

Lecture 11: Signal Separation

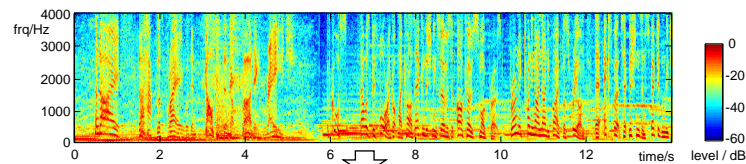
- 1 Sound Mixture Organization
- 2 Computational Auditory Scene Analysis
- 3 Independent Component Analysis
- 4 Model-Based Separation

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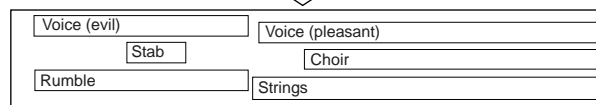
Columbia University Dept. of Electrical Engineering
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1 Sound Mixture Organization



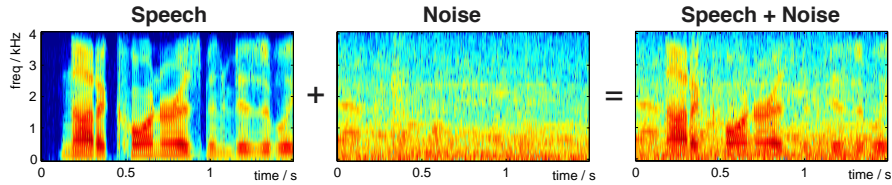
Analysis



- **Auditory Scene Analysis**: describing a complex sound in terms of high-level sources / events
 - ... like listeners do
- **Hearing is ecologically grounded**
 - reflects 'natural scene' properties
 - subjective, not absolute



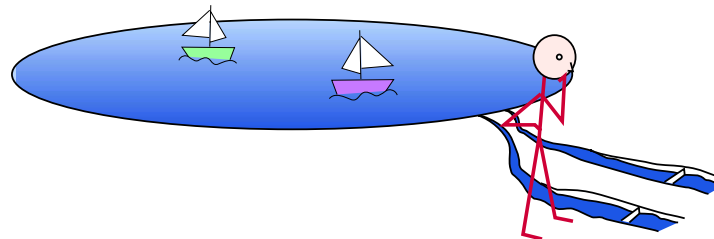
Sound, mixtures, and learning



- **Sound**
 - carries useful information about the world
 - complements vision
- **Mixtures**
 - .. are the rule, not the exception
 - medium is 'transparent', sources are many
 - must be handled!
- **Learning**
 - the 'speech recognition' lesson:
let the data do the work
 - like listeners



The problem with recognizing mixtures



“Imagine two narrow channels dug up from the edge of a lake, with handkerchiefs stretched across each one. Looking only at the motion of the handkerchiefs, you are to answer questions such as: How many boats are there on the lake and where are they?” (after Bregman'90)

- **Received waveform is a mixture**
 - two sensors, N signals ... **underconstrained**
- **Disentangling mixtures as the primary goal?**
 - perfect solution is not possible
 - need experience-based **constraints**

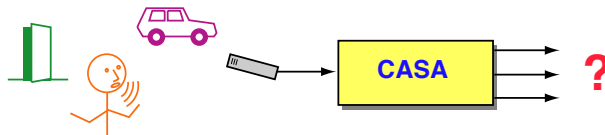


Approaches to sound mixture recognition

- **Separate signals, then recognize**
 - e.g. Computational Auditory Scene Analysis (CASA), Independent Component Analysis (ICA)
 - nice, if you can do it
- **Recognize combined signal**
 - 'multicondition training'
 - combinatorics..
- **Recognize with parallel models**
 - full joint-state space?
 - divide signal into fragments, then use missing-data recognition



What is the goal of CASA?



- **Separate signals?**
 - output is unmixed waveforms
 - underconstrained, very hard ...
 - too hard? not required?
- **Source classification?**
 - output is set of event-names
 - listeners do more than this...
- **Something in-between?**
Identify independent sources + characteristics
 - standard task, results?



Segregation vs. Inference

- **Source separation requires attribute separation**
 - sources are characterized by attributes (pitch, loudness, timbre + finer details)
 - need to identify & gather different attributes for different sources ...
- **Need representation that segregates attributes**
 - spectral decomposition
 - periodicity decomposition
- **Sometimes values can't be separated**
 - e.g. unvoiced speech
 - maybe **infer** factors from probabilistic model?
$$p(O, x, y) \rightarrow p(x, y|O)$$
 - or: just skip those values, **infer** from higher-level context



Outline

- 1 **Sound Mixture Organization**
- 2 **Computational Auditory Scene Analysis**
 - Human Auditory Scene Analysis
 - Bottom-up and Top-down models
 - Evaluation
- 3 **Independent Component Analysis**
- 4 **Model-Based Separation**

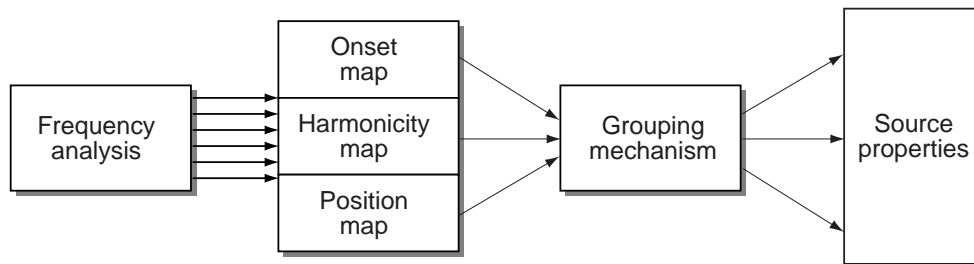


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Auditory Scene Analysis

(Bregman 1990)

- **How do people analyze sound mixtures?**
 - break mixture into small **elements** (in time-freq)
 - elements are **grouped** in to sources using **cues**
 - sources have aggregate **attributes**
- **Grouping 'rules' (Darwin, Carlyon, ...):**
 - cues: common onset/offset/modulation, harmonicity, spatial location, ...

