

# Lecture 14: Source Separation

1. Sources, Mixtures, & Perception
2. Spatial Filtering
3. Time-Frequency Masking
4. Model-Based Separation

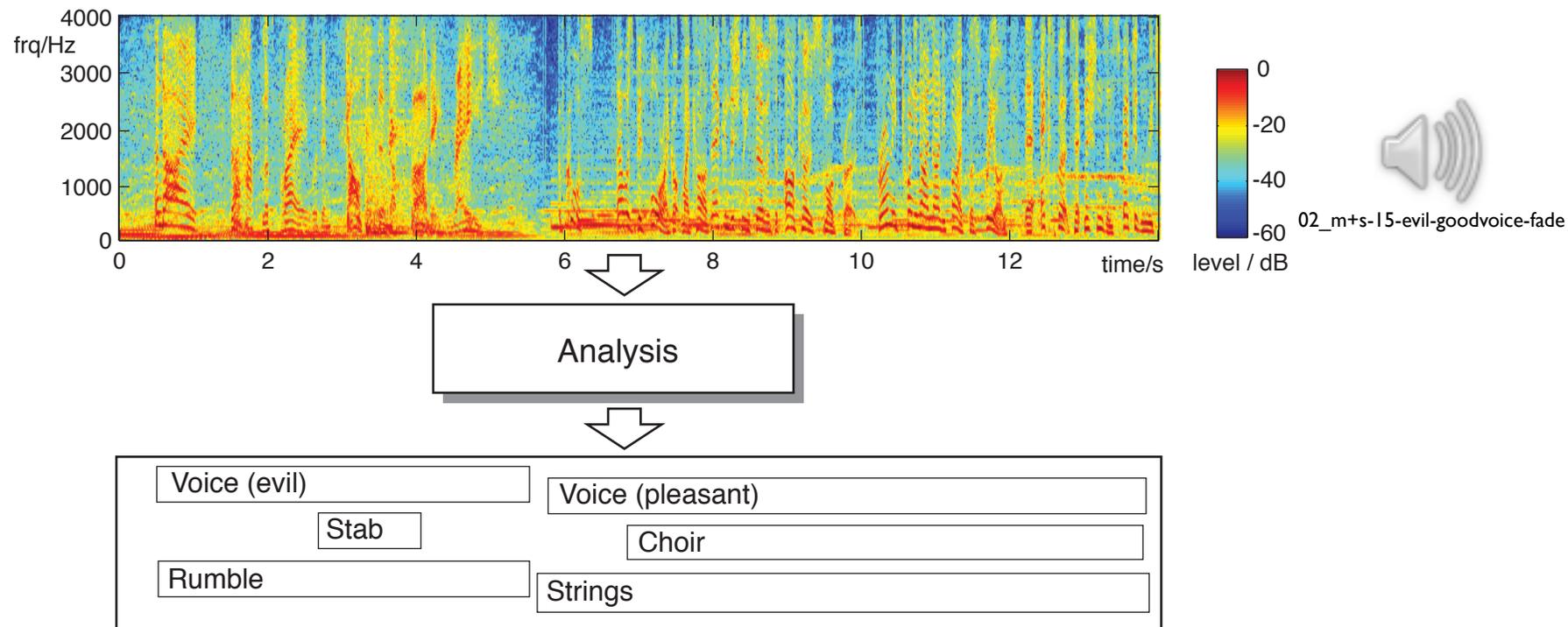
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# I. Sources, Mixtures, & Perception

- Sound is a **linear** process (superposition)
  - no “opacity” (unlike vision)
  - sources → “auditory scenes” (polyphony)

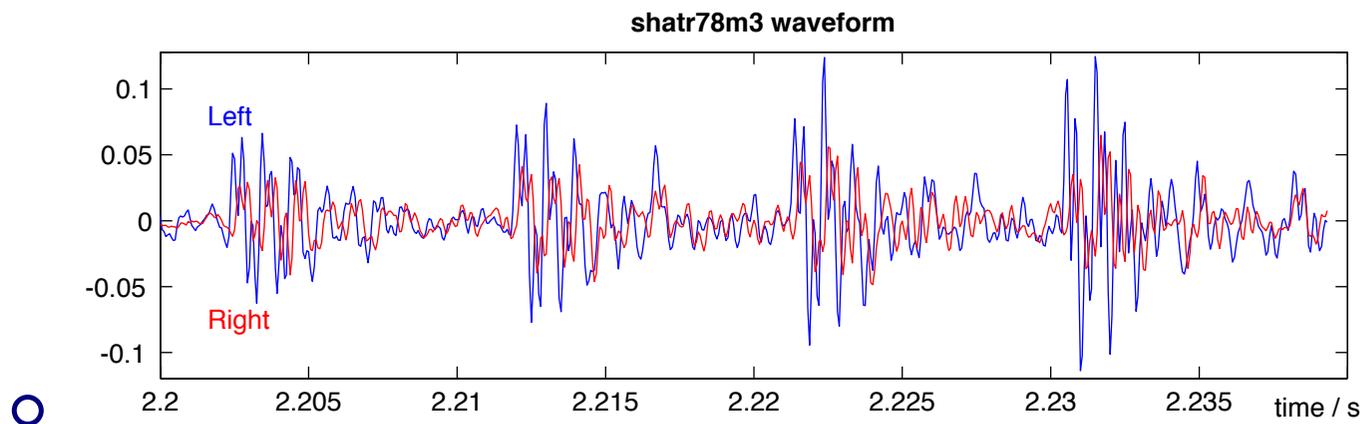
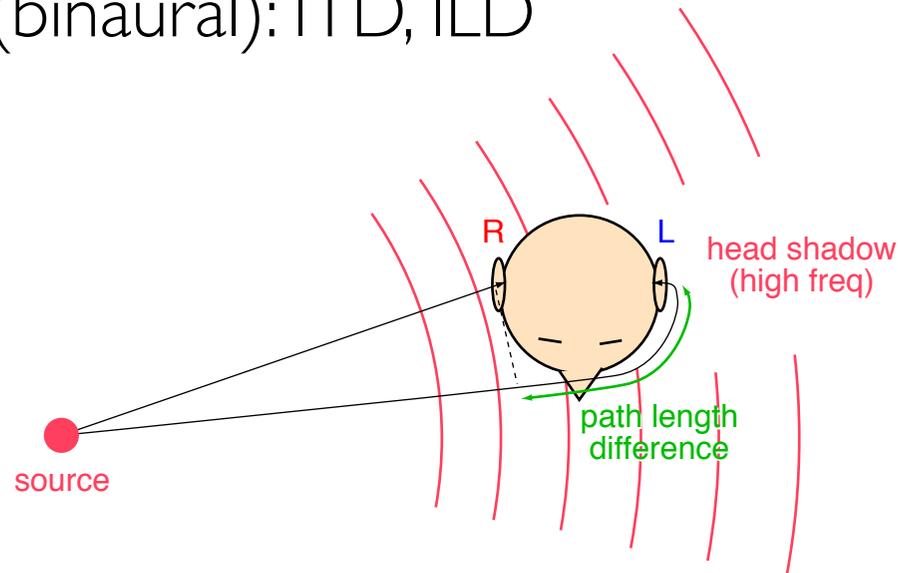


