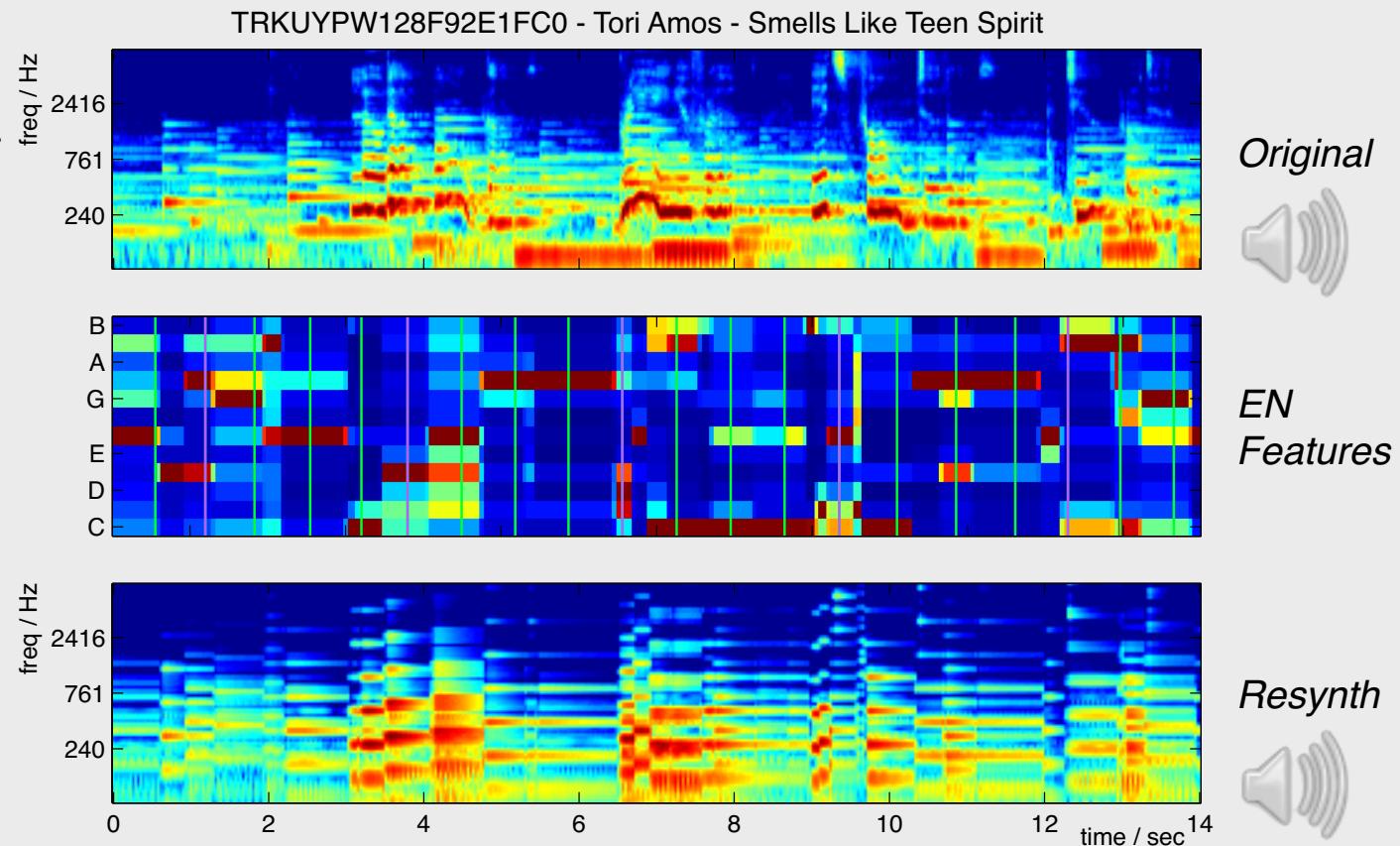
# MSD Audio Features

- Use Echo Nest “Analyze” features

- segment audio into variable-length “events”

- represent by  
12 chroma +  
12 “timbre”

- supports  
a crude  
resynthesis:



# MSD Metadata

## EN Metadata

```
artist: 'Tori Amos'  
release: 'LIVE AT MONTREUX'  
title: 'Smells Like Teen Spirit'  
id: 'TRKUYPW128F92E1FC0'  
key: 5  
mode: 0  
loudness: -16.6780  
tempo: 87.2330  
time_signature: 4  
duration: 216.4502  
sample_rate: 22050  
audio_md5: '8'  
7digitalid: 5764727  
familiarity: 0.8500  
year: 1992
```

