

# Multipath TCP with Network Coding for Wireless Mesh Networks

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**Abstract**—In wireless multihop networks, techniques such as multipath, local retransmissions and network coding have been successfully used to increase throughput and reduce losses. However, while these techniques improve forwarding performance for UDP, they often introduce side effects such as packet reordering and delay that heavily affect TCP traffic.

In this paper we introduce *CoMP*, a network coding multipath forwarding scheme that improves the reliability and the performance of TCP sessions in wireless mesh networks. *CoMP* exploits the wireless mesh path diversity using network coding, performs congestion control and uses a credit-based method to control the rate at which linear combinations are transmitted. *CoMP* uses a simple algorithm to estimate losses and to send redundant linear combinations in order to maintain the decoding delay at a minimum and to prevent TCP timeouts and retransmissions.

We evaluate *CoMP* through extensive simulations and compare it to state-of-the-art protocols. We show that *CoMP* not only achieves a higher throughput, but also is more efficient than existing protocols, making TCP sessions feasible for wireless mesh networks even under heavy losses.

**Index Terms**—network coding, wireless, TCP, multipath

## I. INTRODUCTION

Wireless mesh networks (WMN) are emerging as the next-generation systems to connect communities. As these networks proliferate, it is expected that users will start demanding more versatile applications such as video streaming and VoIP. Unfortunately, the performance of TCP degrades very fast in WMN [4]. When losses occur in a wireless environment, TCP considers them as being caused by congestion, and triggers its congestion avoidance mechanism which reduces the sending rate to adapt to the new network conditions. Still, the actual capacity of the network has not changed, and hence the network becomes underutilized.

A typical approach to address the problem of improving TCP performance in WMN is to exploit the path diversity in the mesh. One example is *Horizon* [7], which also implements a mechanism to signal congestion to TCP, but it does not offer any reliability and every loss is recovered through retransmissions at TCP layer.

However, multiple paths pose further challenges. Consider the simple scenario from Fig. 1, where the source  $S$  can communicate with destination  $D$  using 3 neighbors,  $A$ ,  $B$  and

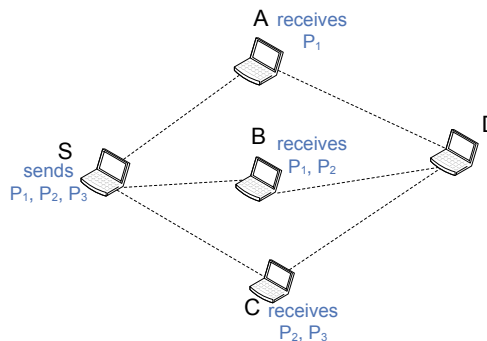


Fig. 1. Multipath example. The source  $S$  can reach the destination  $D$  through three neighbors,  $A$ ,  $B$  and  $C$ .

$C$ . Assume that  $S$  sends three packets,  $P_1, P_2, P_3$ , and the three relays receive the packets as illustrated in the figure. In this situation, the nodes need to *coordinate* and *schedule* the packets transmissions so that the destination receives all of them without duplicates.

Network coding [3] can effectively be employed to solve the relay coordination and the packet scheduling problems. In the above example, each of the relays can use network coding to simply forward a linear combination of the received packets. Once the destination  $D$  receives the three linear combinations, it solves a linear system and recovers the original packets.

Typical network coding techniques divide traffic in *generations* [6] and a coded packet is a linear combination of the packets that belong to the same group, e.g. *MORE* [5]. This approach introduces a coding delay, because the source can send coded packets only after it has all the packets from a group, and a receiver can decode native packets only after it receives a number of independent linear combinations. Furthermore, this delay in the coding operations has a negative impact on the TCP performance in wireless environments.