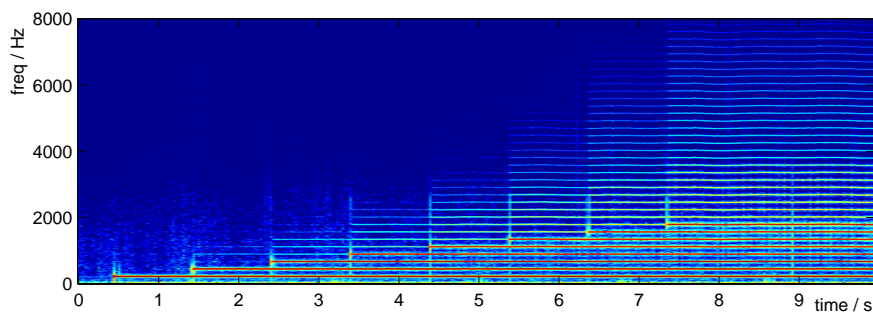


(after Darwin, 1996)



Cues to simultaneous grouping

- **Elements + attributes**

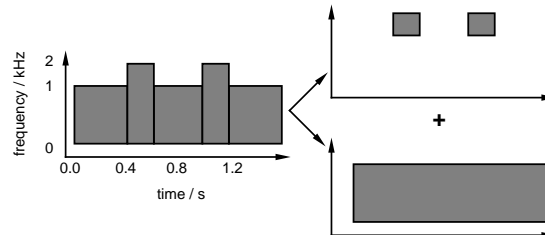


- **Common onset**
 - simultaneous energy has common source
- **Periodicity**
 - energy in different bands with same cycle
- **Other cues**
 - spatial (ITD/IID), familiarity, ...



The effect of context

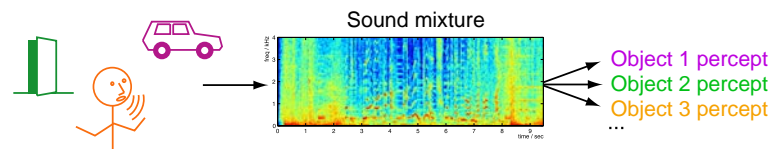
- **Context can create an ‘expectation’:**
i.e. a bias towards a particular interpretation
- **e.g. Bregman’s “old-plus-new” principle:**
A change in a signal will be interpreted as an *added* source whenever possible



- a different division of the same energy depending on what preceded it



Computational Auditory Scene Analysis (CASA)

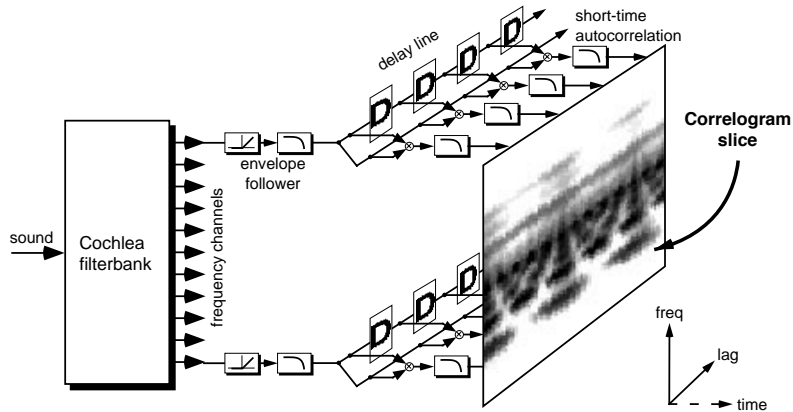


- **Goal: Automatic sound organization;**
Systems to ‘pick out’ sounds in a mixture
 - ... like people do
- **E.g. voice against a noisy background**
 - to improve speech recognition
- **Approach:**
 - psychoacoustics describes grouping ‘rules’
 - ... just implement them?



CASA front-end processing

- **Correlogram:**
Loosely based on known/possible physiology



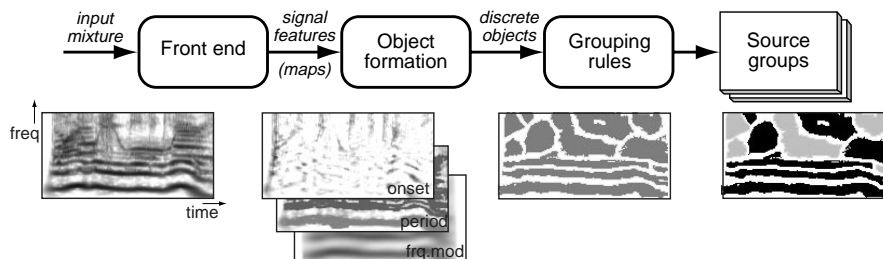
- linear filterbank cochlear approximation
- static nonlinearity
- zero-delay slice is like spectrogram
- periodicity from delay-and-multiply detectors