## Last.fm Tags

100.0 – cover	5.0 – cover songs
57.0 – covers	4.0 – soft rock
43.0 – female vocalists	4.0 – nirvana cover
42.0 – piano	4.0 – Mellow
34.0 – alternative	4.0 – alternative rock
14.0 – singer-songwriter	3.0 – chick rock
11.0 – acoustic	3.0 – Ballad
8.0 – tori amos	3.0 – Awesome Covers
7.0 – beautiful	2.0 – melancholic
6.0 – rock	2.0 – k001 ch1x
6.0 – pop	2.0 – indie
6.0 – Nirvana	2.0 – female vocalistist
6.0 – female vocalist	2.0 – female
6.0 – 90s	2.0 – cover song
5.0 – out of genre covers	2.0 – american

## SHS Covers

```
%5489,4468, Smells Like Teen Spirit  
TRTUOVJ128E078EE10 Nirvana  
TRFZJOZ128F4263BE3 Weird Al Yankovic  
TRJHCKN12903CDD274 Pleasure Beach  
TRELTOJ128F42748B7 The Flying Pickets  
TRJKBXL128F92F994D Rhythms Del Mundo feat. Shanade  
TRIHLAW128F429BBF8 The Bad Plus  
TRKUYPW128F92E1FC0 Tori Amos
```

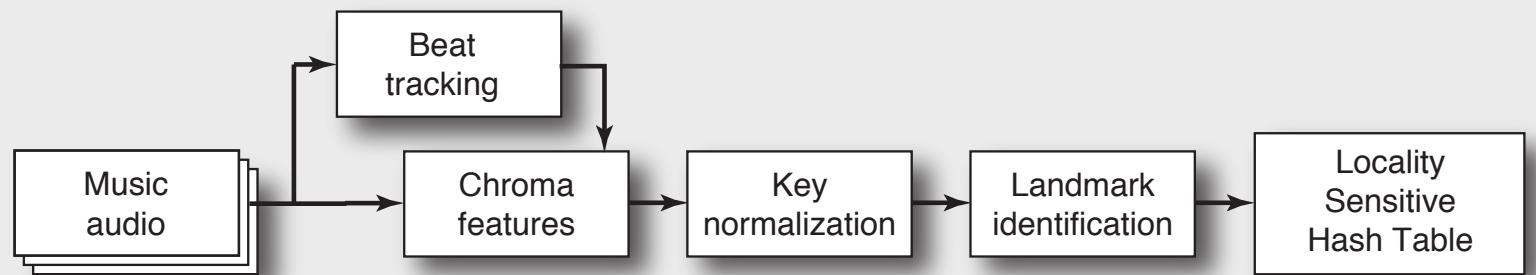
## MxM Lyric Bag-of-Words

12 hello	6 here	3 is
11 i	6 us	3 with
10 a	6 entertain	3 oh
9 and	4 the	3 out
7 it	4 feel	3 an
6 are	4 yeah	3 light
6 we	3 to	3 less
6 now	3 my	3 danger