In order to avoid the coding delay, [8] presents *online coding*, where the source mixes the packets from the TCP congestion window and the receiver acknowledges every innovative linear combination it receives, even if it cannot decode a native packet immediately. This approach gives a new interpretation of the ACKs, and allows for a TCP-sliding window scheme for coding. However, this scheme is single path and the coding operations are performed end-to-end. For the rest of the paper we refer to this approach as *TCP-ARQ*.

With these considerations in mind, we introduce *CoMP*, a network coding multipath protocol for WMN that extends current state-of-the-art and combines network coding with multipath routing to increase throughput for TCP sessions in

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WMN. *CoMP* is situated below TCP/IP in the protocol stack. The main features of our protocol are as follows:

- a multipath online network coding scheme that exploits the path diversity in a mesh network, and eliminates the delay problems introduced by coding (section II-A);
- an algorithm to estimate the loss probability in the network and to adjust online the rate of sending linear combinations (section II-B);
- a hybrid credit-based algorithm, where nodes compute distributedly the rate of generating linear combinations (section II-C);
- a congestion control mechanism based on back-pressure (section II-D).

We extensively evaluate *CoMP* using the *ns-2.33* network simulator [1], and compare it to state-of-the-art protocols: *Horizon* [7], *MORE* [5], and *TCP-ARQ* [8]. The results show that *CoMP* not only achieves a higher throughput, but it is also more efficient, due to exploiting path diversity and re-encoding packets on a hop-by-hop basis.

The paper is organized as follows. In section II we present our protocol with a detailed description of its features. Section III provides the results of our simulations and a comparison to *Horizon*, *MORE*, and *TCP-ARQ*. Section IV concludes with some final remarks.

## II. PROTOCOL DESCRIPTION

In this section we describe the main aspects of *CoMP*.

### A. Multipath online coding

For our multipath coding scheme, we use a similar approach as the one in [8], but with some essential differences. First, *TCP-ARQ* uses only one path to forward the packets from sender to receiver, while *CoMP* takes advantage of the path diversity characteristic of WMN and forwards packets along multiple paths. Second, in *TCP-ARQ* relays only forward the packets received from the upstream nodes and the coding is performed end-to-end. In our scheme, intermediate nodes re-encode packets received from different upstream neighbors, on a hop-by-hop basis. In the next sections we discuss in more detail the mechanisms that we use to enable online network coding for multipath schemes.

### B. Online loss estimation and rate adaptation

The rate at which nodes need to forward linear combinations to recover from losses remains an open research question. If the rate is too low, due to the unreliability of the wireless medium, receivers may not be able to decode. On the other hand, if the rate is too high, nodes may receive redundant linear combinations that consume network resources, but are not innovative. Moreover, since the wireless channel is variable in time, the rate of sending coded packets needs to be updated frequently enough to take into account current channel conditions. With these considerations in mind, we introduce an algorithm to estimate the loss between any two nodes and to distributedly compute the rate at which each node should forward linear combinations.

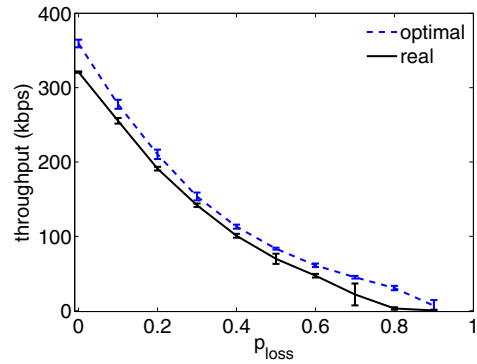


Fig. 2. Evaluation of the loss estimation algorithm for the topology in Fig. 1.

In order to estimate the loss, each node  $N_k$  keeps the following information:

- $p_i$ : a list of the *ids* of the packets sent to each of its downstream neighbors,  $N_i$ ;
- $r_i$ : the total number of packets that each of its downstream neighbors  $N_i$  reports it had received from  $N_k$ ;
- $s_{kl}$ : the *id* of the last packet that node  $N_k$  received from each of its upstream neighbors,  $N_l$ ;
- $t_{kl}$ : the total number of packets that  $N_k$  received from each of its upstream neighbors,  $N_l$ .