The Representational Approach

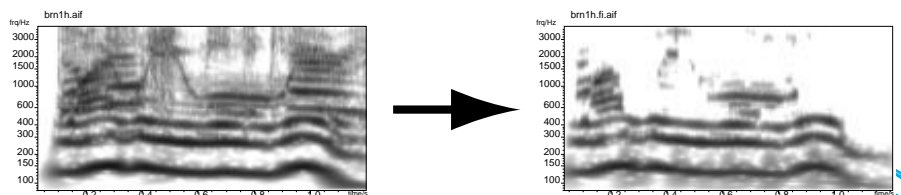
(Brown & Cooke 1993)

- **Implement psychoacoustic theory**

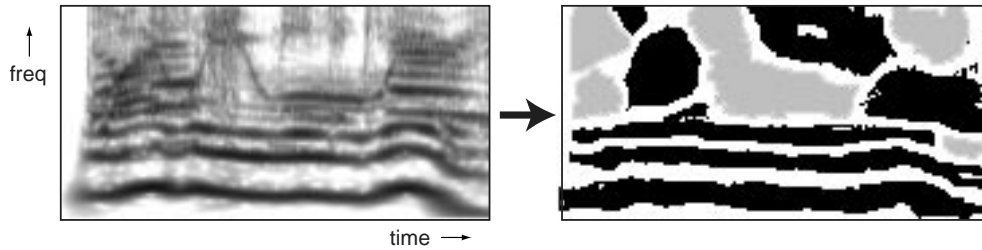


- 'bottom-up' processing
- uses common onset & periodicity cues

- **Able to extract voiced speech:**



Problems with 'bottom-up' CASA

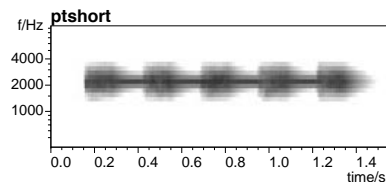


- **Circumscribing time-frequency elements**
 - need to have 'regions', but hard to find
- **Periodicity is the primary cue**
 - how to handle aperiodic energy?
- **Resynthesis via masked filtering**
 - cannot separate within a single t-f element
- **Bottom-up leaves no ambiguity or context**
 - how to model illusions?

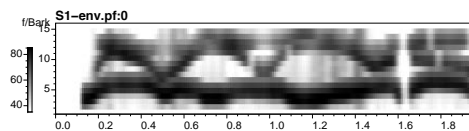


Restoration in sound perception

- **Auditory 'illusions'** = hearing what's not there
- **The continuity illusion**



- **Sinewave Speech (SWS)**



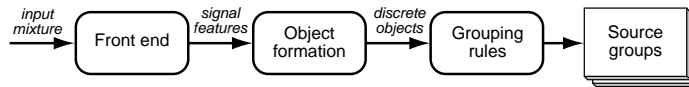
- **duplex** perception
- **What kind of model accounts for this?**
 - is it an **important part** of hearing?



Adding top-down constraints: Prediction-Driven CASA (PDCASA)

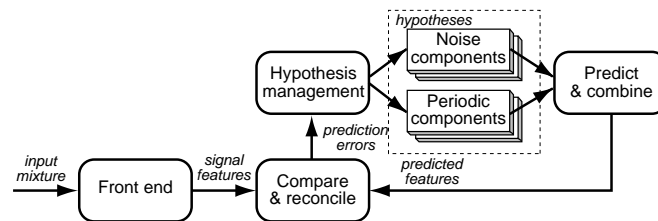
Perception is **not direct**
but a **search** for plausible hypotheses

- **Data-driven (bottom-up)...**



- objects irresistibly appear

vs. Prediction-driven (top-down)

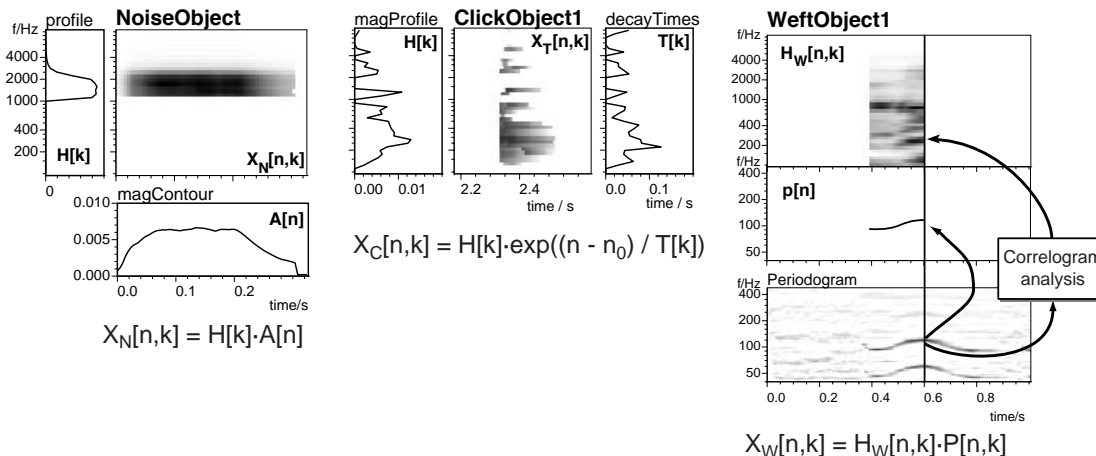


- match observations with a 'world-model'
- need world-model constraints...