- Humans perceive discrete **sources**
  - .. a **subjective** construct

# Spatial Hearing

Blauert '96

- People perceive sources based on cues
  - spatial (binaural): ITD, ILD

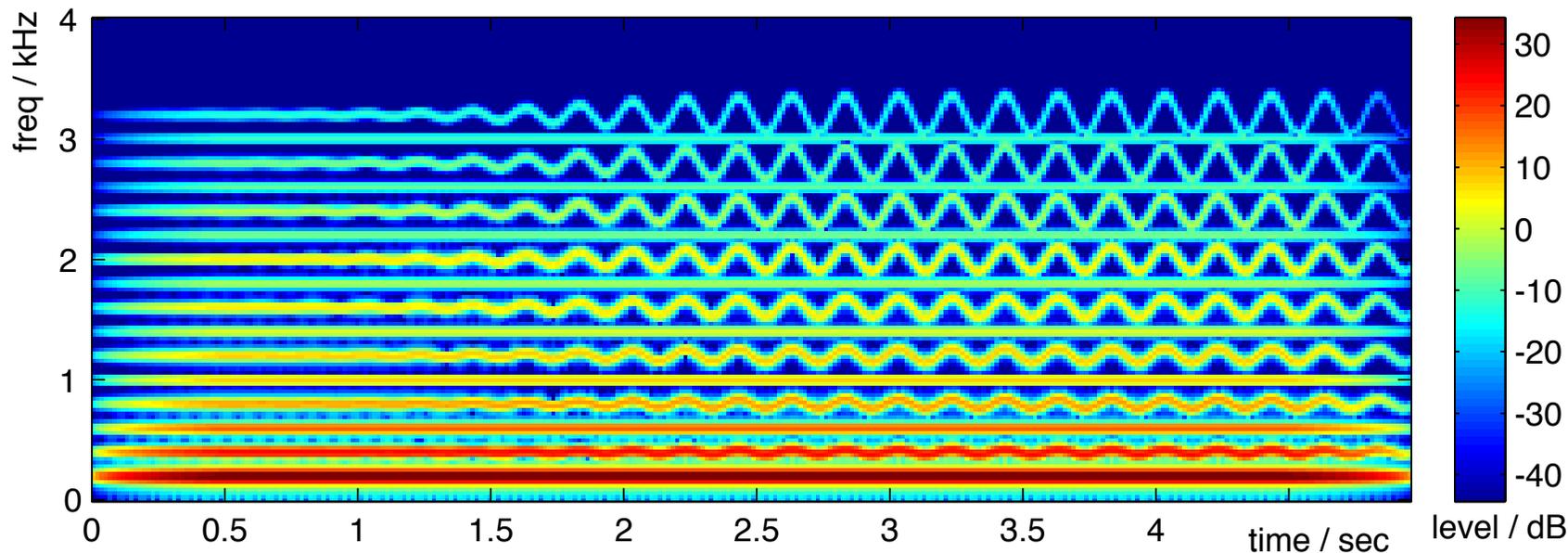


# Auditory Scene Analysis

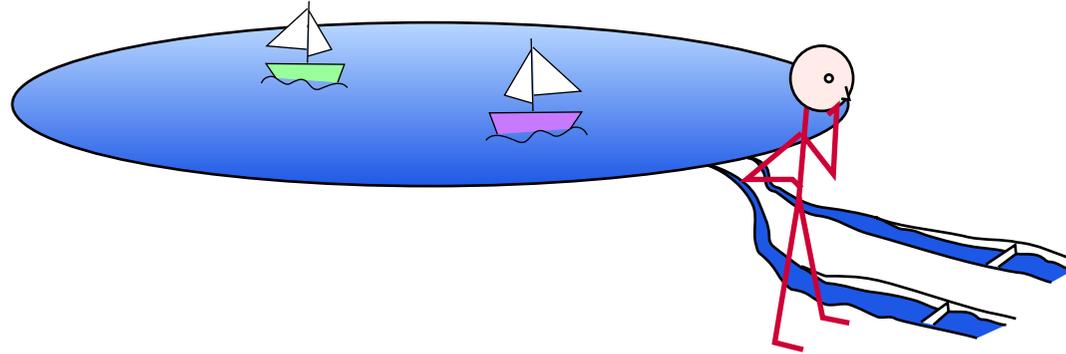
Bregman '90

- Spatial cues may not be enough/available
  - single channel signal
- Brain uses **signal-intrinsic cues** to form sources
  - onset, harmonicity

Reynolds-McAdams Oboe



# Auditory Scene Analysis



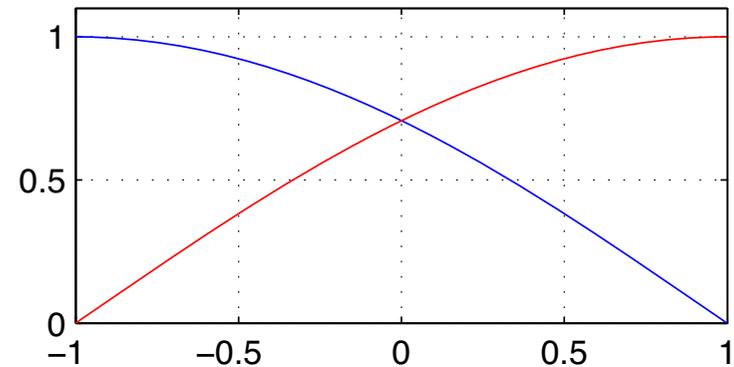
*“Imagine two narrow channels dug up from the edge of a lake, with handkerchiefs stretched across each one. Looking only at the motion of the handkerchiefs, you are to answer questions such as: How many boats are there on the lake and where are they?” (after Bregman’90)*