Node  $N_k$  updates the  $p_i$  list whenever it sends a packet to downstream node  $N_i$ .  $s_{kl}$  and  $t_{kl}$  are updated with each reception of a new packet from upstream neighbor  $N_l$ . Note that the update is done even if the packet is not innovative.

Due to the broadcast nature of the wireless medium, a node may overhear the transmissions of its downstream neighbor, and we take advantage of this feature as follows. Whenever  $N_k$  has to send a packet, it piggybacks  $s_{kl}$  and  $t_{kl}$  in the header for each of its upstream nodes,  $N_l$ . Next, its upstream neighbors can pick up the packet and find out the information they need to estimate the loss. Since the destination does not forward any linear combination, the previous approach cannot be used. However, the destination needs to send TCP ACKs to the sender, so it piggybacks  $s_{kl}$  and  $t_{kl}$  on these packets.

Once a node  $N_k$  receives feedback from one of its next hops, say  $N_i$ , it updates the information for the corresponding hop and computes the loss towards that hop, according to Alg. 1. If the node determines that a packet has been lost, it sends a redundant linear combination and adjusts the sending rate taking into account the total estimated loss. The total loss that  $N_k$  sees is given by:  $loss_k = \prod_{j=1}^{n_h} loss_{kj}$ , where  $n_h$  represents the number of downstream nodes of relay  $N_k$ .

We evaluate our loss estimation algorithm for the topology in Fig. 1, where two relays forward packets to destination. For the *optimal* curve, the nodes send packets at the optimal redundancy rate, which is computed based on the given loss probability. For the *real* case when the nodes use Alg. 1, the throughput is very close to the optimal one, see Fig. 2. Note that our loss estimation algorithm is accurate, and it does not incur any cost, since it piggybacks the needed information on the packets sent in the network.

### C. Hybrid credit-based scheme

When multiple paths are used in parallel, one important decision is how much of the traffic needs to be sent through

**Algorithm 1 Loss estimation.** Node  $N_k$  uses the feedback received from  $N_i$  to estimate the loss towards  $N_i$ ,  $loss_{ki}$

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- 1: **if** node  $N_k$  receives  $s_{ik}$  and  $t_{ik}$  from downstream neighbor  $N_i$  **then**
  - 2:   count no. pkts that  $N_k$  sent to  $N_i$ ,  $w_s = |C|$ , where  $C = \{p_i(j)/p_i(j) \leq s_{ik}, j = 1 : size(p_i)\}$
  - 3:   compute no. pkts that  $N_i$  received from  $N_k$ ,  $w_r \leftarrow t_{ik} - r_i$
  - 4:    $loss_{ki} = \frac{w_s - w_r}{w_s}$
  - 5:    $r_i \leftarrow t_{ik}$
  - 6:   erase  $p_i(j)$  for which  $p_i(j) \leq s_{ik}$
  - 7: **end if**
- 

each path. For the example in Fig. 1, if each node  $A$ ,  $B$  and  $C$  generates a linear combination every time it receives a packet from the source, it results in an explosion of the rate, with the destination receiving several packets that are not innovative.

To address this issue, [5] and [6] associate a credit with each packet sent in the network. The credits are created by the source, transferred to the downstream nodes and consumed at the destination. For *CoMP*, we use a hybrid credit-based scheme which has two parts. First, credits are generated at source and transferred to the forwarders, as the schemes mentioned above do. Second, credits can be generated by intermediate nodes as well whenever they detect a loss, which differentiates our approach from the existing ones. This second part enables each node to compute locally and distributedly the rate that it needs to send to recover the losses.