Generic sound elements for PDCASA

- **Goal is a representational space that**
 - covers real-world perceptual sounds
 - minimal parameterization (sparseness)
 - separate attributes in separate parameters

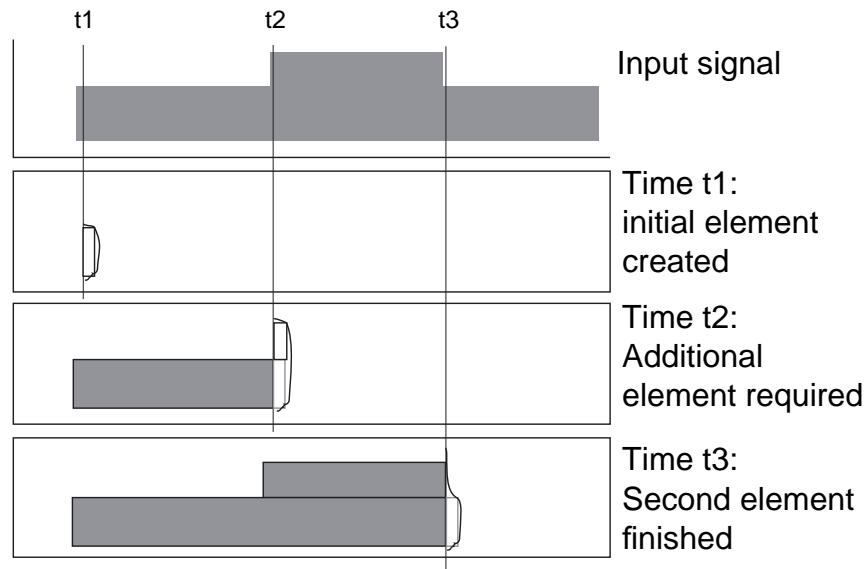


- **Object hierarchies built on top...**



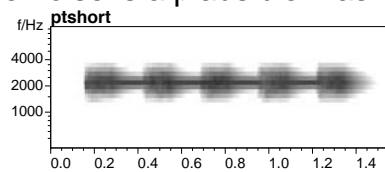
PDCASA for old-plus-new

- Incremental analysis

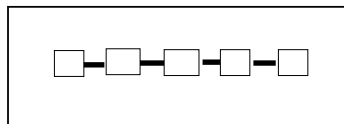


PDCASA for the continuity illusion

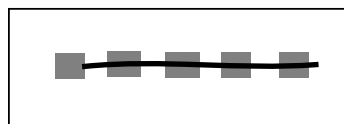
- Subjects hear the tone as continuous
... if the noise is a plausible masker



- Data-driven analysis gives just visible portions:

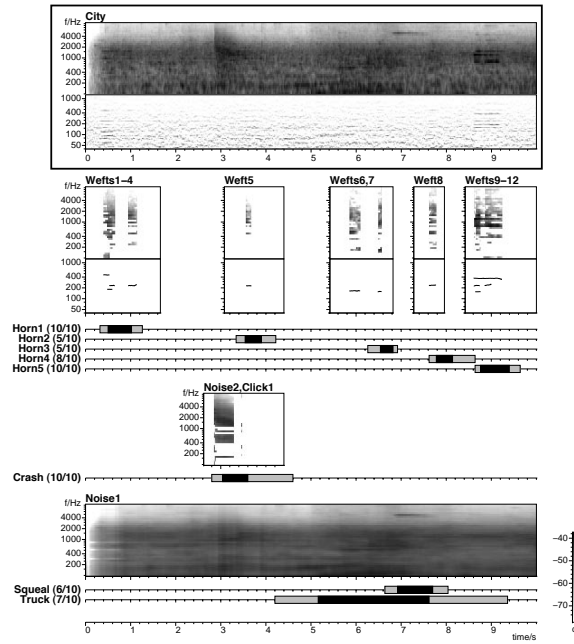


- Prediction-driven can infer masking:



Prediction-Driven CASA

- **Explain** a complex sound with basic elements



Aside: Ground Truth

- **What do people hear in sound mixtures?**
 - do interpretations match?
- **Listening tests to collect 'perceived events':**

Subject dpwe / Example city / Part A

Names	Marks
horn1	
crash	
squeal	
horn2	

Play Stop Go on...



Aside: Evaluation

- **Evaluation is a big problem for CASA**
 - what is the goal, really?
 - what is a good test domain?
 - how do you measure performance?
- **SNR improvement**
 - tricky to derive from before/after signals: correspondence problem
 - can do with fixed filtering mask; but rewards removing signal as well as noise
- **Speech Recognition (ASR) improvement**
 - recognizers typically very sensitive to artefacts
- **'Real' task?**
 - mixture corpus with specific sound events...



Outline

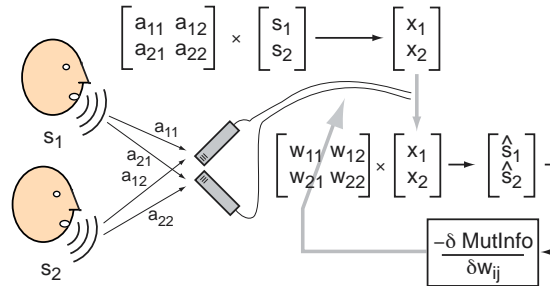
- 1 Sound Mixture Organization
- 2 Computational Auditory Scene Analysis
- 3 **Independent Component Analysis**
 - Blind source separation
 - Independence and kurtosis
 - Limits of the approach
- 4 Model-Based Separation



3 Independent Component Analysis (ICA)

(Bell & Sejnowski 1995 etc.)