- **Quite a challenge!**

# Audio Mixing

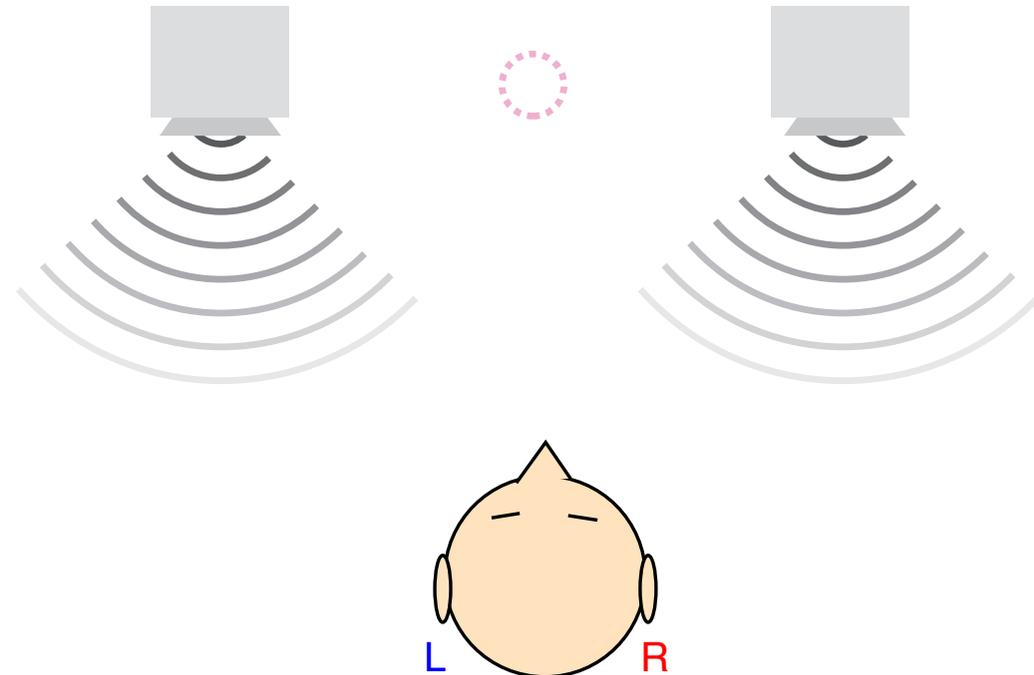
- Studio recording combines separate tracks into, e.g., 2 channels (stereo)

- different levels
- panning
- other effects



- Stereo Intensity Panning

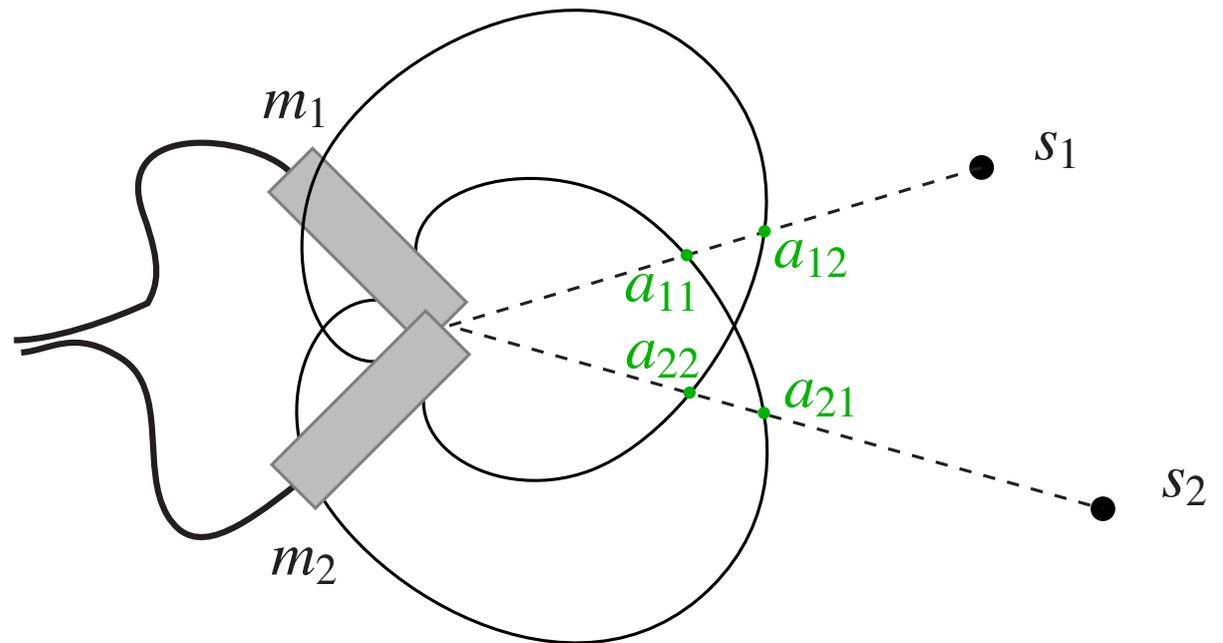
- manipulating ILD only
- constant power
- more channels: use just nearest pair?



# 2. Spatial Filtering

- **N** sources detected by **M** sensors
  - degrees of freedom
  - (else need other **constraints**)

- **Consider**  
**2 x 2 case:**
  - directional mics



- $\rightarrow$  mixing matrix:

$$\begin{bmatrix} m_1 \\ m_2 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} s_1 \\ s_2 \end{bmatrix} \Rightarrow \begin{bmatrix} \hat{s}_1 \\ \hat{s}_2 \end{bmatrix} = \hat{A}^{-1} m$$

# Source Cancellation

- Simple 2 x 2 case example:

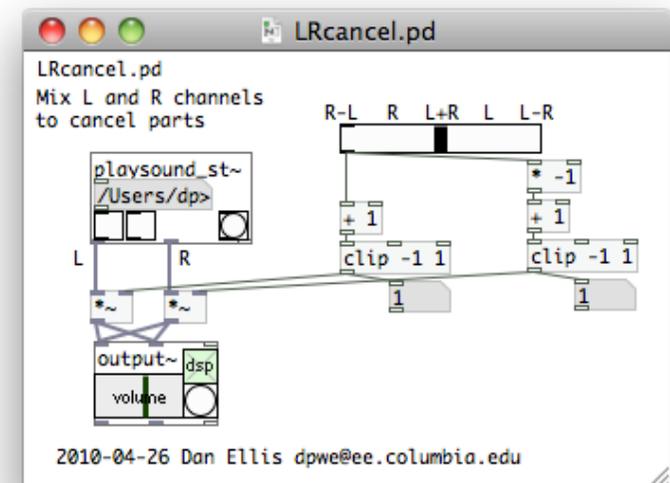
$$\begin{bmatrix} m_1 \\ m_2 \end{bmatrix} = \begin{bmatrix} 1 & 0.5 \\ 0.8 & 1 \end{bmatrix} \begin{bmatrix} s_1 \\ s_2 \end{bmatrix}$$

$$m_1(t) = s_1(t) + 0.5s_2(t)$$

$$m_2(t) = 0.8s_1(t) + s_2(t)$$

$$\Rightarrow m_1(t) - 0.5m_2(t) = 0.6s_1(t)$$

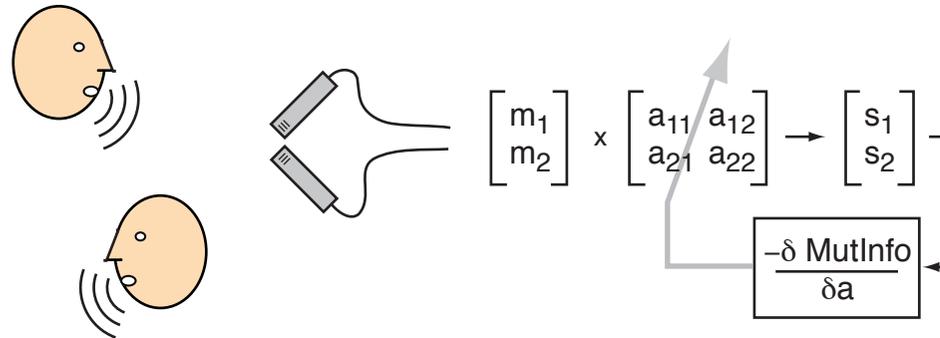
- if **no delay** and **linearly-independent** sums, can **cancel** one source per combination