#### D. Congestion control

For multipath schemes in WMN, where multiple flows can traverse the same set of links, one must ensure fairness and balance the load among the available paths. To this end, we introduce a congestion control mechanism to select a forwarder for a packet, based on the *backpressure* methodology [9], which allows a node to send packets to a neighbor as long as the neighbor is less congested. The level of congestion is given by the size of the queue, i.e. the more packets are queueing at a node, the more congested the node is. For the congestion control mechanism, each node  $N_k$  keeps the following information for every flow that it forwards:

- an output queue,  $output\_buffer_i, i = 1 : n_f$ , where  $n_f$  is the number of flows that node  $N_k$  forwards;
- the queue sizes of its next hops for each flow,  $q_{ij}, i = 1 : n_f, j = 1 : n_{hi}$ , where  $n_{hi}$  is the number of next hops that  $N_k$  has for flow  $i$ .

Whenever the node has the opportunity to transmit a packet in the wireless medium, it first selects the flow for which to forward a packet, as the one for which it queues the highest number of packets (see Alg. 2). After the flow is selected,  $N_k$  chooses the forwarder to be the node with the shortest output queue, say  $N_h$ , as long as the backpressure condition holds.

Next,  $N_k$  removes the first packet from the  $output\_buffer_f$  and it adds the packet id in  $p_h$ , the list of packets sent to  $N_h$ . It adds in the header of the packet the size of its own queue,  $q_{fk}$  for backpressure computation and for each of its upstream neighbors  $N_l$ , the *id* of the last received packet,

**Algorithm 2 Flow scheduling and forwarder selection.** When sending a packet, node  $N_k$  selects a flow  $f$  and chooses the forwarder for that flow. Next, it updates the state information and it sends the first packet from the  $output\_buffer_f$ .

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- 1: select the flow  $f$  such that:
  - 2:  $f = \operatorname{argmax}_i size(output\_buffer_i), i = 1 : n_f$
  - 3: select forwarder:  $N_h = \operatorname{argmin}_j q_{fj}, j = 1 : n_{hf}$
  - 4: remove  $P_0$  from  $output\_buffer_f$
  - 5: add  $id(P_0)$  in  $p_h$  list
  - 6: add  $q_{fk}$  and  $(s_{kl}, t_{kl})$  for each upstream neighbor  $N_l$ , in the header of  $P_0$
  - 7: send  $P_0$
- 

$s_{kl}$ , and the total number of received packets,  $t_{kl}$ , for loss estimation. Finally,  $N_k$  sends the packet.

#### E. System Design

For each flow  $f$ , every node keeps a  $coding\_buffer_f$  and an  $output\_buffer_f$ . The  $coding\_buffer_f$  contains packets that the node uses to generate linear combinations. The source stores here native, uncoded packets, while the other nodes store linear combinations. The  $output\_buffer_f$  contains coded packets that will be sent in the network. Packets are removed from the  $output\_buffer_f$  whenever the node has the possibility to transmit a packet. In this case, a node first runs Alg. 2 to select a flow  $f$  and a forwarder  $N_h$ . After that, the node removes the first packet from the  $output\_buffer_f$ , it updates the statistics for node  $N_h$  and it sends the packet.

**Sender.** When a native packet of flow  $f$  is produced, the source stores it in the  $coding\_buffer_f$ . Note that source performs *online coding*, which means that it generates a new linear combination every time it receives a new packet. To generate a coded packet, the source mixes all the packets from the  $coding\_buffer_f$  and stores the resulting linear combination in the  $output\_buffer_f$  (see Alg. 3). When the source receives a TCP ACK for flow  $f$ , it removes the oldest packet from the  $coding\_buffer_f$ , thus sliding the coding window.

**Algorithm 3 Online coding at source.** If a data packet arrives, the source stores it and generates a linear combination.  $m$  represents the size of the  $coding\_buffer_f$ . The coefficients  $c_i$  are randomly chosen from  $GF(2^{16})$ . If it receives a TCP ACK, the source removes the oldest packet from the  $coding\_buffer_f$ .