- If **mixing** is like **matrix multiplication**, then **separation** is searching for the **inverse matrix**



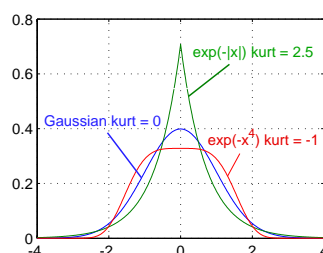
- i.e. $W \approx A^{-1}$
- with N different versions of the mixed signals (microphones), we can find N different input contributions (sources)
- how to rate quality of outputs?
i.e. when do outputs look **separate**?



Gaussianity, Kurtosis & Independence

- **A signal can be characterized by its PDF $p(x)$**
 - i.e. as if successive time values are drawn from a **random variable** (RV)
 - Gaussian PDF is '**least interesting**'
 - Sums of **independent** RVs (PDFs convolved) tend to Gaussian PDF (Weak law of large nums)
- **Measures of deviations from Gaussianity:**
4th moment is **Kurtosis** ("bulging")

$$kurt(y) = E\left[\left(\frac{y - \mu}{\sigma}\right)^4\right] - 3$$



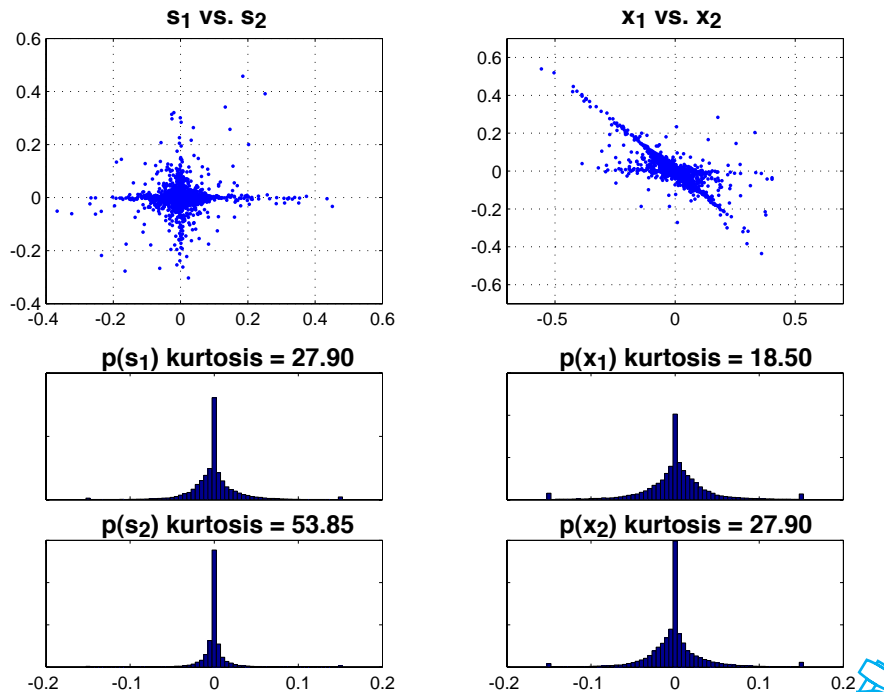
- kurtosis of Gaussian is zero (this def.)
- 'heavy tails' $\rightarrow kurt > 0$
- closer to uniform dist. $\rightarrow kurt < 0$

• **Directly related to KL divergence from Gaussian PDF**



Independence in Mixtures

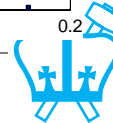
- Scatter plots & Kurtosis values



E6820 SAPR - Dan Ellis

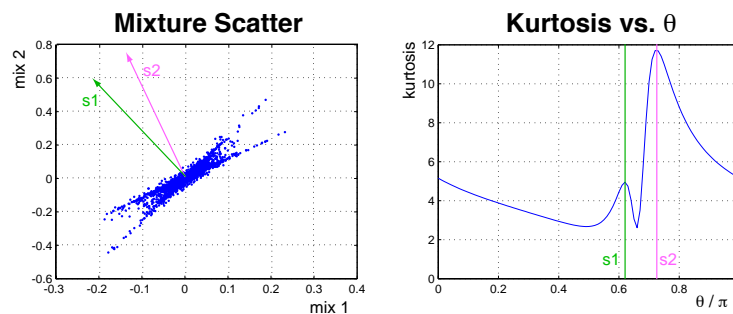
L11 - Signal Separation

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Finding Independent Components

- Sums of independent RVs are **more Gaussian**
 → **minimize** Gaussianity to undo sums
 - i.e. search over w_{ij} terms in inverse matrix