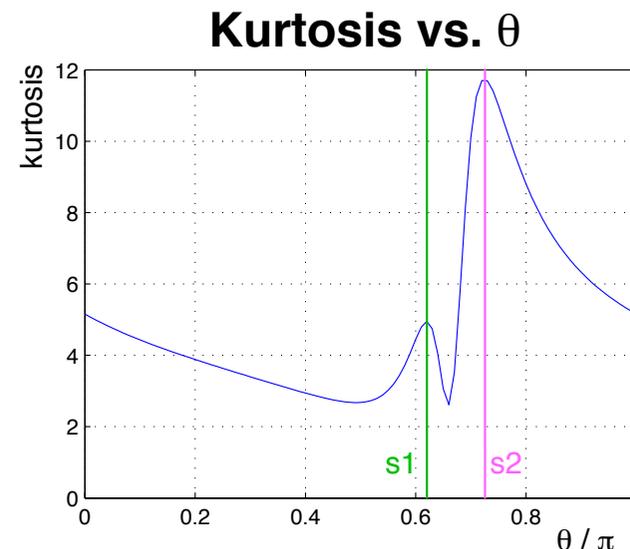
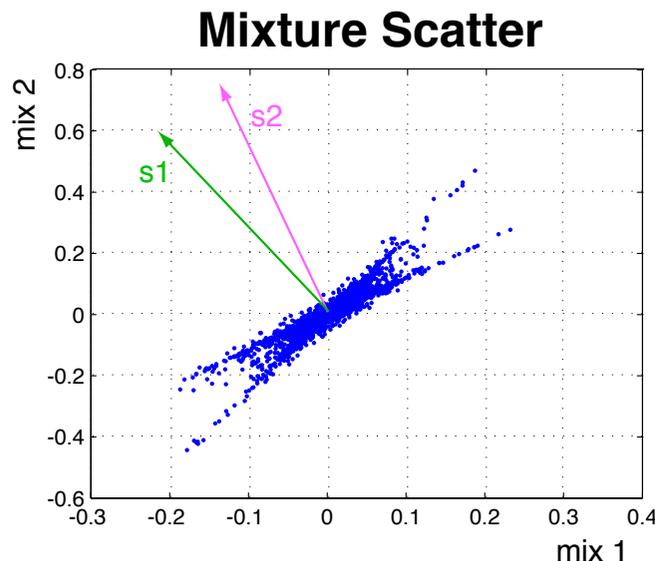
# Independent Component Analysis

Bell & Sejnowski '95

- Can separate “blind” combinations by maximizing **independence** of outputs



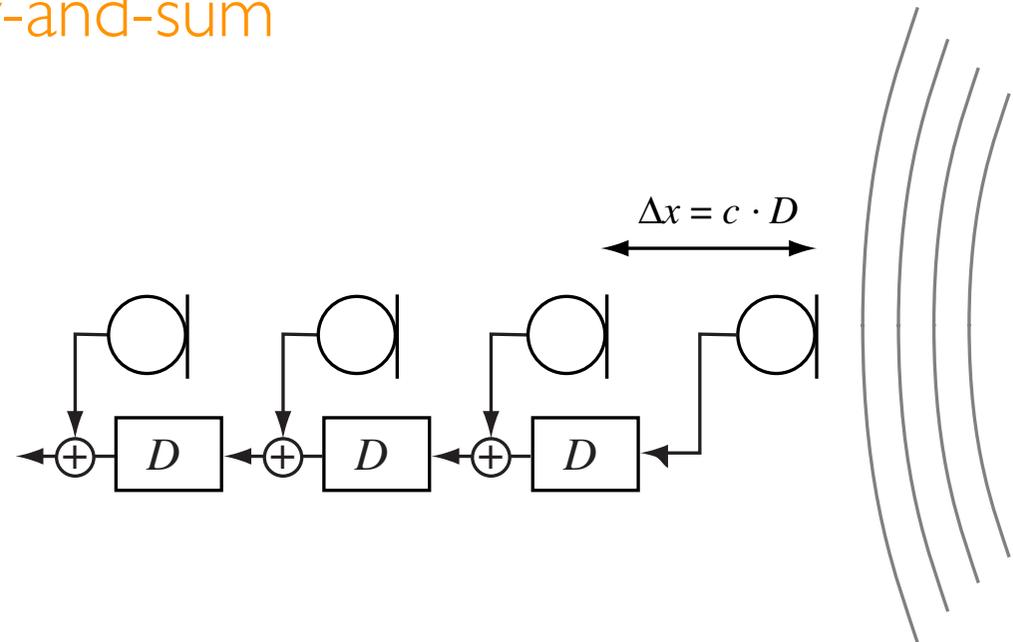
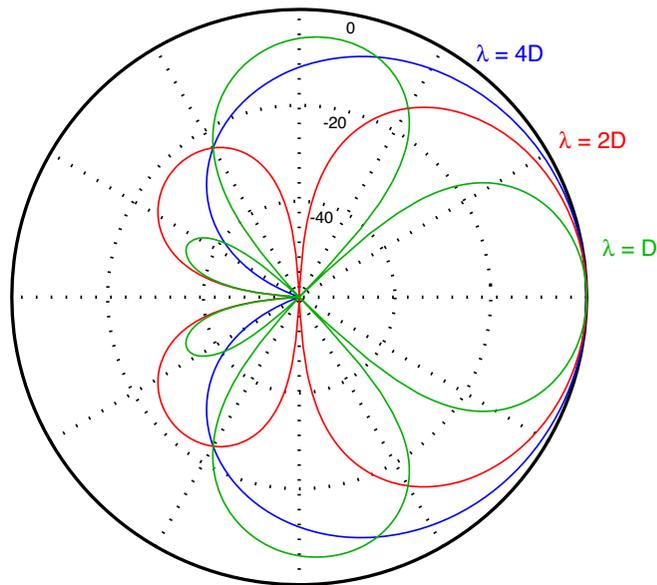
○ **kurtosis**  $kurt(y) = E \left[ \left( \frac{y - \mu}{\sigma} \right)^4 \right] - 3$  for independence?



