

## Lecture 11: Signal Separation

- 1 Sound Mixture Organization
- 2 Computational Auditory Scene Analysis
- 3 Independent Component Analysis
- 4 Model-Based Separation

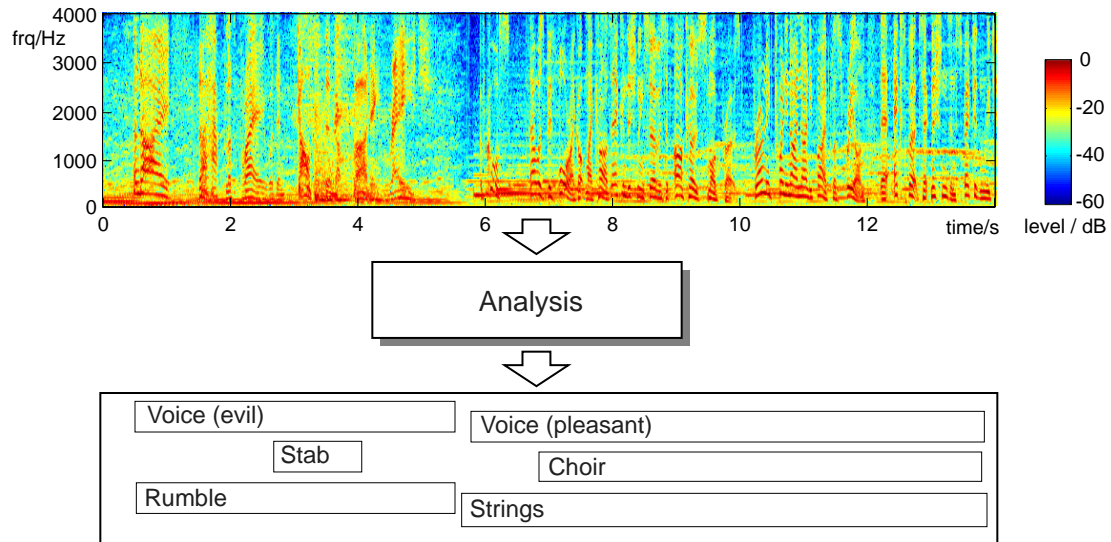
Dan Ellis <[dpwe@ee.columbia.edu](mailto:dpwe@ee.columbia.edu)>  
<http://www.ee.columbia.edu/~dpwe/e6820/>

Columbia University Dept. of Electrical Engineering  
Spring 2006



# 1

## Sound Mixture Organization



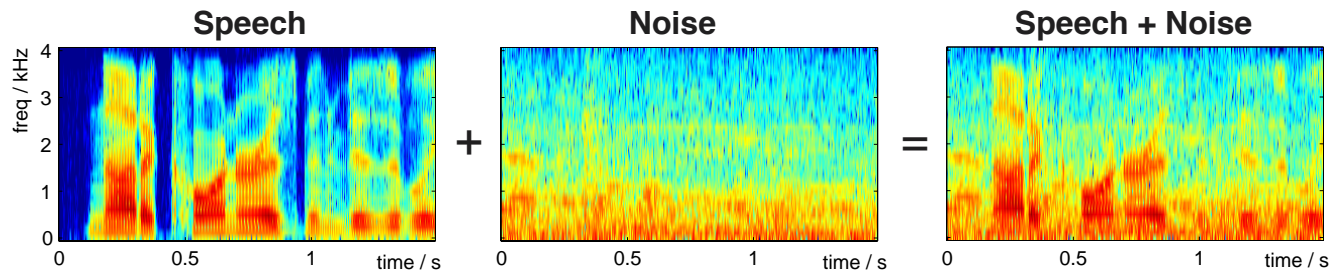
- **Auditory Scene Analysis:** describing a complex sound in terms of high-level sources / events
  - ... like listeners do
- **Hearing is ecologically grounded**
  - reflects 'natural scene' properties
  - subjective, not absolute



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# Sound, mixtures, and learning



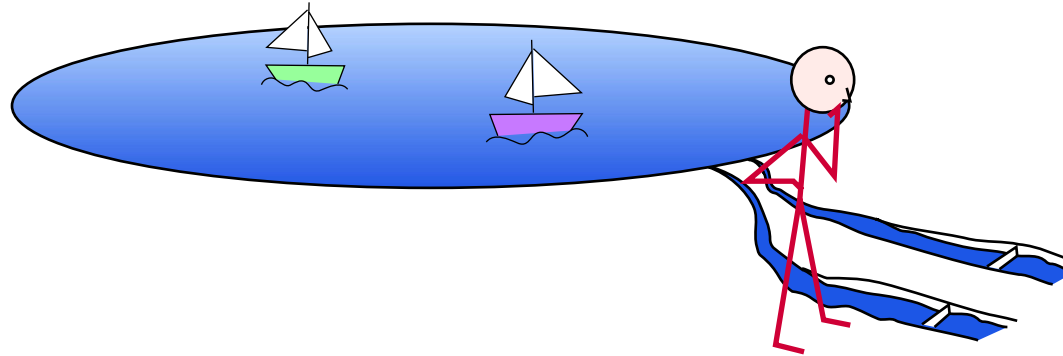
- **Sound**
  - carries useful information about the world
  - complements vision
- **Mixtures**
  - .. are the rule, not the exception
  - medium is 'transparent', sources are many
  - must be handled!
- **Learning**
  - the 'speech recognition' lesson:  
let the data do the work
  - like listeners



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## The problem with recognizing mixtures



*“Imagine two narrow channels dug up from the edge of a lake, with handkerchiefs stretched across each one. Looking only at the motion of the handkerchiefs, you are to answer questions such as: How many boats are there on the lake and where are they?” (after Bregman’90)*

- **Received waveform is a mixture**
  - two sensors,  $N$  signals ... **underconstrained**
- **Disentangling mixtures as the primary goal?**
  - perfect solution is not possible
  - need experience-based **constraints**



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# Approaches to sound mixture recognition

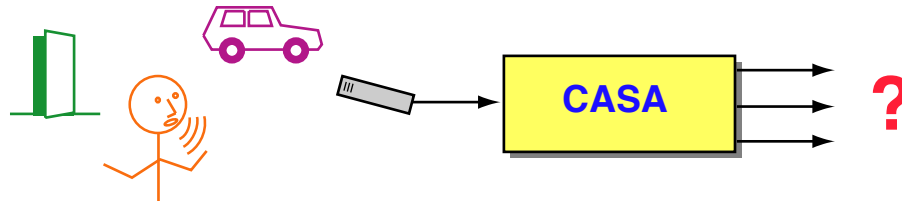
- **Separate signals, then recognize**
  - e.g. Computational Auditory Scene Analysis (CASA), Independent Component Analysis (ICA)
  - nice, if you can do it
- **Recognize combined signal**
  - 'multicondition training'
  - combinatorics..
- **Recognize with parallel models**
  - full joint-state space?
  - divide signal into fragments, then use missing-data recognition



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## What is the goal of CASA?



- **Separate signals?**
  - output is unmixed waveforms
  - underconstrained, very hard ...
  - too hard? not required?
- **Source classification?**
  - output is set of event-names
  - listeners do more than this...
- **Something in-between?**  
**Identify independent sources + characteristics**
  - standard task, results?

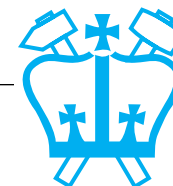


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## Segregation vs. Inference

- **Source separation requires attribute separation**
  - sources are characterized by attributes (pitch, loudness, timbre + finer details)
  - need to identify & gather different attributes for different sources ...
- **Need representation that segregates attributes**
  - spectral decomposition
  - periodicity decomposition
- **Sometimes values can't be separated**
  - e.g. unvoiced speech
  - maybe **infer** factors from probabilistic model?
$$p(O, x, y) \rightarrow p(x, y | O)$$
  - or: just skip those values, **infer** from higher-level context



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# Outline

- 1 Sound Mixture Organization
- 2 **Computational Auditory Scene Analysis**
  - Human Auditory Scene Analysis
  - Bottom-up and Top-down models
  - Evaluation
- 3 Independent Component Analysis
- 4 Model-Based Separation



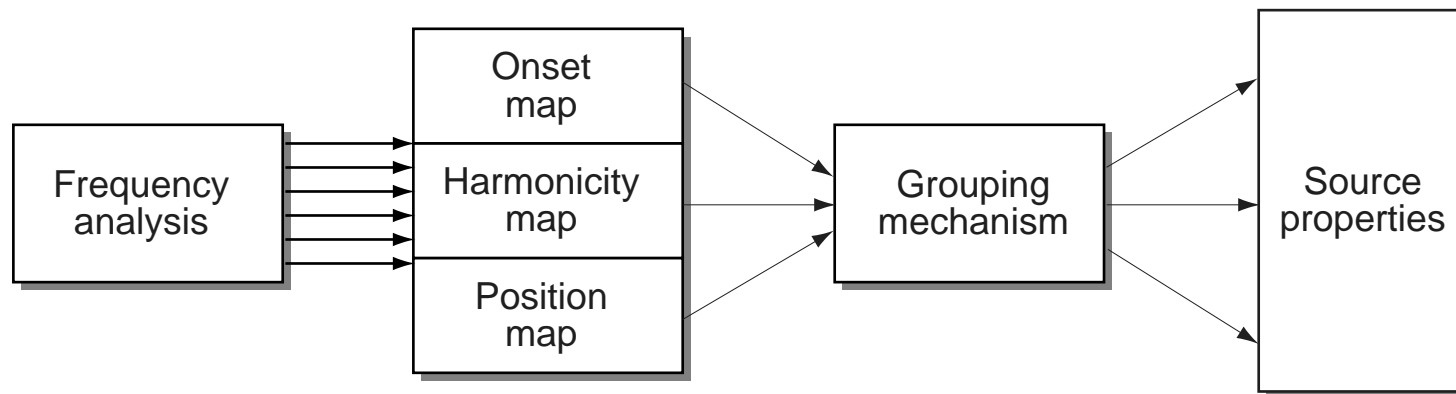


## 2

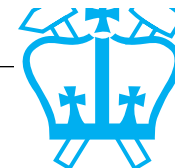
# Auditory Scene Analysis

(Bregman 1990)

- **How do people analyze sound mixtures?**
  - break mixture into small **elements** (in time-freq)
  - elements are **grouped** in to sources using **cues**
  - sources have aggregate **attributes**
- **Grouping 'rules' (Darwin, Carlyon, ...):**
  - cues: common onset/offset/modulation, harmonicity, spatial location, ...