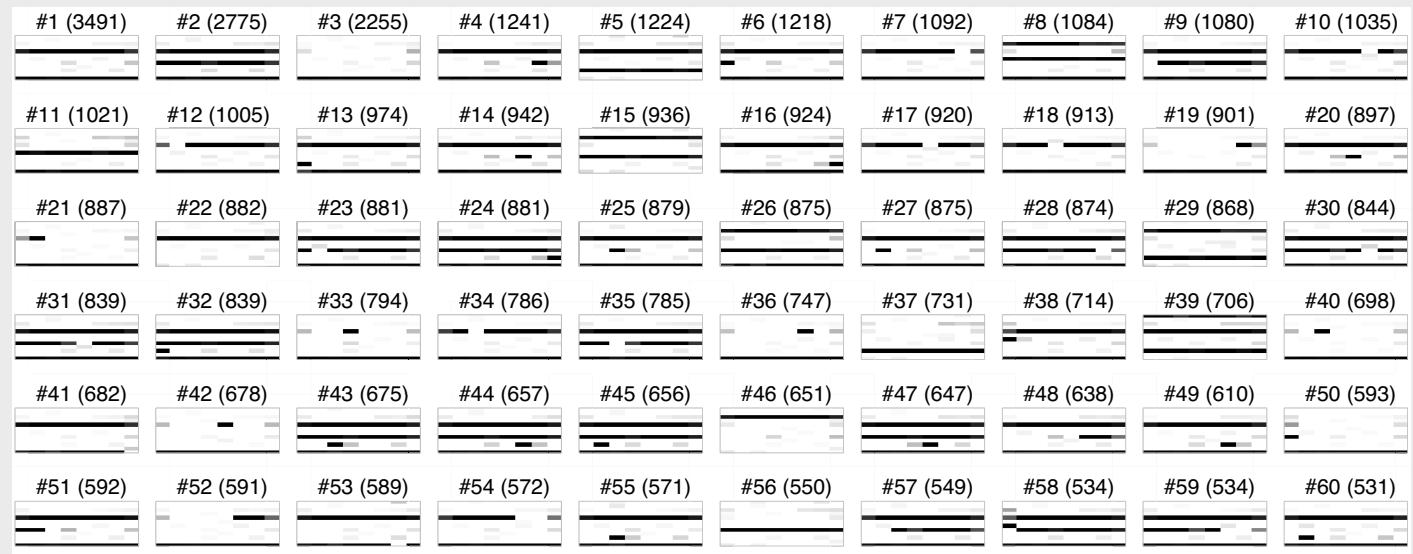
# Melodic-Harmonic Mining

Bertin-Mahieux et al. '10

- What can you find in a million songs?
  - what characterizes the content?

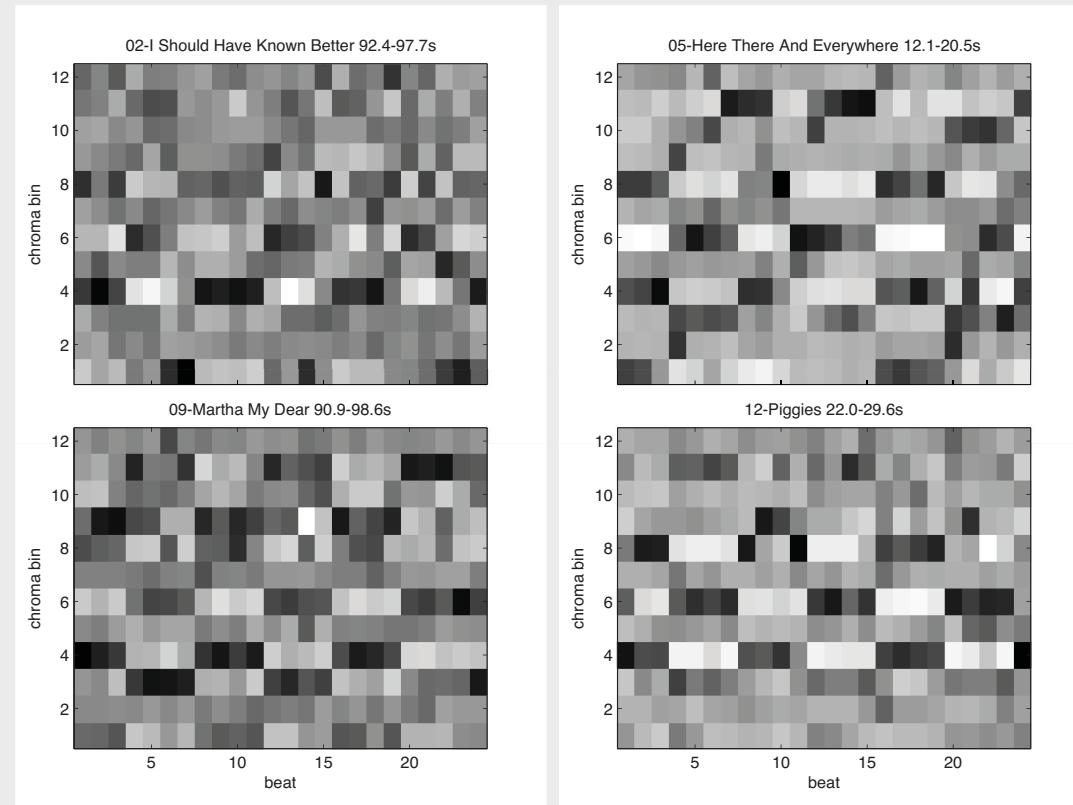


- Frequent clusters of  $12 \times 8$  binarized event-chroma



# Results - Beatles

- Over 86 Beatles tracks
- All beat offsets = 41,705 patches
  - LSH takes 300 sec - approx NlogN in patches?
- High-pass along time
  - to avoid sustained notes
- Song filter
  - remove hits in same track



# 5. Outstanding Issues

- **Perceptually Inspired?**
  - Music Perception is complex:  
Structure  
Expectation  
Memory  
Enjoyment
- **Many problems still to solve**
  - structure
  - metrical hierarchy
  - music similarity & preference

# Summary

- **Machine Listening:**  
Getting useful information from sound
- **Musical sound**  
... constructed to confound scene analysis?
- **Transcription tasks**  
... recover notes, beats, chords etc.
- **Million Song Dataset** for research  
... large-scale, multiple facets

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