# Microphone Arrays

Benesty, Chen, Huang '08

- If interference is **diffuse**, can simply **boost** energy from target direction
  - e.g. shotgun mic - **delay-and-sum**

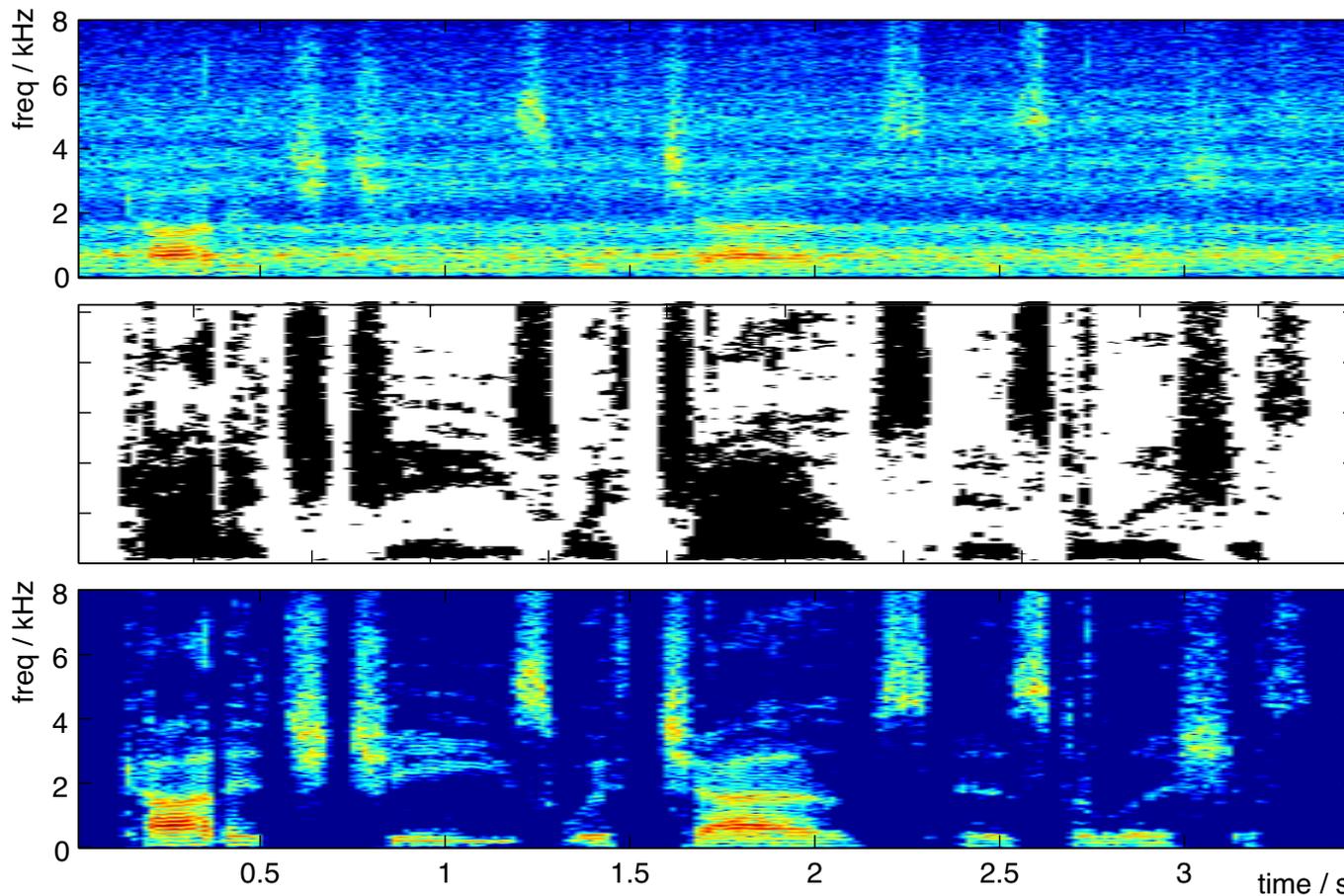


- off-axis spectral **coloration**
- many variants - filter & sum, sidelobe cancelation ...

# 3. Time-Frequency Masking

Brown & Cooke '94  
Roweis '01

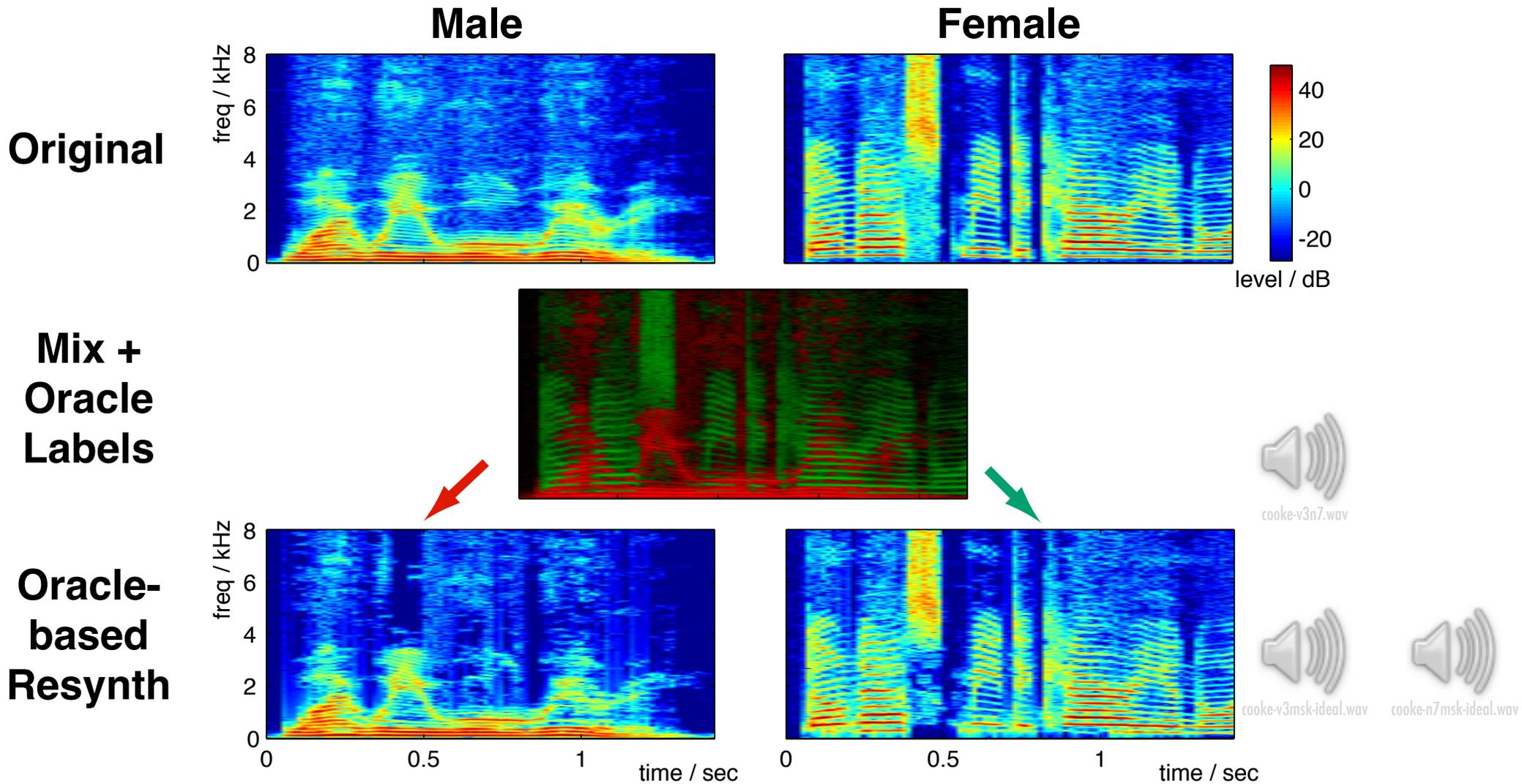
- What if there is only **one channel**?
  - cannot have fixed cancellation
  - but could have fast **time-varying** filtering:



- The trick is finding the right **mask**...