(after Darwin, 1996)

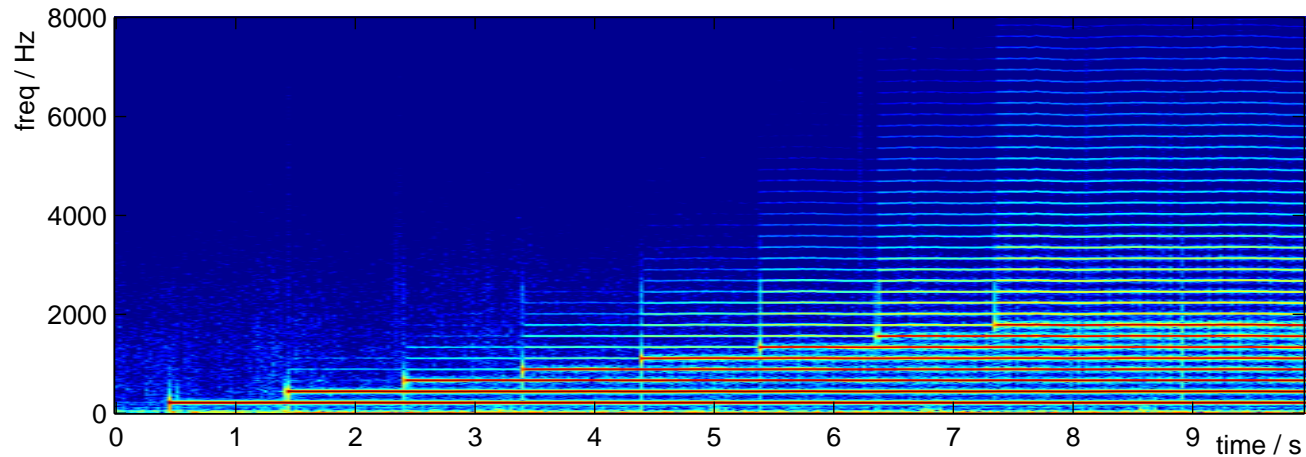


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# Cues to simultaneous grouping

- **Elements + attributes**



- **Common onset**
  - simultaneous energy has common source
- **Periodicity**
  - energy in different bands with same cycle
- **Other cues**
  - spatial (ITD/IID), familiarity, ...

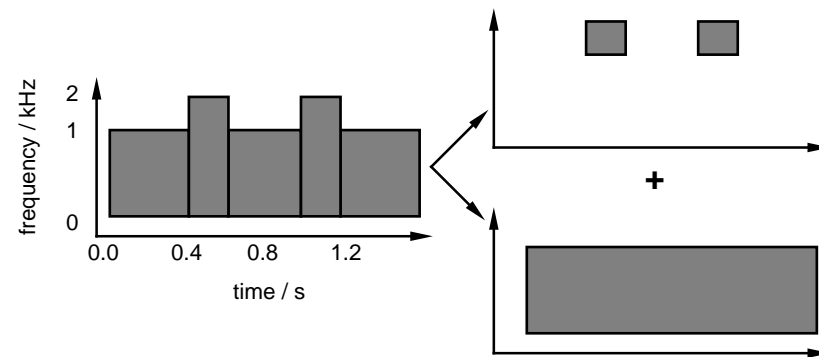


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## The effect of context

- **Context can create an ‘expectation’:**  
i.e. a bias towards a particular interpretation
- **e.g. Bregman’s “old-plus-new” principle:**  
A change in a signal will be interpreted as an *added* source whenever possible



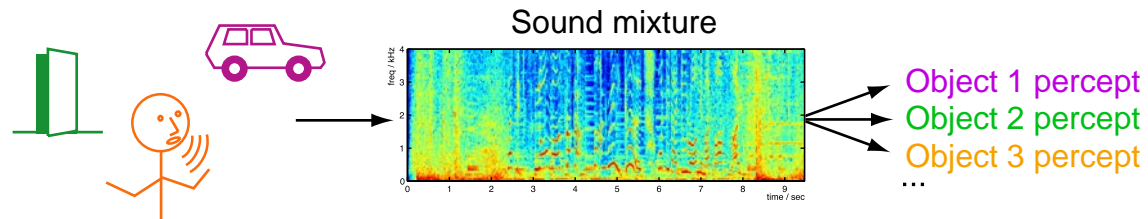
- a different division of the same energy depending on what preceded it



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# Computational Auditory Scene Analysis (CASA)

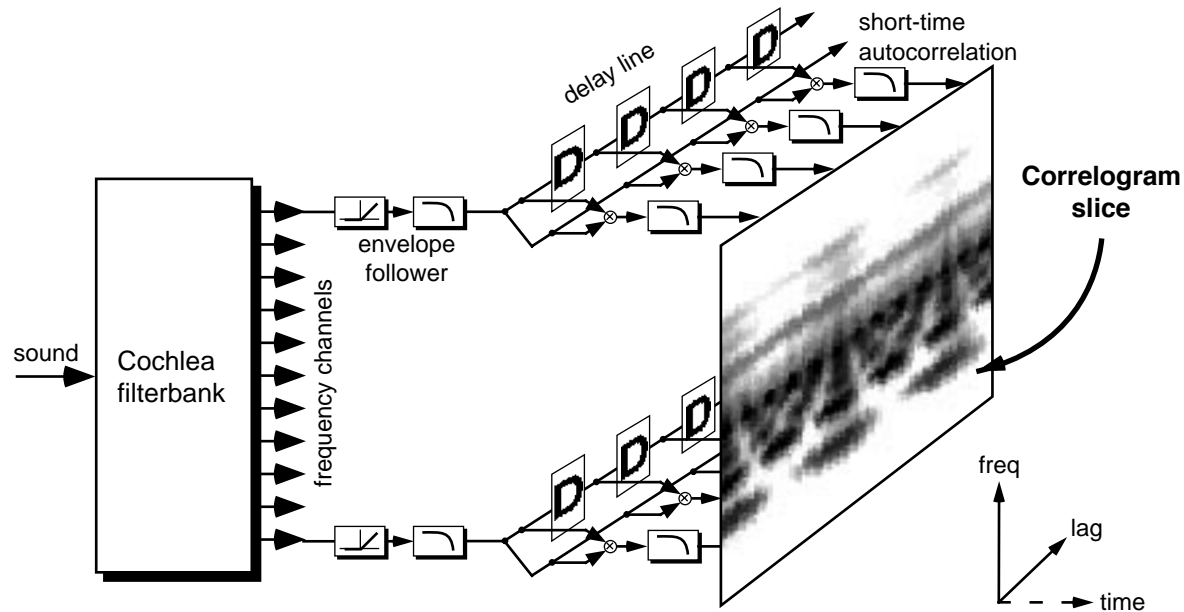


- **Goal: Automatic sound organization;**  
**Systems to ‘pick out’ sounds in a mixture**
  - ... like people do
- **E.g. voice against a noisy background**
  - to improve speech recognition
- **Approach:**
  - psychoacoustics describes grouping ‘rules’
  - ... just implement them?