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- 1: receive packet  $P_k$  of flow  $f$
  - 2: **if**  $P_k$  is DATA packet **then**
  - 3:   store packet in the  $coding\_buffer_f$
  - 4:   generate  $LC_k = \sum_{i=1}^m c_i P_i$
  - 5:   store  $LC_k$  in the  $output\_buffer_f$
  - 6: **else**
  - 7:    $P_k$  is TCP ACK
  - 8:   remove  $P_0$  from  $coding\_buffer_f$
  - 9: **end if**
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**Relays.** When receiving a coded packet  $LC_r$  from flow  $f$ , an intermediate node  $N_k$  first removes from the  $coding\_buffer_f$  those linear combinations that contain native packets older than those mixed in  $LC_r$ . Then, he updates the state for the upstream neighbor  $N_l$  who sent  $LC_r$ . The updated



information is the  $id$  of the last received packet  $s_{kl}$ , and the total number of received packets,  $t_{kl}$ . Next, if the coded packet is innovative,  $N_k$  stores it in the coding\_buffer $_f$ , otherwise  $N_k$  drops it (see Alg. 4). A relay generates and forwards a linear combination when it receives a credit. Note that a linear combination of coded packets is also a linear combination of the original packets.

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**Algorithm 4 Coding at relays.** The relay  $N_k$  receives a packet of flow  $f$  from neighbor  $N_l$ .  $m$  represents the size of the coding\_buffer $_f$ . The coefficients  $c_i$  are chosen from  $GF(2^{16})$  at random.

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1: receive coded packet  $LC_r$  of flow  $f$ 
2: update coding_buffer $_f$ 
3:  $s_{kl} = id(LC_r)$ ;  $t_{kl} \leftarrow t_{kl} + 1$ 
4: if  $LC_r$  is innovative then
5:   store  $LC_r$  in the coding_buffer $_f$ 
6:   if receive credit associated to  $LC_r$  then
7:     generate  $LC_j = \sum_{i=1}^m c_i LC_i$ 
8:     store  $LC_j$  in output_buffer $_f$ 
9:   end if
10: else
11:   drop  $LC_r$ 
12: end if

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**Receiver.** When destination  $N_d$  receives a linear combination of flow  $f$ , it updates the  $id$  of the last received packet and the total number of received packets for the sender. Next, it stores the coded packet only if it is linear independent with all the packets received previously. Since the source is coding online, then the destination decodes a native packet on the fly, if possible, and passes it up to the TCP layer (see Alg. 5). If no native packet can be decoded, the destination acknowledges the reception of the current packet to the source.

### III. PERFORMANCE EVALUATION

We evaluate our protocol through extensive simulations in *ns-2.33* [1] and compare it to improved versions of *Horizon* [7], *MORE* [5], and *TCP-ARQ* [8]. *Horizon* estimates the TCP window and signals congestion to the TCP sender whenever the estimated value reaches a certain threshold. In our simulations, we feed *Horizon* with the actual TCP window size, not an estimate. Also, *MORE* sends probe packets periodically to estimate the loss in the network and adjusts the rate of sending linear combinations accordingly. For our implementation of *MORE* we use our algorithm to estimate losses instead, eliminating the overhead of sending probes. For *TCP-ARQ*, only the source sends redundant linear combinations and the authors state that the redundancy factor  $R$  should be adjusted online. Since the authors do not give any indication on how to adjust  $R$  online, we use our loss estimation algorithm Alg.1.

#### A. Simulation Setup

We run the protocols over the Roofnet topology provided at [2]. The losses are given by the Shadowing propagation model and depend on the distances between the nodes. We choose randomly 100 pairs of (source, destination) nodes and compute the routing information in MATLAB using a modified

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**Algorithm 5 Decoding at destination.** The destination  $N_d$  receives a linear combination.