- Solve by Gradient descent or Newton-Raphson:

$$; \mathbf{w}^+ = E\{\mathbf{x}g(\mathbf{w}^T \mathbf{x})\} - E\{g'(\mathbf{w}^T \mathbf{x})\}\mathbf{w}$$

$$; \mathbf{w} = \mathbf{w}^+ / \|\mathbf{w}^+\|$$

"Fast ICA", <http://www.cis.hut.fi/projects/ica/fastica/>

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Limitations of ICA

- **Assumes instantaneous mixing**
 - real world mixtures have delays & reflections
 - STFT domain?
$$x_1(t) = a_{11}(t) \otimes s_1(t) + a_{12}(t) \otimes s_2(t)$$
$$\Rightarrow X_1(\omega) = A_{11}(\omega)S_1(\omega) + A_{12}(\omega)S_2(\omega)$$
Solve ω subbands separately, match up answers
- **Searching for best possible inverse matrix**
 - cannot find more than N outputs from N inputs
but: “projection pursuit” ideas
+ time-frequency masking...
- **Cancellation inherently fragile**
 - $\hat{s}_1 = w_{11} \cdot x_1 + w_{12} \cdot x_2$ to cancel out s_2
 - sensitive to noise in x channels
 - time-varying mixtures are a problem



Outline

- 1 Sound Mixture Organization
- 2 Computational Auditory Scene Analysis
- 3 Independent Component Analysis
- 4 **Model-Based Separation**
 - Fitting models to mixtures
 - Missing-data recognition
 - Speech Fragment Decoding

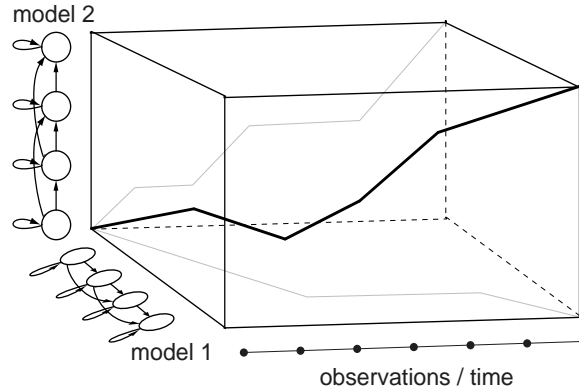


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Model-Based Separation: HMM decomposition

(e.g. Varga & Moore 1991, Gales & Young 1996)

- **Independent state sequences for 2+ component source models**

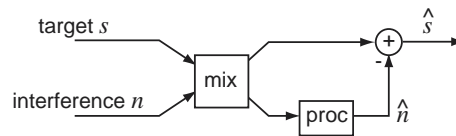


- **New combined state space** $q' = \{q_1 q_2\}$
- need pdfs for combinations $p(X|q_1, q_2)$

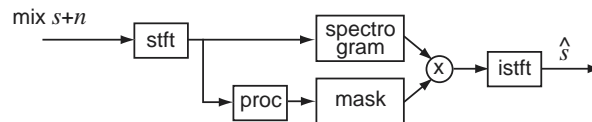


One-channel Separation: Masked Filtering

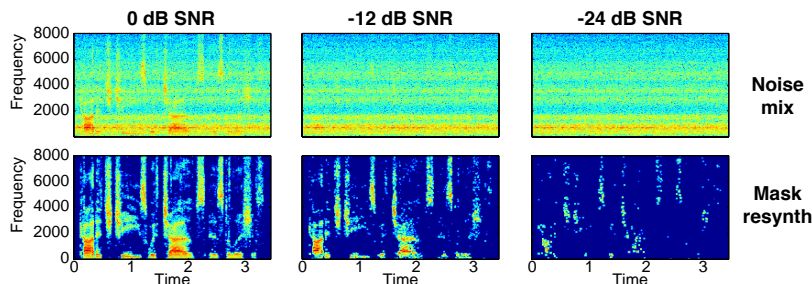
- **Multichannel → ICA: Inverse filter & cancel**



- **One channel: find a time-frequency mask**



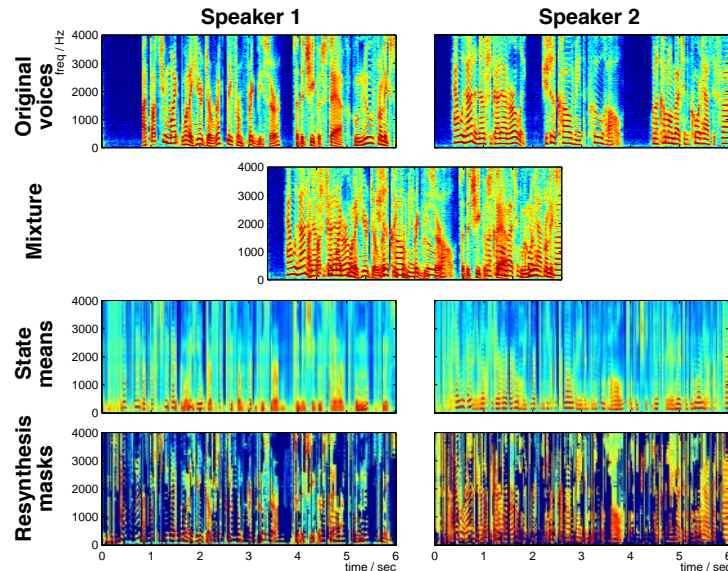
- **Cannot remove overlapping noise in TF cells, but surprisingly effective (psy. masking?):**



“One microphone source separation”

(Roweis 2000, Manuel Reyes)

- **State sequences** → **t-f estimates** → **mask**



- 1000 states/model (→ 10^6 transition probs.)
- simplify by **subbands** (coupled HMM)?