# CASA front-end processing

- **Correlogram:**  
Loosely based on known/possible physiology



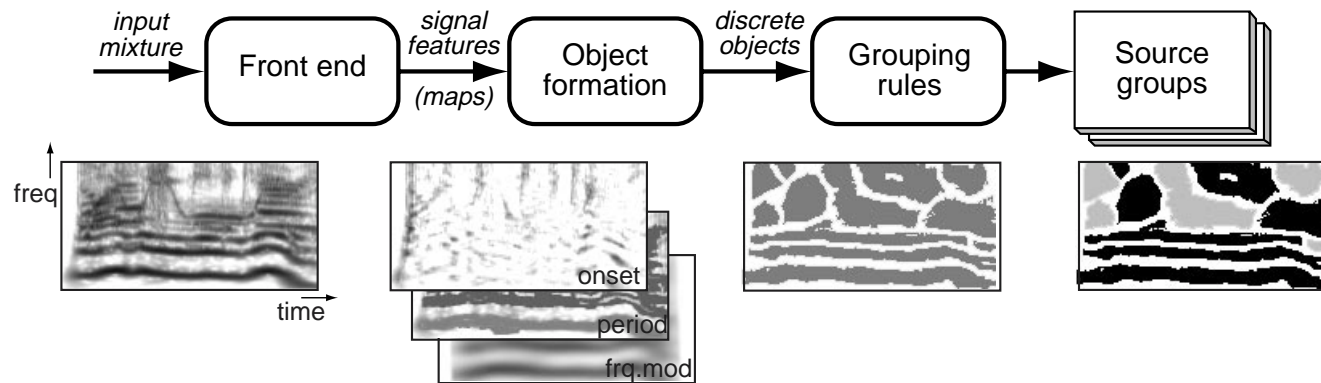
- linear filterbank cochlear approximation
- static nonlinearity
- zero-delay slice is like spectrogram
- periodicity from delay-and-multiply detectors



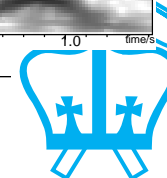
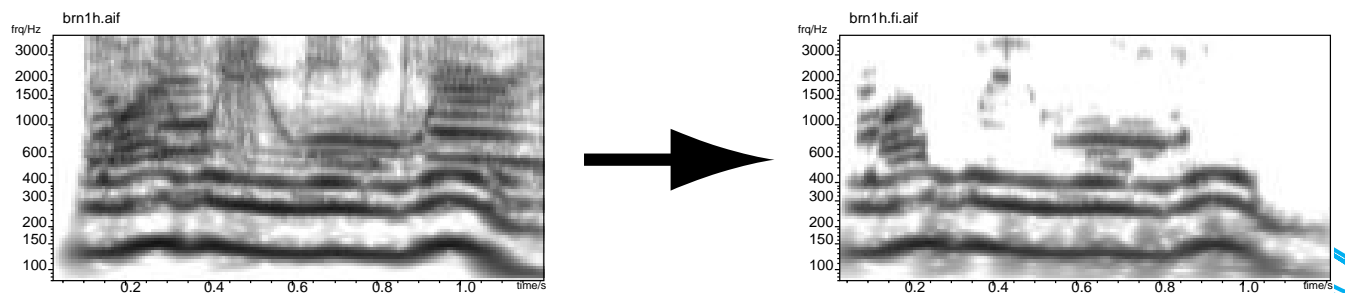
# The Representational Approach

(Brown & Cooke 1993)

- **Implement psychoacoustic theory**



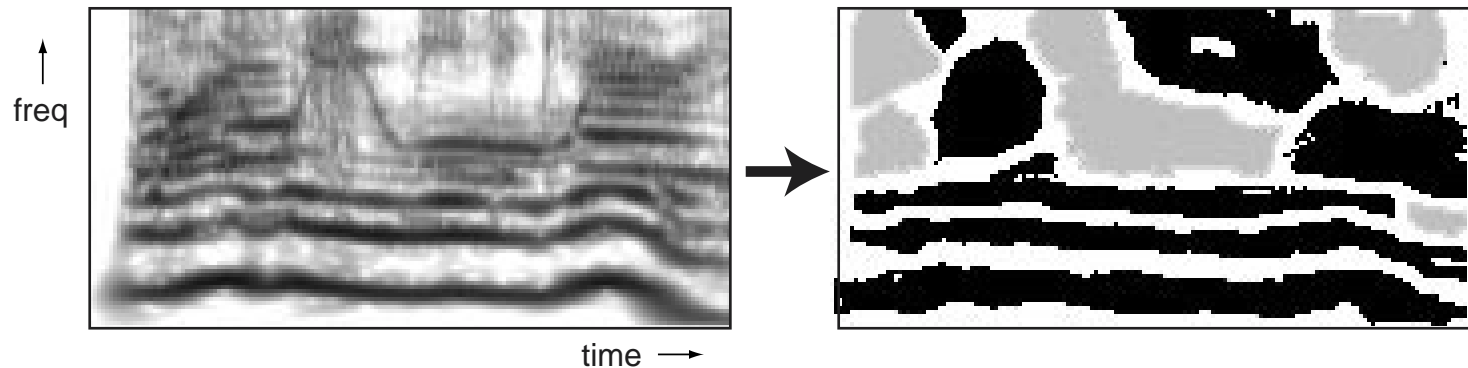
- 'bottom-up' processing
  - uses common onset & periodicity cues
- **Able to extract voiced speech:**



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## Problems with 'bottom-up' CASA



- **Circumscribing time-frequency elements**
  - need to have 'regions', but hard to find
- **Periodicity is the primary cue**
  - how to handle aperiodic energy?
- **Resynthesis via masked filtering**
  - cannot separate within a single t-f element
- **Bottom-up leaves no ambiguity or context**
  - how to model illusions?

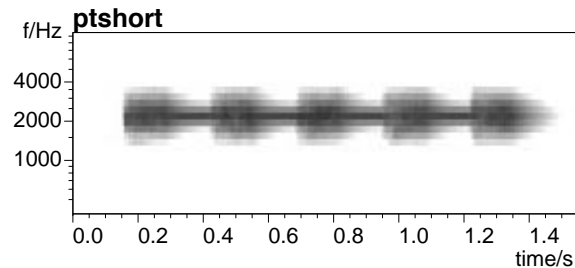


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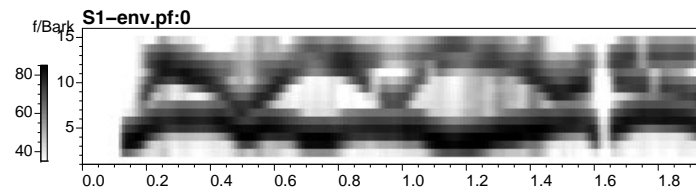
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## Restoration in sound perception

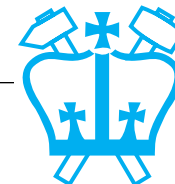
- Auditory ‘**illusions**’ = hearing what’s not there
- The continuity illusion



- Sinewave Speech (SWS)



- **duplex** perception
- What kind of **model** accounts for this?
  - is it an **important part** of hearing?





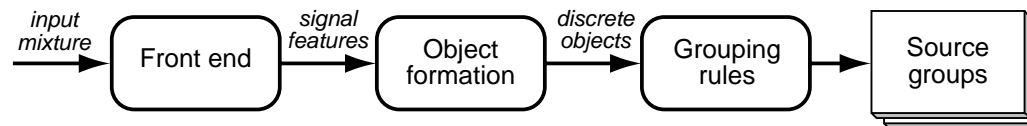
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# Adding top-down constraints: Prediction-Driven CASA (PDCASA)

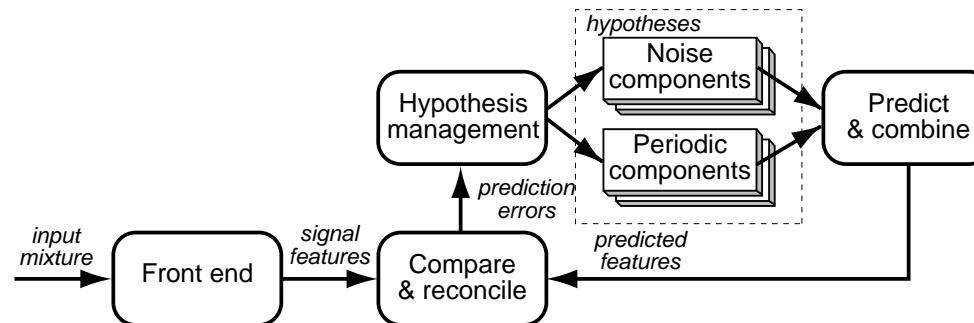
Perception is **not direct**  
but a **search** for plausible hypotheses

- **Data-driven (bottom-up)...**



- objects irresistibly appear

vs. **Prediction-driven (top-down)**

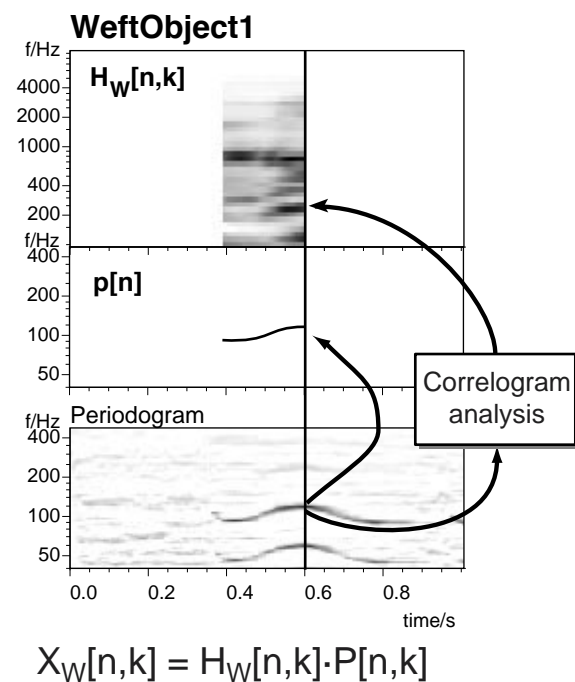
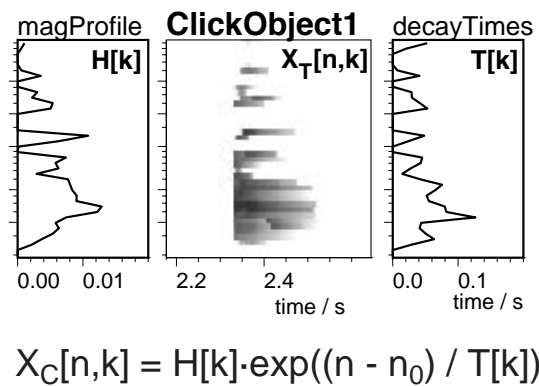
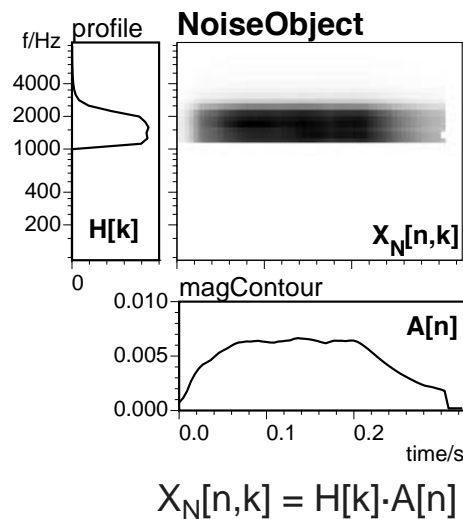


- match observations with a 'world-model'
- need world-model constraints...