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1: receive coded packet  $LC_k$  of flow  $f$  from neighbor  $N_l$ 
2:  $s_{dl} = id(LC_k)$ ;  $t_{dl} \leftarrow t_{dl} + 1$ 
3: if  $LC_k$  is innovative then
4:   store  $LC_k$  in the coding_buffer $_f$ 
5:   if a packet can be decoded then
6:     deliver the decoded packet to the TCP layer
7:   else
8:     send an ack to the sender
9:   end if
10: else
11:   drop packet  $LC_k$ 
12: end if

```

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version of the directed diffusion algorithm, reinforcing up to  $d$  paths [10]. By varying the number of reinforced paths  $d$ , we vary the number of downstream neighbors that a node can pick as next-hops for the packets. The average path length is of 2.5 hops.

We disable RTS/CTS for all experiments. In order to simulate heavy loss conditions, we also disable MAC layer retransmissions for all the experiments. The rest of the parameters have the default *ns-2.33* values.

We use the following metrics to evaluate our protocol:

- *throughput* measured at destination (decoded rate);
- *efficiency*, defined as the ratio of the goodput at destination to the total throughput transmitted in the network;
- *relative improvement of CoMP* over the other protocols, defined as the ratio of the throughput obtained with *CoMP* to the throughput obtained with the other protocols;
- *aggregate throughput* only for the case when multiple flows are running in parallel in the network. The aggregate throughput is computed as the sum of the individual throughput of all flows that run simultaneously.

For all the figures, each point is the average of at least 10 runs such that the standard deviations for the different protocols do not overlap.

#### B. Overall Results

In this section we discuss the results for different scenarios.

1) *Multiple paths*: In this case, there is only one flow active in the network at a time. Note from Fig. 3(a) that *CoMP* achieves significantly higher throughput than the other protocols, and it can yield an improvement of 10x over *TCP-ARQ* and more for *Horizon* and *MORE* (see Fig. 3(c)). There are about 20% of flows in the network for which the source and the destination are one hop away, and for those flows *TCP-ARQ* has a similar performance to *CoMP*. If the paths are longer, then *TCP-ARQ* is more sensitive to losses. *Horizon* achieves a lower throughput because it relies on TCP retransmissions to recover every lost packet. *MORE*'s throughput decreases significantly if the generation size increases due to the additional delay introduced by coding.

Regarding the efficiency, we compute it as the ratio of the decoded rate at destination to the total rate sent into the network, and therefore for a 2-hop long flow, the maximum efficiency can be equal to 0.5. *CoMP* generally outperforms

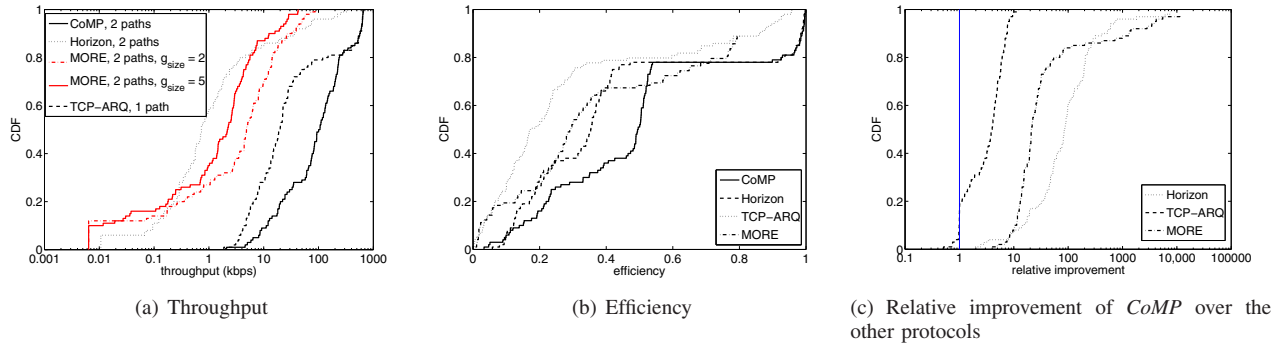