Speech Fragment Recognition

(Jon Barker & Martin Cooke, Sheffield)

- **Signal separation is too hard!**
Instead:
 - segregate features into **partially-observed** sources
 - then classify
- **Made possible by missing data recognition**
 - integrate over uncertainty in observations for true posterior distribution
- **Goal:**
Relate clean speech models $P(X|M)$ to speech-plus-noise mixture observations
 - .. and make it tractable

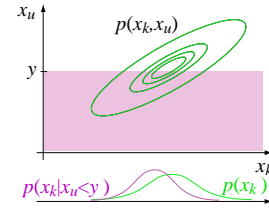


Missing Data Recognition

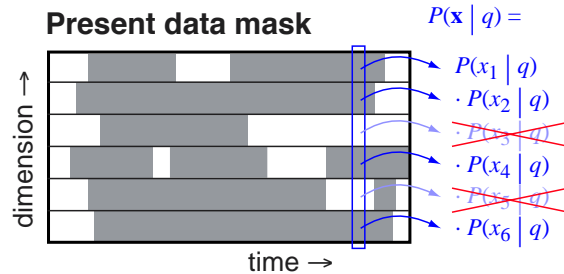
- **Speech models $p(\mathbf{x}|m)$ are multidimensional...**
 - i.e. means, variances for every freq. channel
 - need values for all dimensions to get $p(\bullet)$

- **But: can evaluate over a subset of dimensions x_k**

$$p(\mathbf{x}_k|m) = \int p(\mathbf{x}_k, \mathbf{x}_u|m) d\mathbf{x}_u$$



- **Hence, missing data recognition:**

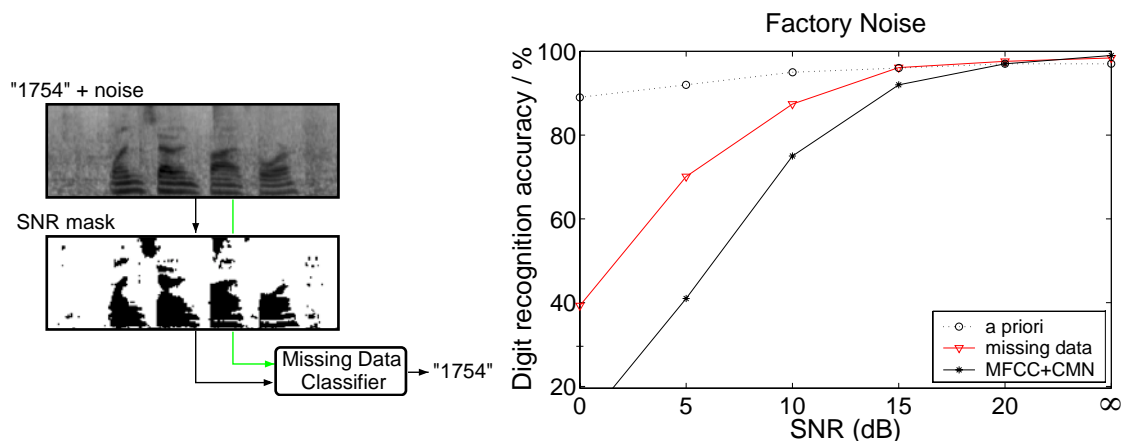


- hard part is finding the mask (segregation)



Missing Data Results

- **Estimate static background noise level $N(f)$**
- **Cells with energy close to background are considered “missing”**



- must use spectral features!

- **But: nonstationary noise → spurious mask bits**
 - can we try removing parts of mask?

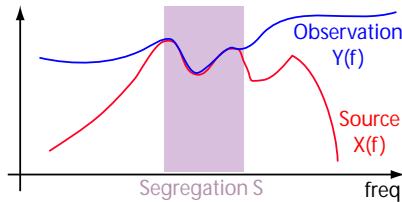


Comparing different segregations

- **Standard classification chooses between models M to match source features X**

$$M^* = \operatorname{argmax}_M P(M|X) = \operatorname{argmax}_M P(X|M) \cdot \frac{P(M)}{P(X)}$$

- **Mixtures: observed features Y , segregation S , all related by $P(X|Y, S)$**



- **Joint classification of model and segregation:**

$$P(M, S|Y) = P(M) \int P(X|M) \cdot \frac{P(X|Y, S)}{P(X)} dX \cdot P(S|Y)$$

- $P(X)$ no longer constant



Calculating fragment matches

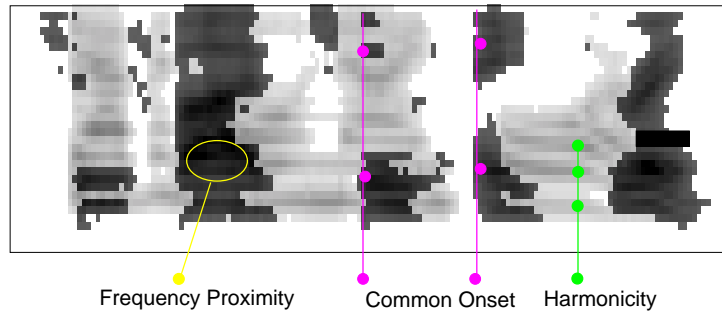
$$P(M, S|Y) = P(M) \int P(X|M) \cdot \frac{P(X|Y, S)}{P(X)} dX \cdot P(S|Y)$$