# Generic sound elements for PDCASA

- **Goal is a representational space that**
  - covers real-world perceptual sounds
  - minimal parameterization (sparseness)
  - separate attributes in separate parameters

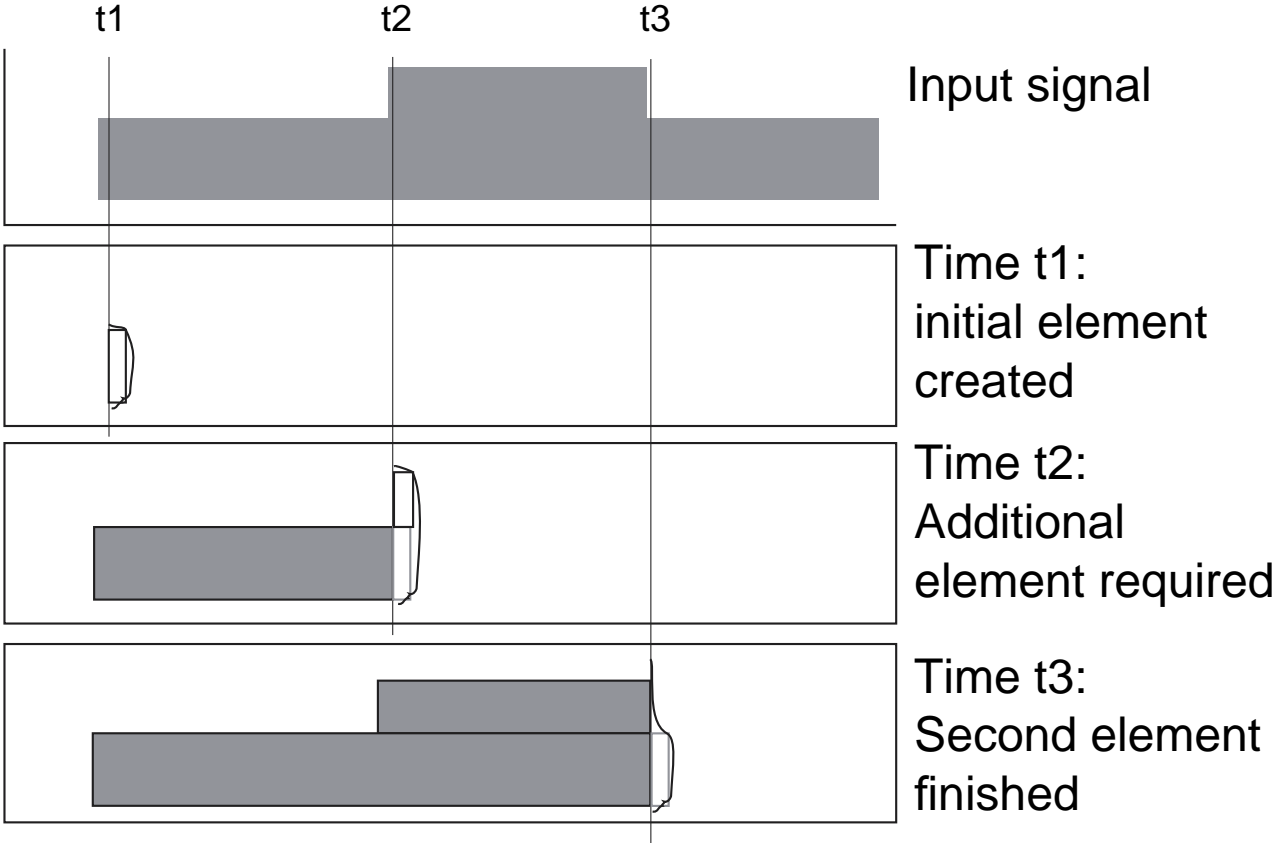


- **Object hierarchies built on top...**



# PDCASA for old-plus-new

- Incremental analysis

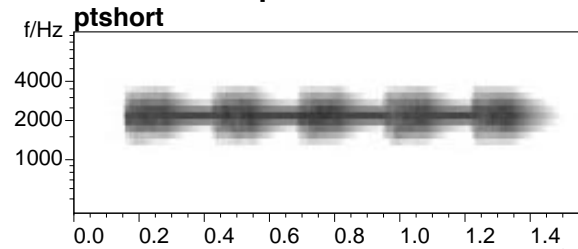


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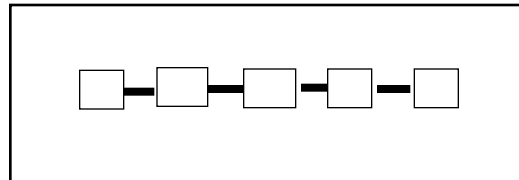
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## PDCASA for the continuity illusion

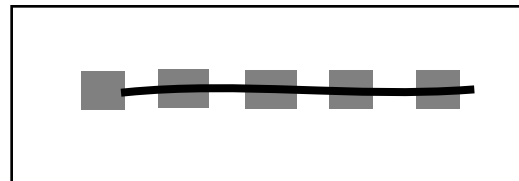
- **Subjects hear the tone as continuous**  
... if the noise is a plausible masker



- **Data-driven analysis gives just visible portions:**

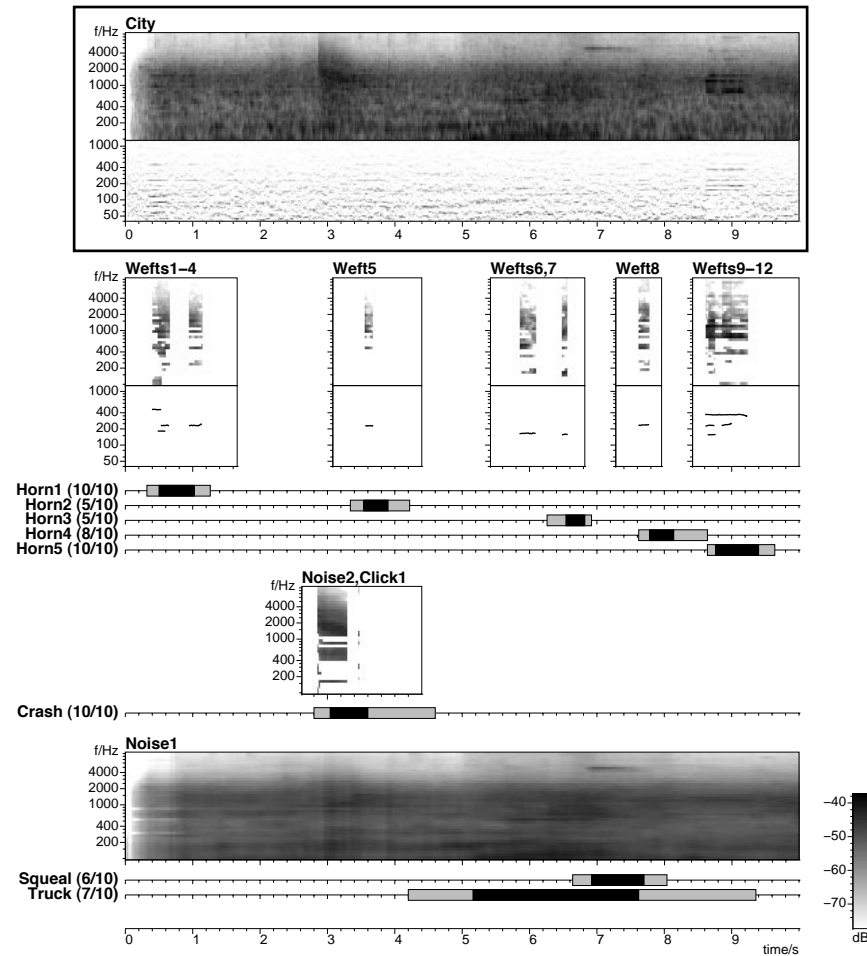


- **Prediction-driven can infer masking:**



# Prediction-Driven CASA

- **Explain** a complex sound with basic elements



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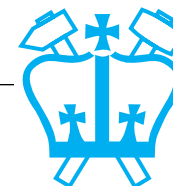
## Aside: Ground Truth

- **What do people hear in sound mixtures?**
  - do interpretations match?
- **Listening tests to collect ‘perceived events’:**

Subject dpwe / Example city / Part A

Names	Marks
horn 1	
crash	
squeal	<input type="checkbox"/>
horn 2	

Play Stop Go on...



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## Aside: Evaluation

- **Evaluation is a big problem for CASA**
  - what is the goal, really?
  - what is a good test domain?
  - how do you measure performance?
- **SNR improvement**
  - tricky to derive from before/after signals:  
correspondence problem
  - can do with fixed filtering mask;  
but rewards removing signal as well as noise
- **Speech Recognition (ASR) improvement**
  - recognizers typically very sensitive to artefacts
- **'Real' task?**
  - mixture corpus with specific sound events...