# Time-Frequency Masking

- Works well for overlapping **voices**

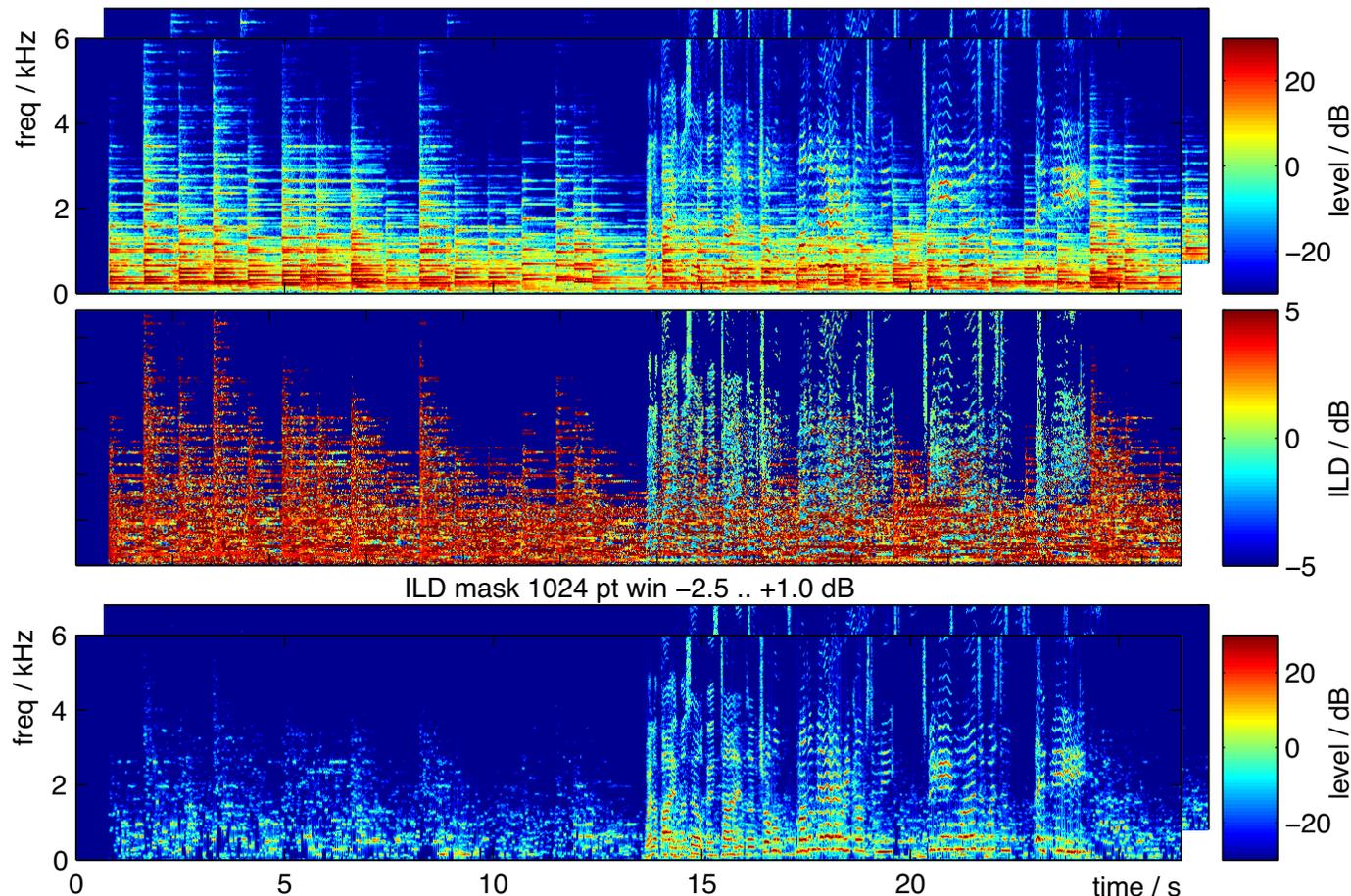


○ time-frequency resolution?

# Pan-Based Filtering

Avendano 2003

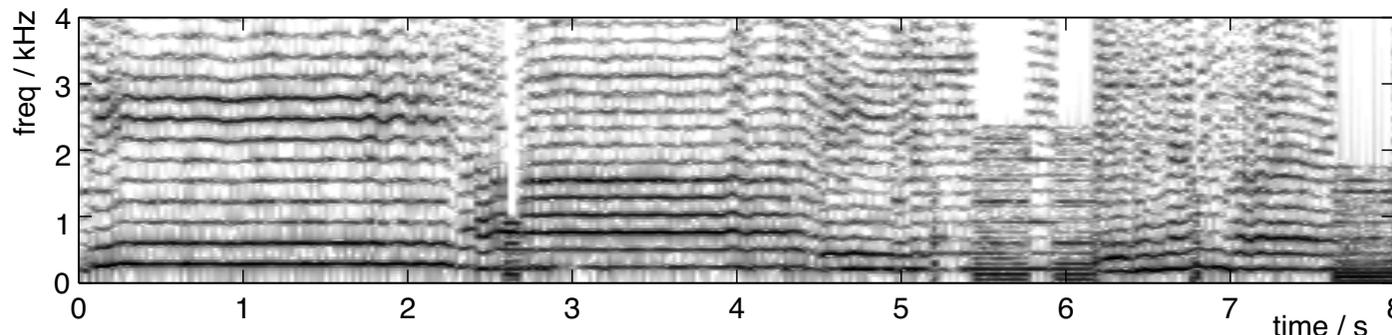
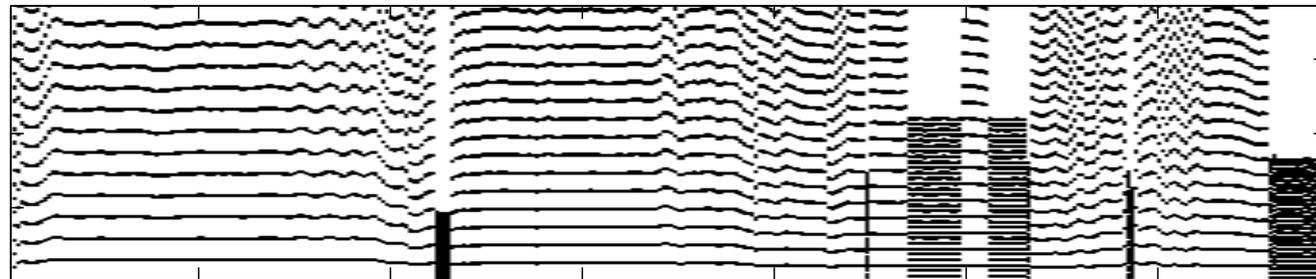
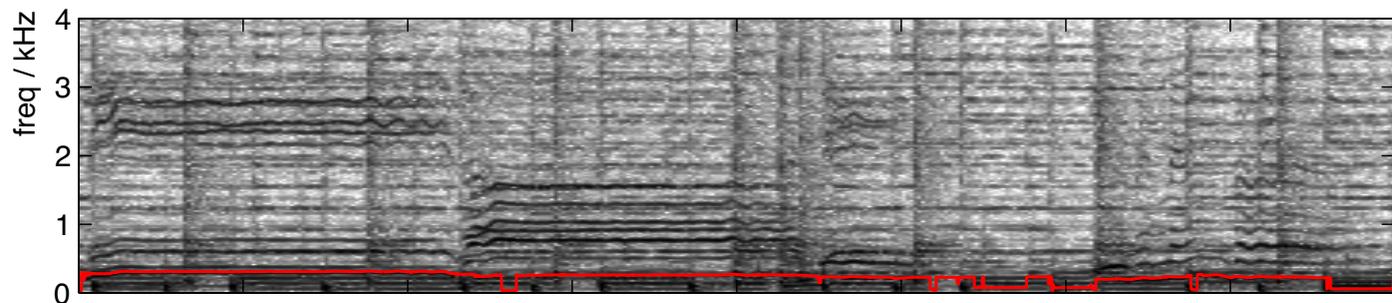
- Can use time-frequency masking even for **stereo**
  - e.g. calculate “panning index” as ILD
  - **mask** cells matching that ILD