Fig. 3. Roofnet topology with only one flow active in the network. Nodes have at most two downstream neighbors (*i.e.* two reinforced paths,  $d = 2$ ).

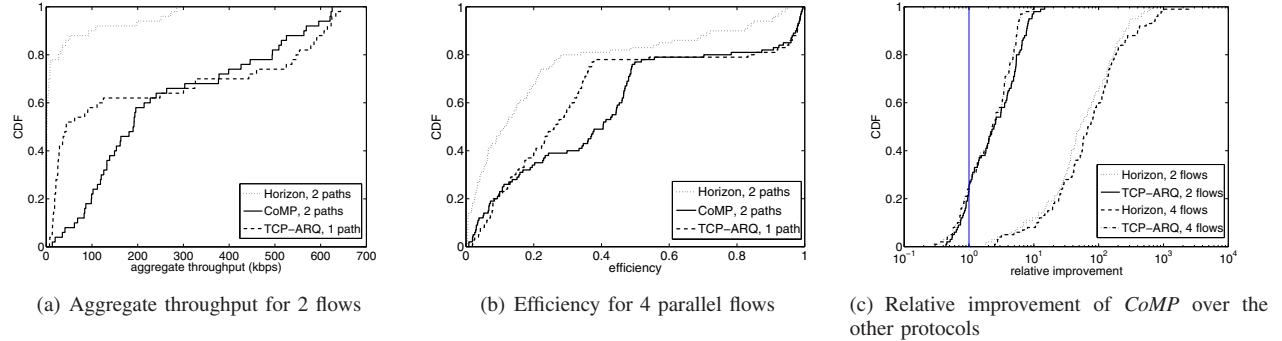


Fig. 4. Roofnet topology with multiple flows running in parallel. Nodes have at most two downstream neighbors (*i.e.* two reinforced paths,  $d = 2$ ).

the other protocols, except for the 20% flows that are one-hop long and *TCP-ARQ* is equally efficient (see Fig. 3(b)).

2) *Multiple flows*: In Fig. 4 we show the results for the case when multiple flows run in parallel in the network. Since *MORE*'s performance degrades very quickly as the generation size increases, we do not take it into account for this case.

Notice from Fig. 4(a) that for 60% of the flows, the aggregate throughput obtained when two sessions run concurrently in the network is higher with *CoMP* than with *TCP-ARQ*. This happens for performance-challenged flows, where paths are long and experience high losses. For these situations, using one extra path together with coding hop-by-hop instead of end-to-end increases throughput. On the other hand, for the case when paths are short and possibly physically overlapping, using one more path increases the interference, thus having a negative effect on the throughput obtained with *CoMP*. The effect of the interference can also be noticed from Fig. 4(c), where 20% of flows have a relative improvement less than 1, meaning the throughput is lower with *CoMP* than with *TCP-ARQ*. *Horizon* achieves a throughput close to 0 for almost 80% of the flows, due to the fact that it does not offer any reliability in an extremely volatile environment.

In terms of efficiency, *CoMP* outperforms the other protocols for 55% of the flows. For the 20% of one-hop flows, *TCP-ARQ* achieves equal efficiency, since multiple paths cannot be exploited. There are another 25% of flows for which *CoMP* is slightly less efficient than *TCP-ARQ*, because even if with *CoMP* the destination receives a higher throughput, there are also more packets sent into the network, lowering efficiency.

#### IV. CONCLUSIONS

In this paper we presented *CoMP*, a network coding multipath protocol that improves TCP performance in lossy environ-

ments by combining online coding and multipath techniques. *CoMP* uses an online algorithm to estimate current loss conditions in the network and to adjust the rate of sending coded packets. *CoMP* relies on a feedback mechanism for TCP, where destination acknowledges the independent linear combinations that it receives, instead of decoded packets. All these features allow a seamless interaction between *CoMP* and TCP. We show through extensive simulations the advantages of our protocol over the current state-of-the-art in terms of throughput and efficiency.

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