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# Outline

- 1 Sound Mixture Organization
- 2 Computational Auditory Scene Analysis
- 3 Independent Component Analysis**
  - Blind source separation
  - Independence and kurtosis
  - Limits of the approach
- 4 Model-Based Separation

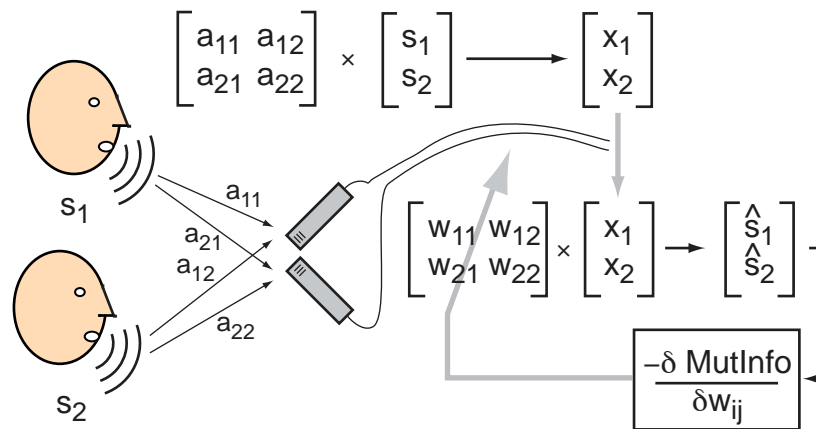




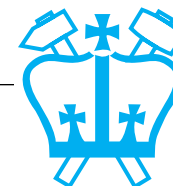
# 3 Independent Component Analysis (ICA)

(Bell & Sejnowski 1995 etc.)

- If **mixing** is like **matrix multiplication**, then **separation** is searching for the **inverse matrix**



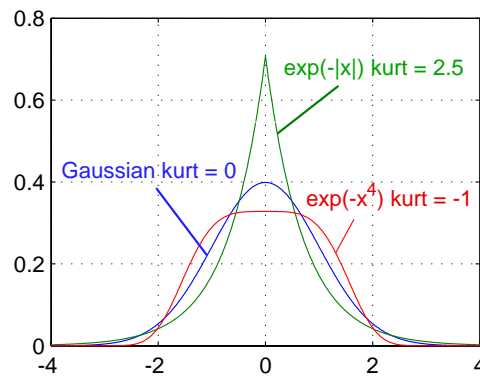
- i.e.  $W \approx A^{-1}$
- with  $N$  different versions of the mixed signals (microphones), we can find  $N$  different input contributions (sources)
- how to rate quality of outputs?  
i.e. when do outputs look **separate**?



# Gaussianity, Kurtosis & Independence

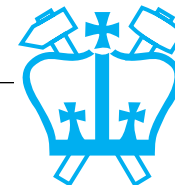
- **A signal can be characterized by its PDF  $p(x)$** 
  - i.e. as if successive time values are drawn from a **random variable** (RV)
  - Gaussian PDF is **'least interesting'**
  - Sums of **independent** RVs (PDFs convolved) tend to Gaussian PDF (Weak law of large numbs)
- **Measures of deviations from Gaussianity:**  
**4th moment is Kurtosis ("bulging")**

$$kurt(y) = E\left[\left(\frac{y - \mu}{\sigma}\right)^4\right] - 3$$



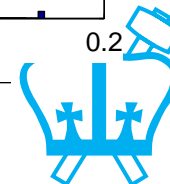
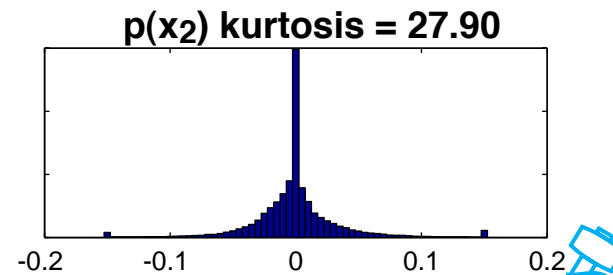
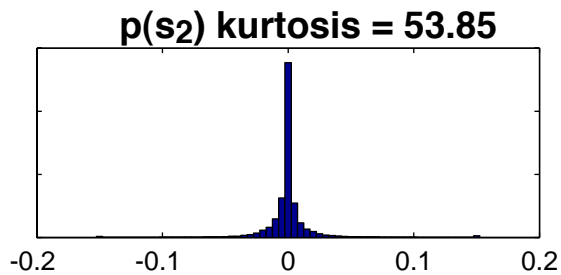
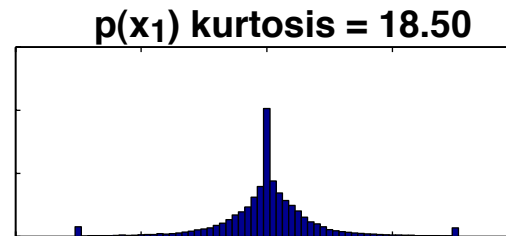
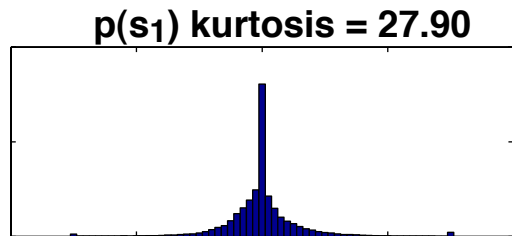
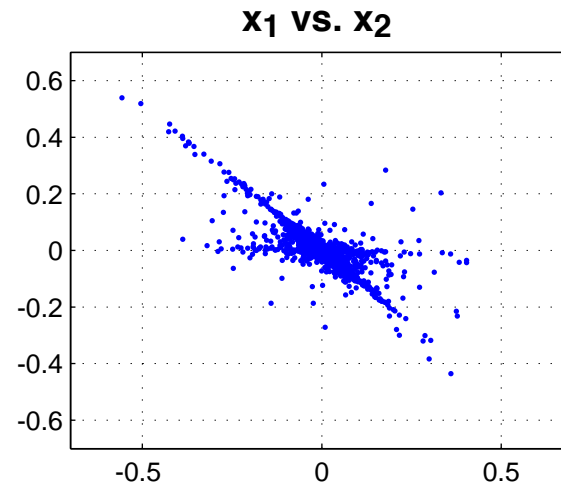
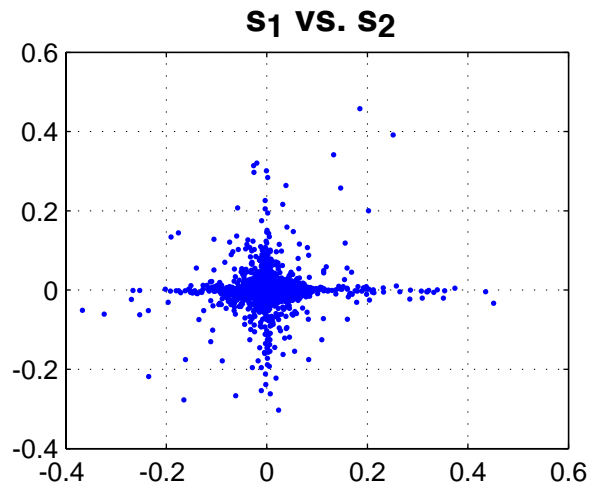
- kurtosis of Gaussian is zero (this def.)
- 'heavy tails'  $\rightarrow kurt > 0$
- closer to uniform dist.  $\rightarrow kurt < 0$

• **Directly related to KL divergence from Gaussian PDF**



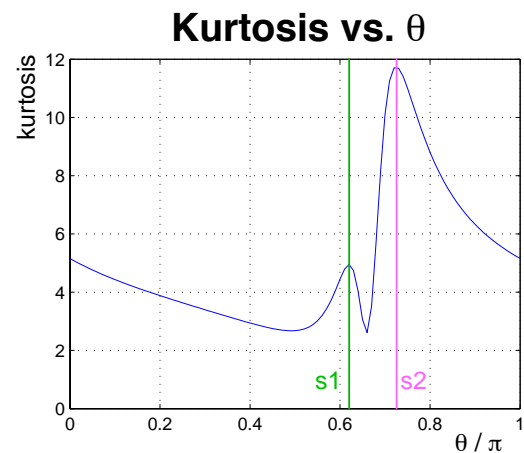
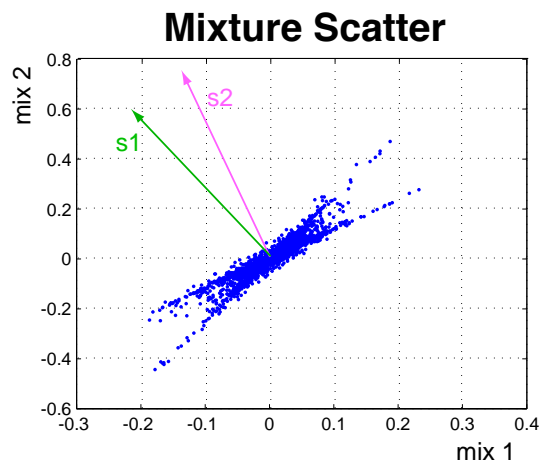
# Independence in Mixtures

- Scatter plots & Kurtosis values



# Finding Independent Components

- Sums of independent RVs are **more Gaussian**  
→ **minimize** Gaussianity to undo sums  
- i.e. search over  $w_{ij}$  terms in inverse matrix