- $P(X|M)$ - the clean-signal feature model
- $P(X|Y,S)/P(X)$ - is X 'visible' given segregation?
- **Integration collapses some bands...**
- $P(S|Y)$ - segregation inferred from observation
 - just assume uniform, find S for most likely M
 - or: use extra information in Y to distinguish S 's...
- **Result:**
 - probabilistically-correct relation between clean-source models $P(X|M)$ and inferred, recognized source + segregation $P(M,S|Y)$



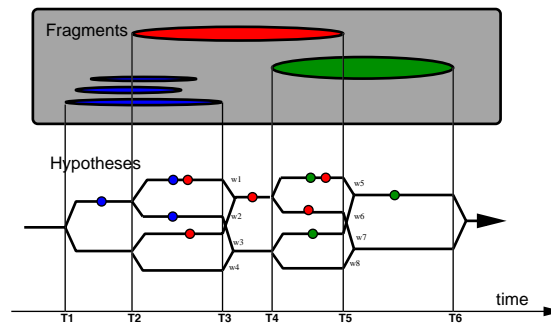
Using CASA features

- $P(S|Y)$ links acoustic information to segregation
 - is this segregation worth considering?
 - how likely is it?
- **Opportunity for CASA-style information to contribute**
 - **periodicity/harmonicity**: these different frequency bands belong together
 - **onset/continuity**: this time-frequency region must be whole



Fragment decoding

- **Limiting S to whole fragments makes hypothesis search tractable:**

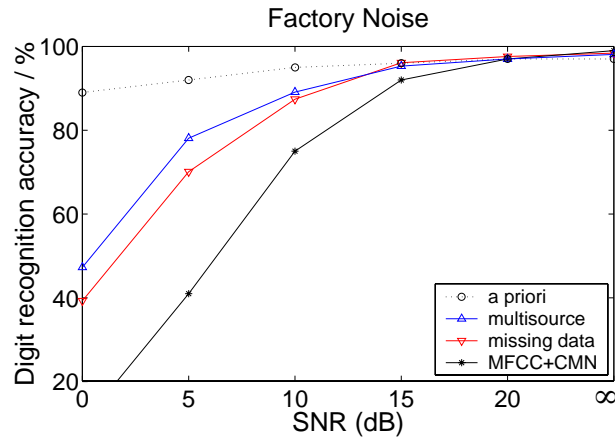
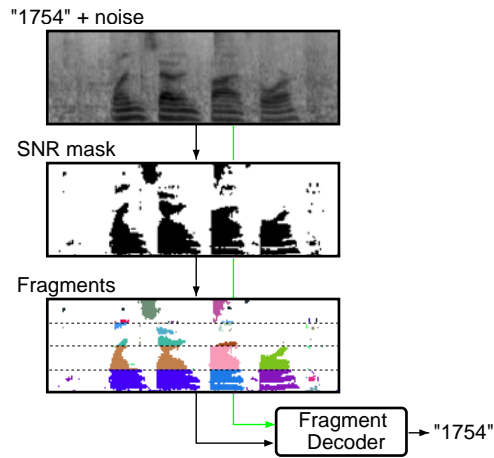


- choice of fragments reflects $P(S|Y) \cdot P(X|M)$
i.e. best combination of segregation and match to speech models
- **Merging hypotheses limits space demands**
 - .. but erases specific history



Speech fragment decoder results

- Simple $P(S|Y)$ model forces contiguous regions to stay together
 - big efficiency gain when searching S space

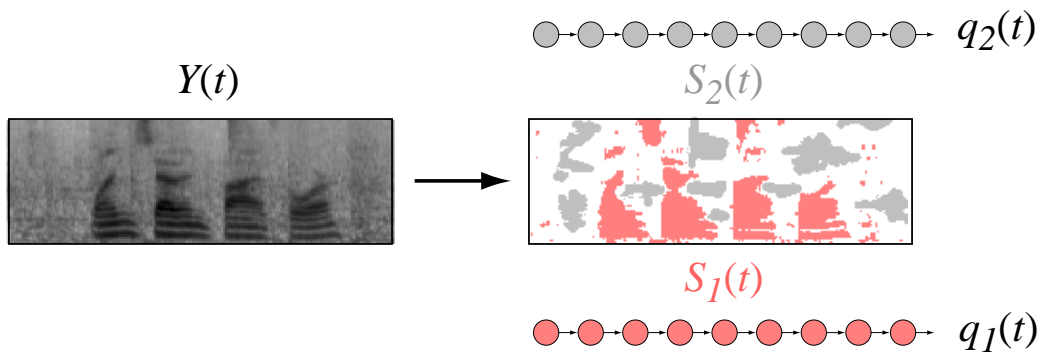


- **Clean-models-based recognition** rivals **trained-in-noise** recognition



Multi-source decoding

- Search for **more than one source**



- **Mutually-dependent data masks**
 - disjoint subsets of cells for each source
 - each model match $P(M_x|S_x, Y)$ is independent
 - masks are mutually dependent: $P(S_1, S_2|Y)$
- **Huge practical advantage over full search**



Summary

- **Auditory Scene Analysis:**
Hearing: partially understood, very successful
- **Independent Component Analysis:**
Simple and powerful, some practical limits
- **Model-based separation:**
Real-world constraints, implementation tricks

Mixture separation the main obstacle in many applications e.g. soundtrack recognition



References

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<http://www.ee.columbia.edu/~dpwe/e6820/papers/HyvO00-icatut.pdf>
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