

**ELEN E6312**  
**Spring 2004**  
**Prof. P. Kinget**

**Midterm**

**Instructions:**

- *You are allowed to use a calculator; please CLEAR the calculator memory before the exam!*
- *You are allowed to use one side of a letter size sheet with formulas.*
- Clearly write your name on every page and every examination booklet you hand in.
- You are graded for your derivations. *Results without a clear derivation do not receive a grade.*
- Do your derivations and calculations in the examination booklets. Clearly indicate which question the derivation is for.
- Give all answers their appropriate S.I. Unit or indicate that the number is unitless.
- Hand in clean and clear derivations.
  
- If you think information is missing to solve the question, make a reasonable assumption and document your assumptions.
- Always make reasonable approximations but document and justify which approximations you are making.

You can assume the following transistor characteristics:

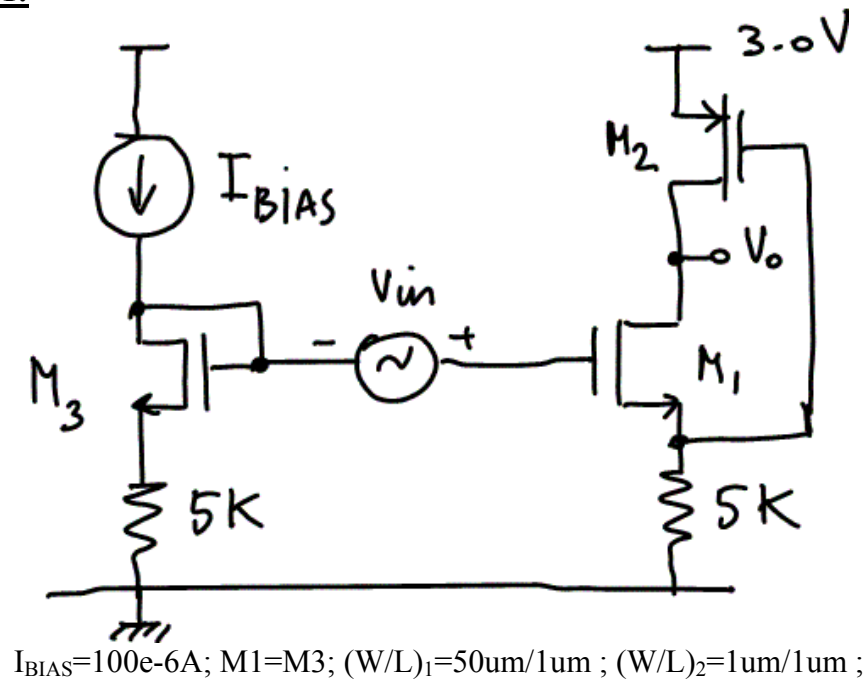
- $(\mu C_{ox})_{nMOS} = 100 \text{ uA/V}^2$  and  $(\mu C_{ox})_{pMOS} = 50 \text{ uA/V}^2$
- $V_{Tn} = |V_{Tp}| = 0.5 \text{ V}$
- $V_{AL} = 10 \text{ V/um}$
- $n=1$  (sub-threshold slope)

For devices in *strong inversion*, you can use the following simplified I/V relationships:

- Saturation:  $I_{DS} = \mu C_{ox} / 2 (W/L) (V_{GS} - V_T)^2 (1 + V_{DS}/V_A)$
- Non-Saturation:  $I_{DS} = \mu C_{ox} (W/L) (V_{GS} - V_T) V_{DS}$

Good luck !