- **Solve by Gradient descent or Newton-Raphson:**

$$; \mathbf{w}^+ = E\{\mathbf{x}g(\mathbf{w}^T \mathbf{x})\} - E\{g'(\mathbf{w}^T \mathbf{x})\}\mathbf{w}$$

$$; \mathbf{w} = \mathbf{w}^+ / \|\mathbf{w}^+\|$$

“Fast ICA”, <http://www.cis.hut.fi/projects/ica/fastica/>



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## Limitations of ICA

- **Assumes instantaneous mixing**
  - real world mixtures have delays & reflections
  - STFT domain?
$$x_1(t) = a_{11}(t) \otimes s_1(t) + a_{12}(t) \otimes s_2(t)$$
$$\Rightarrow X_1(\omega) = A_{11}(\omega)S_1(\omega) + A_{12}(\omega)S_2(\omega)$$
Solve  $\omega$  subbands separately, match up answers
- **Searching for best possible inverse matrix**
  - cannot find more than  $N$  outputs from  $N$  inputs but: “projection pursuit” ideas  
+ time-frequency masking...
- **Cancellation inherently fragile**
  - $\hat{s}_1 = w_{11} \cdot x_1 + w_{12} \cdot x_2$  to cancel out  $s_2$
  - sensitive to noise in  $x$  channels
  - time-varying mixtures are a problem



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# Outline

- 1 Sound Mixture Organization
- 2 Computational Auditory Scene Analysis
- 3 Independent Component Analysis
- 4 **Model-Based Separation**
  - Fitting models to mixtures
  - Missing-data recognition
  - Speech Fragment Decoding

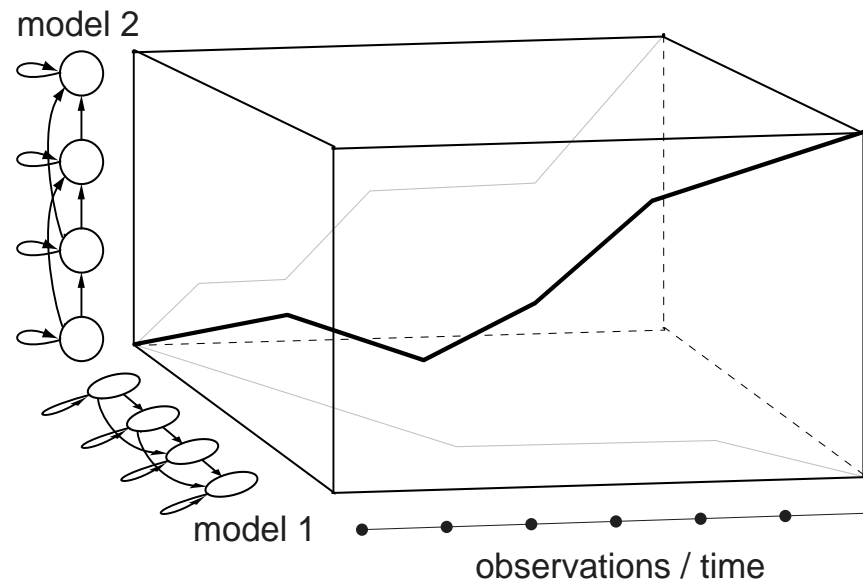


# 4

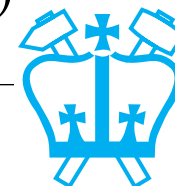
## Model-Based Separation: HMM decomposition

(e.g. Varga & Moore 1991, Gales & Young 1996)

- **Independent state** sequences for 2+ component source models

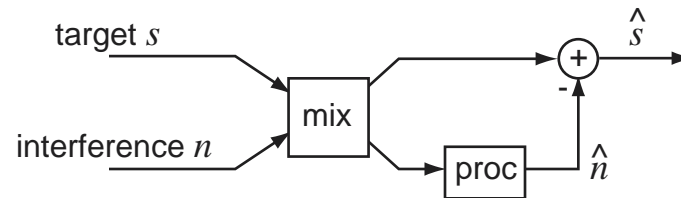


- **New combined state space**  $q' = \{q_1 q_2\}$ 
  - need pdfs for combinations  $p(X|q_1, q_2)$

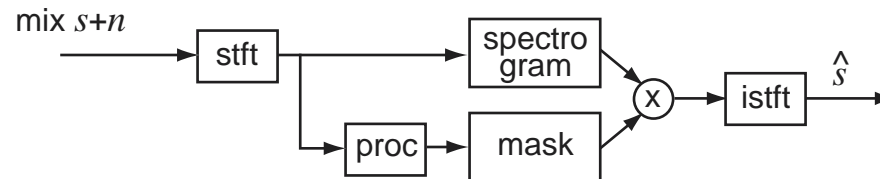


# One-channel Separation: Masked Filtering

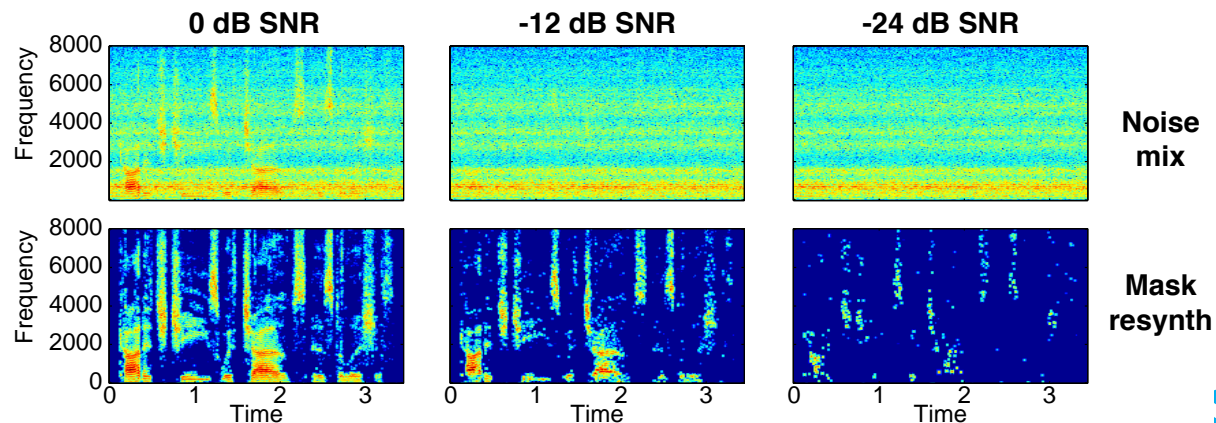
- Multichannel  $\rightarrow$  ICA: Inverse filter & **cancel**



- One channel: find a time-frequency **mask**



- Cannot remove **overlapping noise** in TF cells, but surprisingly effective (psy. masking?):

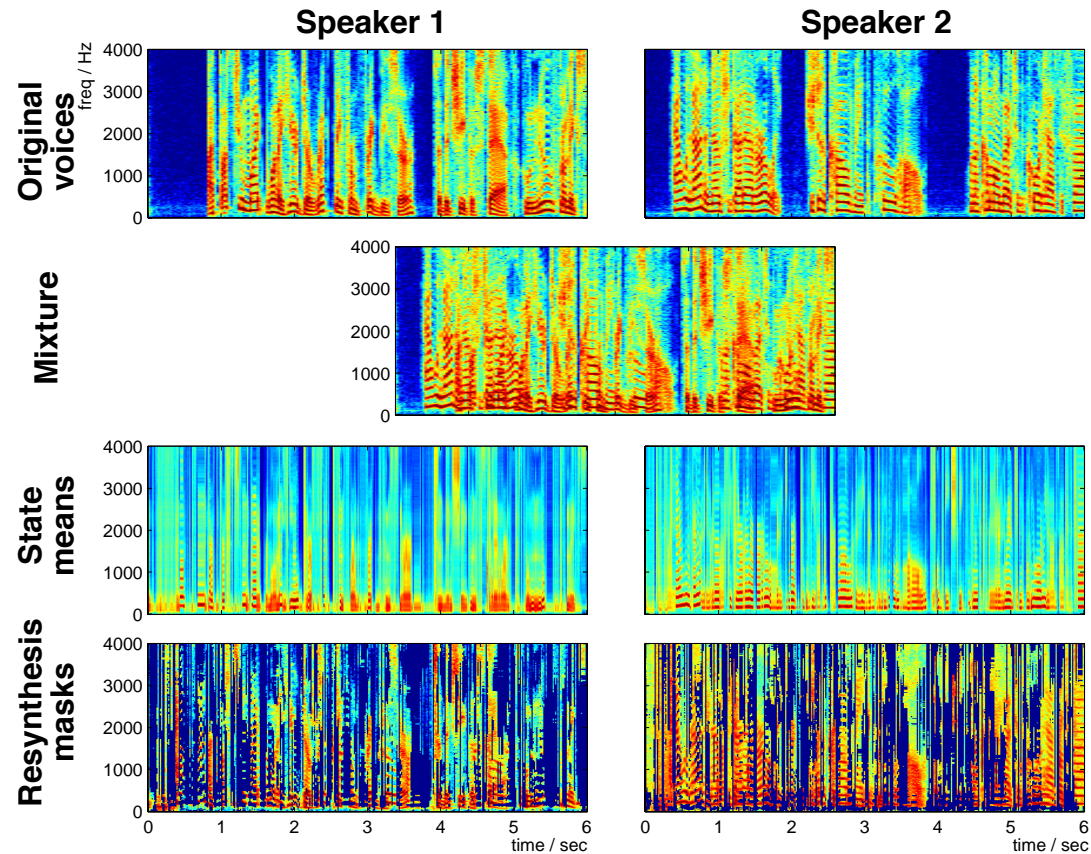




# “One microphone source separation”

(Roweis 2000, Manuel Reyes)

- **State sequences** → **t-f estimates** → **mask**



- 1000 states/model ( $\rightarrow 10^6$  transition probs.)
- simplify by **subbands** (coupled HMM)?



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# Speech Fragment Recognition

(Jon Barker & Martin Cooke, Sheffield)

- **Signal separation is too hard!**  
**Instead:**
  - segregate features into **partially-observed** sources
  - then classify
- **Made possible by missing data recognition**
  - integrate over uncertainty in observations for true posterior distribution
- **Goal:**  
**Relate clean speech models  $P(X|M)$  to speech-plus-noise mixture observations**
  - .. and make it tractable

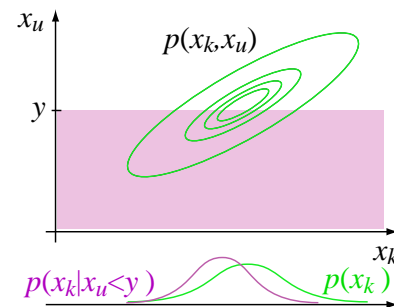


# Missing Data Recognition

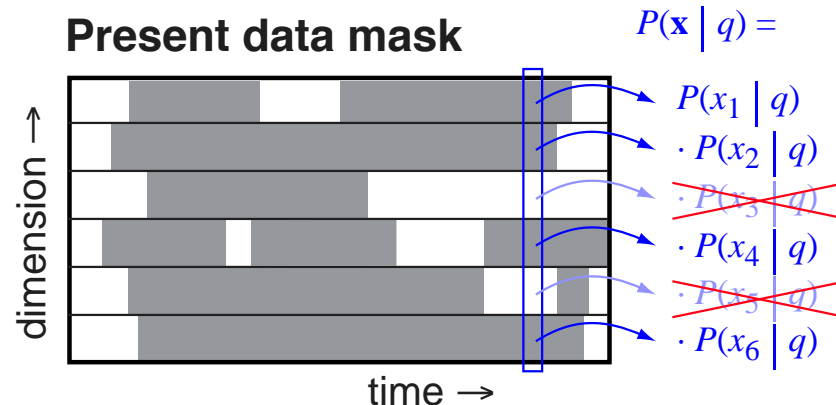
- **Speech models  $p(\mathbf{x}|m)$  are multidimensional...**
  - i.e. means, variances for every freq. channel
  - need values for all dimensions to get  $p(\bullet)$

- **But: can evaluate over a subset of dimensions  $x_k$**

$$p(\mathbf{x}_k | m) = \int p(\mathbf{x}_k, \mathbf{x}_u | m) d\mathbf{x}_u$$



- **Hence, missing data recognition:**

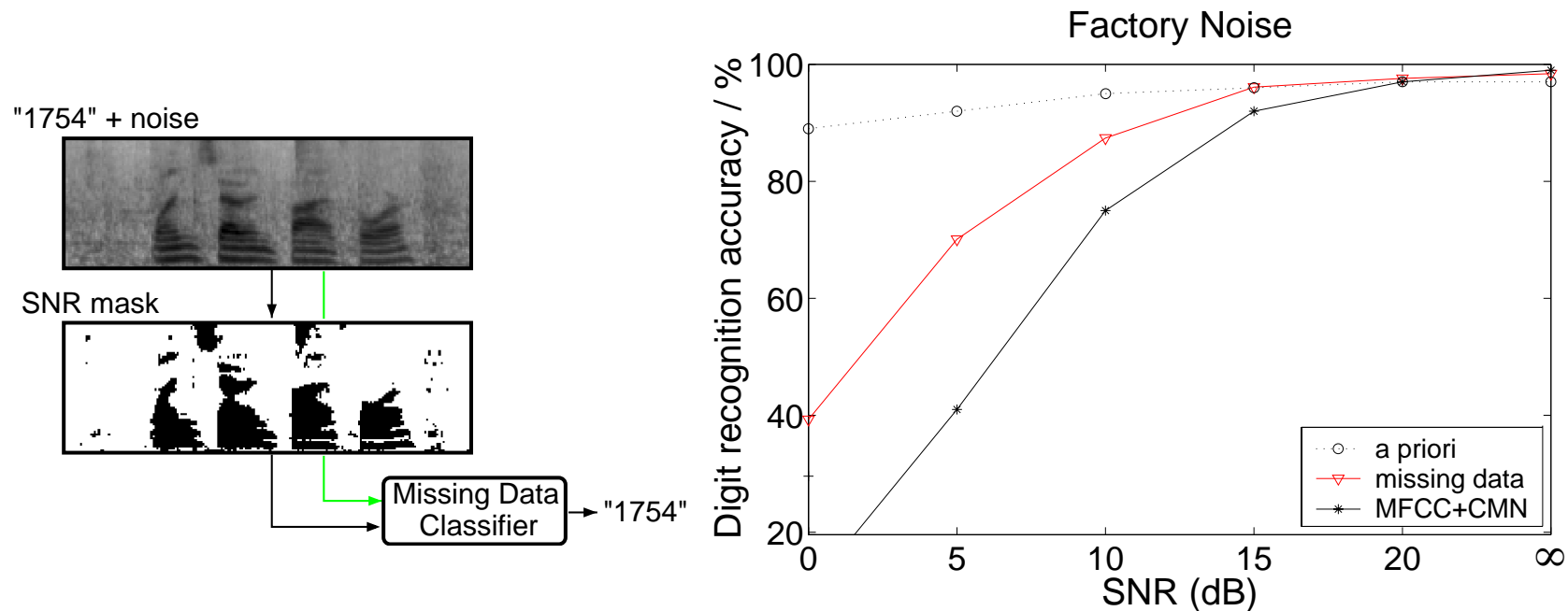


- hard part is finding the mask (segregation)



## Missing Data Results

- Estimate static background noise level  $N(f)$
- Cells with energy close to background are considered “missing”



- must use spectral features!
- **But: nonstationary noise → spurious mask bits**
  - can we try **removing** parts of mask?



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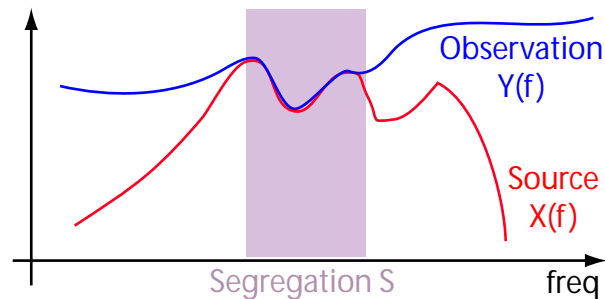
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## Comparing different segregations

- **Standard classification chooses between models  $M$  to match source features  $X$**

$$M^* = \operatorname{argmax}_M P(M|X) = \operatorname{argmax}_M P(X|M) \cdot \frac{P(M)}{\cancel{P(X)}}$$

- **Mixtures: observed features  $Y$ , segregation  $S$ , all related by  $P(X|Y, S)$**



- **Joint classification of model and segregation:**

$$P(M, S|Y) = P(M) \int P(X|M) \cdot \frac{P(X|Y, S)}{P(X)} dX \cdot P(S|Y)$$

- $P(X)$  no longer constant



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## Calculating fragment matches

$$P(M, S|Y) = P(M) \int P(X|M) \cdot \frac{P(X|Y, S)}{P(X)} dX \cdot P(S|Y)$$

- $P(X|M)$  - the clean-signal feature model
- $P(X|Y,S)/P(X)$  - is  $X$  'visible' given segregation?
- Integration collapses some bands...
- $P(S|Y)$  - segregation inferred from observation
  - just assume uniform, find  $S$  for most likely  $M$
  - or: use extra information in  $Y$  to distinguish  $S$ 's...
- **Result:**
  - probabilistically-correct relation between clean-source models  $P(X|M)$  and inferred, recognized **source** + segregation  $P(M,S|Y)$