**Question 1:**

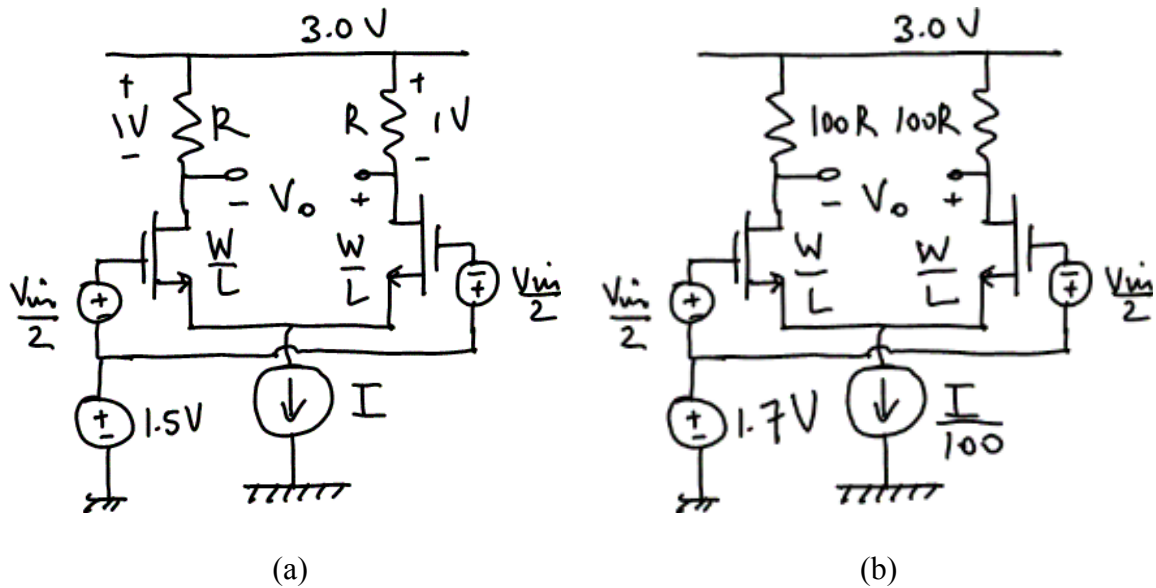


- 1) Find the DC bias point for the circuit
  - a) Put the node voltage of all nodes on the schematic.
  - b) Give the region of operation of all devices:
    - i) Saturation/non-Saturation,
    - ii) Strong/Moderate/Weak inversion.
  - c) Calculate the small signal equivalent circuit for all devices.

***If you cannot find the solution to part 1, make reasonable assumptions and solve for the symbolic expressions below.***

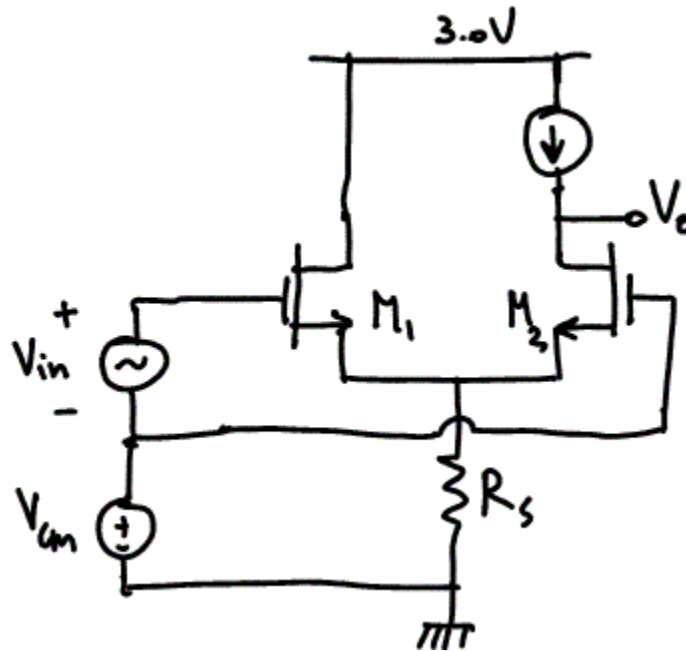
- 2) Find a symbolic expression for the small signal output impedance of the circuit. Calculate the value of the output impedance.
- 3) Find a symbolic expression for the small signal gain of the circuit. Calculate the value of the small signal gain.

**Question 2:**



- For circuit (a) the bias information is indicated on the schematic and the  $(V_{GS}-V_T)$  of the nMOS devices is 200mV; you can assume the early voltage of the transistors is infinitely large.
  - Find an expression for the small signal gain  $(V_o/V_{in})$ ,
  - and calculate its value.
- Circuit (b) uses the same devices but with a 100 times smaller bias current and 100 times larger load resistors; you can again assume the early voltage of the transistors is infinitely large.
  - Find an expression for the small signal gain  $(V_o/V_{in})$ ,
  - and calculate its value.

**Question 3:**



You can assume the circuit is properly biased and that all devices are operating in strong inversion and saturation with the following parameters:  $M_1=M_2$ ,  $g_{m1}=2\text{mS}$ ,  $r_{o1}=10\text{K}$ ;  $R_s=5\text{K}$

- 1) Find a symbolic expression for small signal gain ( $V_o/V_{cm}$ ) and calculate its value.
- 2) Find a symbolic expression for small signal gain ( $V_o/V_{in}$ ) and calculate its value.