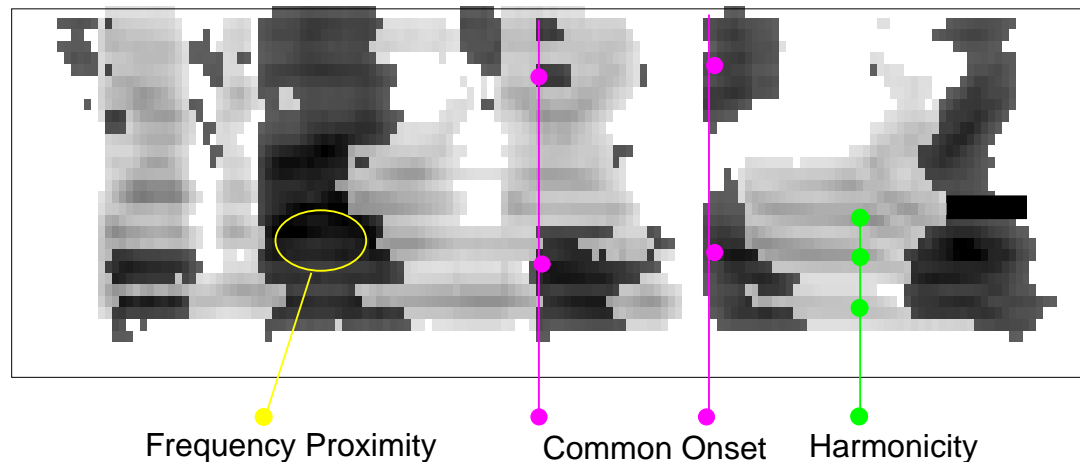


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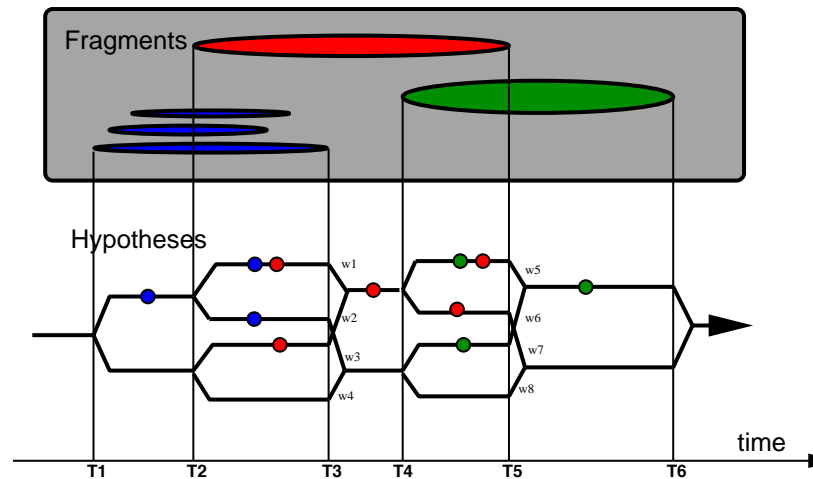
## Using CASA features

- $P(S|Y)$  links acoustic information to segregation
  - is this segregation worth considering?
  - how likely is it?
- **Opportunity for CASA-style information to contribute**
  - **periodicity/harmonicity:**  
these different frequency bands belong together
  - **onset/continuity:**  
this time-frequency region must be whole



# Fragment decoding

- Limiting  $S$  to whole fragments makes hypothesis search tractable:



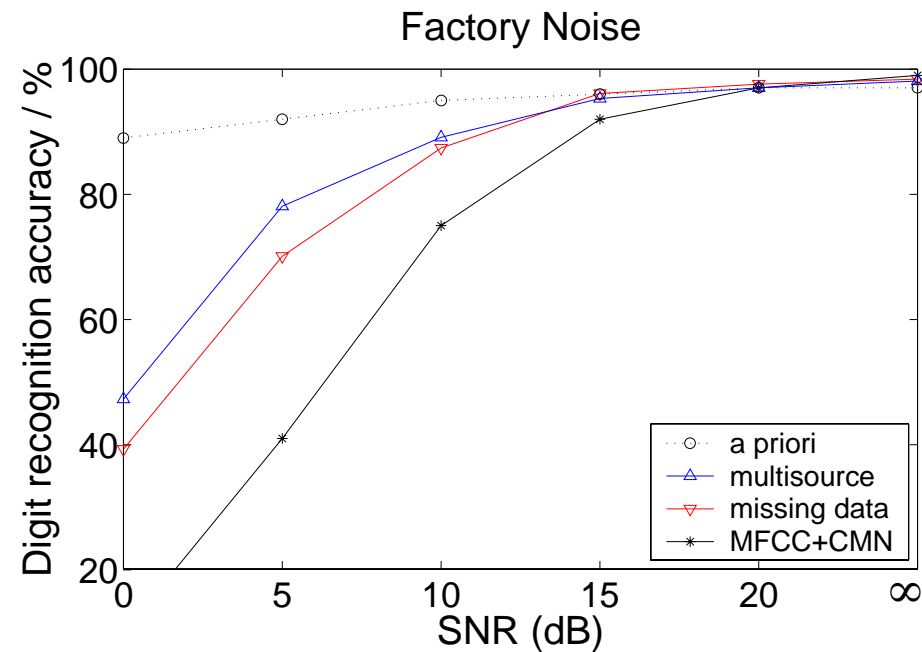
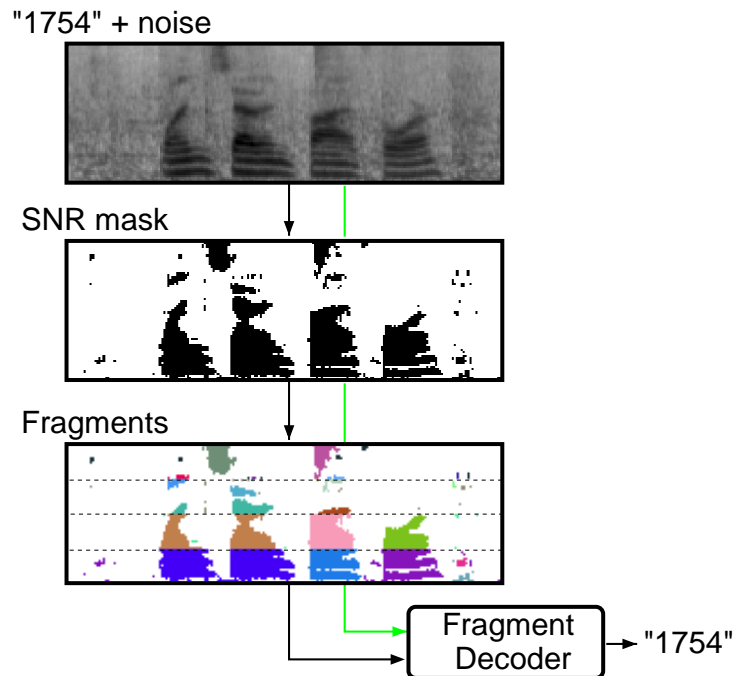
- choice of fragments reflects  $P(S|Y) \cdot P(X|M)$   
i.e. best combination of segregation  
and match to speech models
- Merging hypotheses limits space demands
  - .. but erases specific history





# Speech fragment decoder results

- Simple  $P(S|Y)$  model forces contiguous regions to stay together
  - big efficiency gain when searching  $S$  space



- **Clean-models-based recognition** rivals **trained-in-noise recognition**

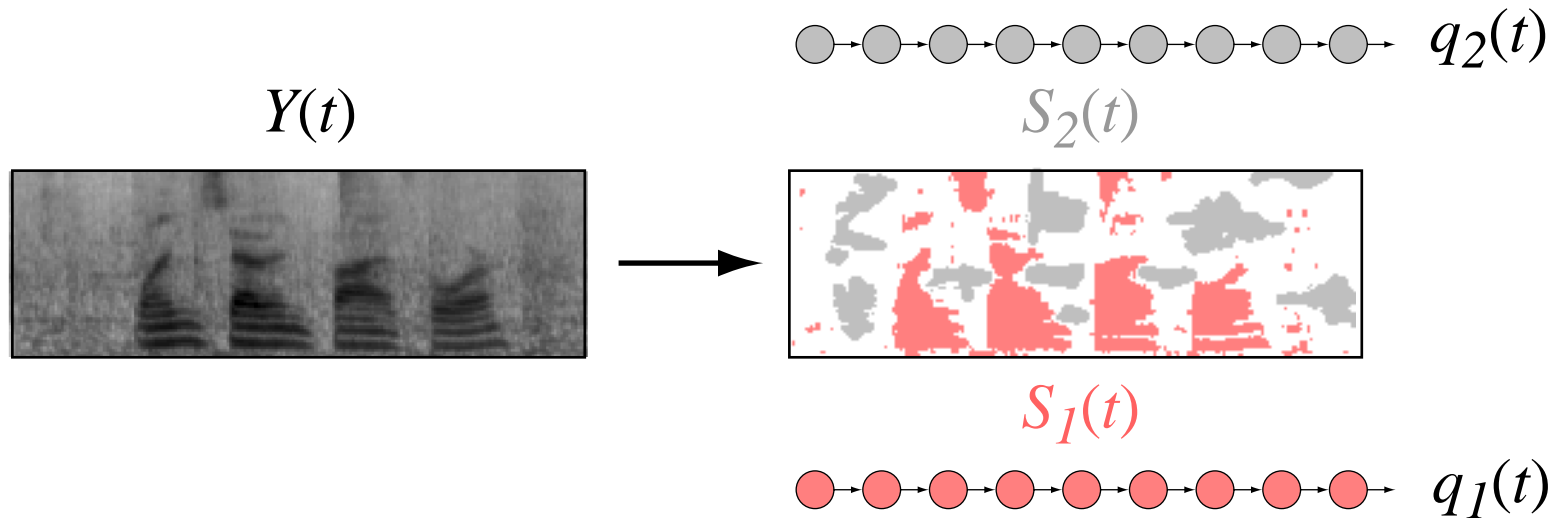


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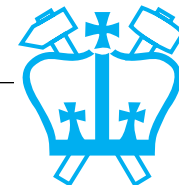
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## Multi-source decoding

- Search for **more than one source**



- **Mutually-dependent data masks**
  - disjoint subsets of cells for each source
  - each model match  $P(M_x|S_x, Y)$  is independent
  - masks are mutually dependent:  $P(S_1, S_2|Y)$
- **Huge practical advantage over full search**



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## Summary

- **Auditory Scene Analysis:**  
Hearing: partially understood, very successful
- **Independent Component Analysis:**  
Simple and powerful, some practical limits
- **Model-based separation:**  
Real-world constraints, implementation tricks

**Mixture separation the main obstacle in many applications e.g. soundtrack recognition**



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