# Harmonic-based Masking

*Denbigh & Zhao 1992*

- Time-frequency masking can be used to pick out **harmonics**
  - given **pitch track**, know where to expect harmonics



# Harmonic Filtering

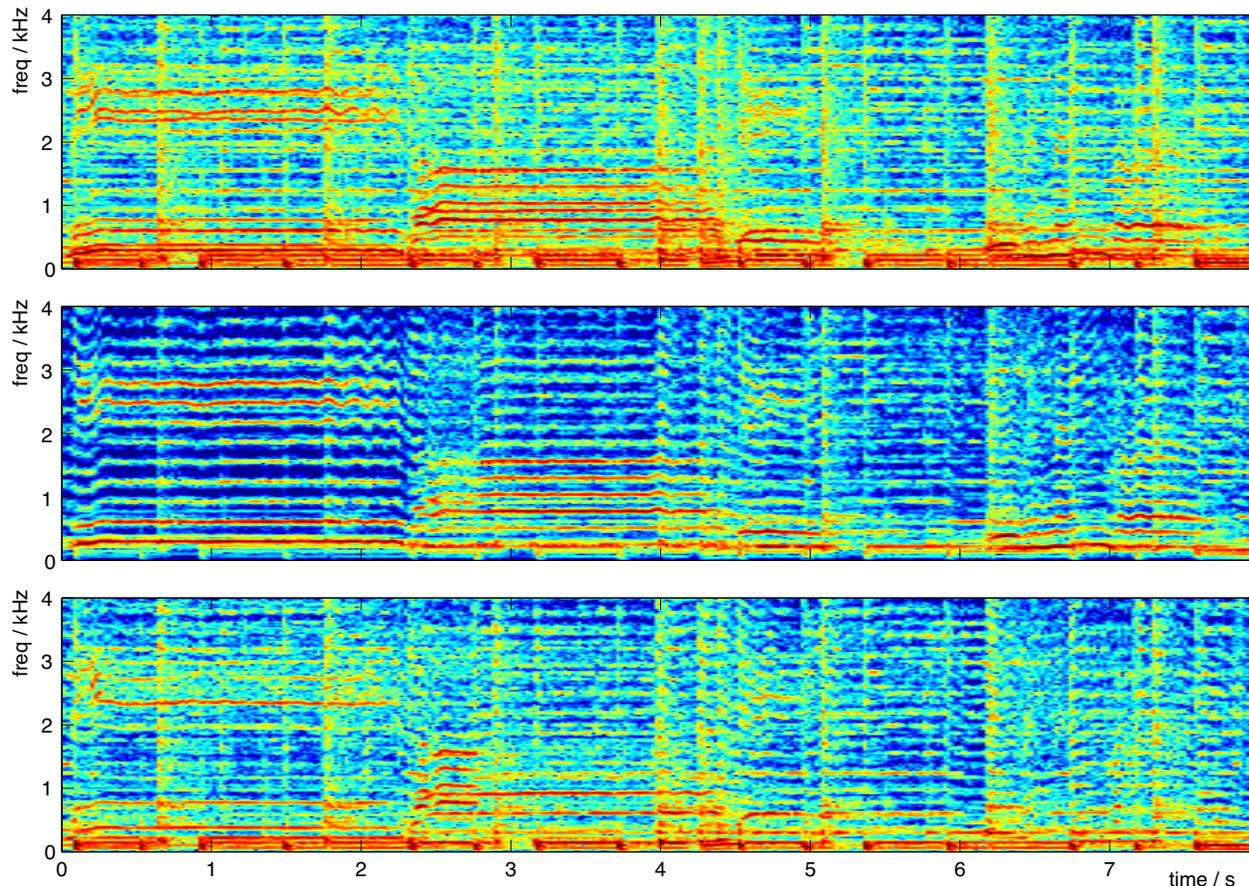
Avery Wang / 1995

- Given pitch track, could use **time-varying comb filter** to get harmonics

- or: isolate each harmonic by **heterodyning**:

$$\hat{x}(t) = \sum_k \hat{a}_k(t) \cos(k\hat{\omega}_0(t)t)$$

$$\hat{a}_k(t) = LPF\{|x(t)e^{-jk\hat{\omega}_0(t)t}|\}$$



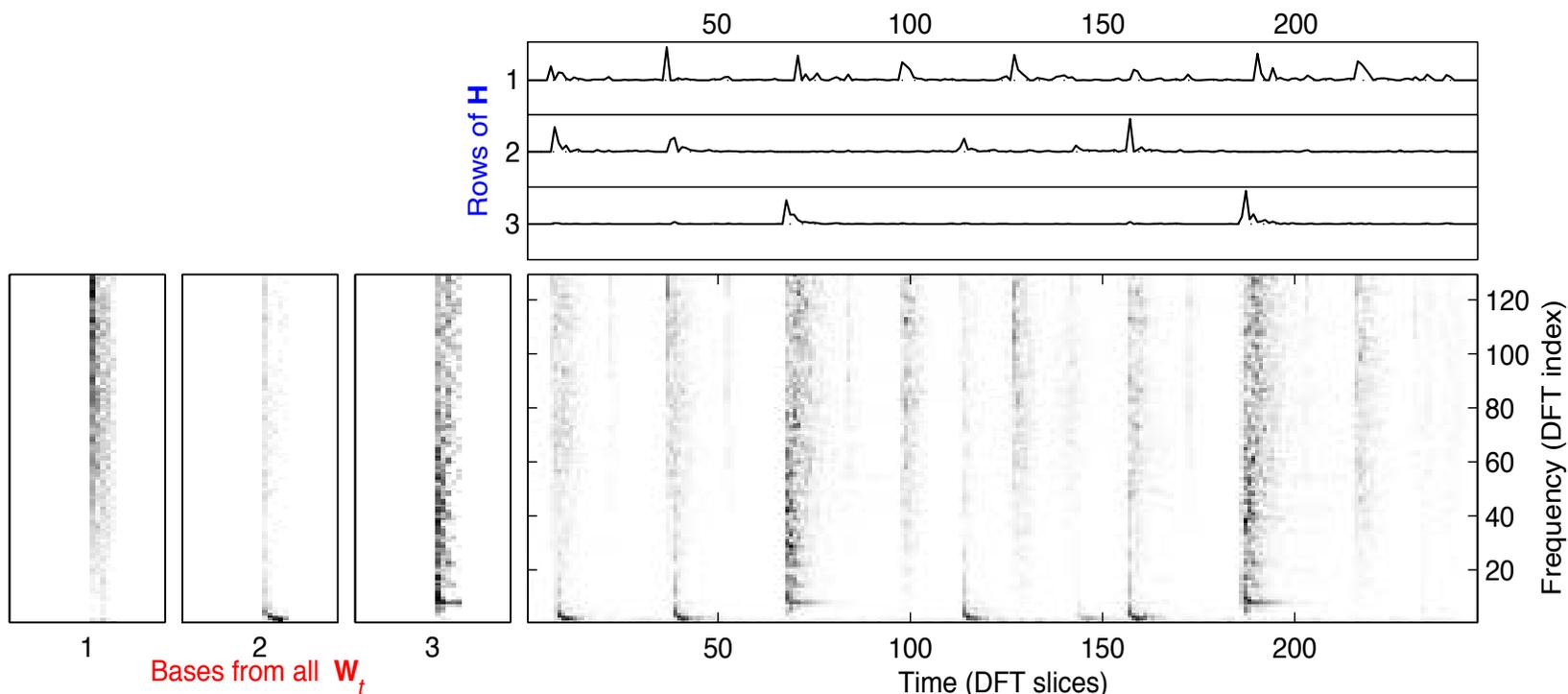
# Nonnegative Matrix Factorization

- Decomposition of spectrograms into **templates** + **activation**

$$\mathbf{X} = \mathbf{W} \cdot \mathbf{H}$$

- fast & forgiving **gradient descent** algorithm
- fits neatly with **time-frequency masking**

Lee & Seung '99  
Abdallah & Plumbley '04  
Smaragdakis & Brown '03  
Virtanen '07



Virtanen '03  
sounds



Smaragdakis '04

# 4. Model-Based Separation

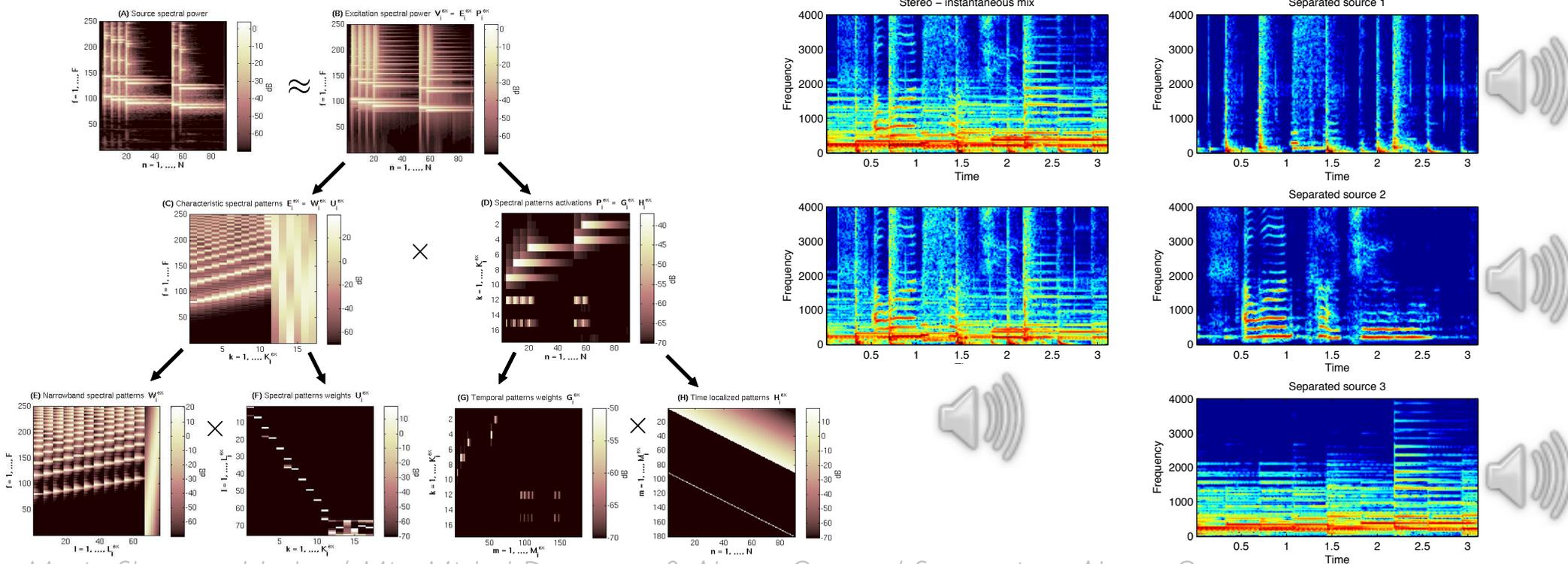
- When  $N$  (sources)  $>$   $M$  (sensors), need additional **constraints** to solve problem
  - e.g. assumption of single dominant pitch
- Can assemble into a **model**  $M$  of source  $s_i$ 
  - defines set of “possible” waveforms
  - ..probabilistically:  $Pr(s_i|M)$
- Source separation from mixture as **inference**:
  - $\mathbf{s} = \{s_i\} = \arg \max_{\mathbf{s}} Pr(\mathbf{x}|\mathbf{s}, A)P(A) \prod_i Pr(s_i|M)$

where  $Pr(\mathbf{x}|\mathbf{s}, A) = \mathcal{N}(\mathbf{x}|A\mathbf{s}, \nu)$

# Source Models

Ozerov, Vincent & Bimbot 2010  
<http://bass-db.gforge.inria.fr/fasst/>

- **Can constrain:**
  - source spectra (e.g. harmonic, noisy, smooth)
  - temporal evolution (piecewise-continuous)
  - spatial arrangements (point-source, diffuse)
- **Factored decomposition:**



Music: Shannon Hurley / Mix: Michel Desnoues & Alexey Ozerov / Separations: Alexey Ozerov

# Summary

- **Acoustic Source Mixtures**  
The normal situation in real-world sounds
- **Spatial filtering**  
Canceling sources by subtracting channels
- **Time-Frequency Masking**  
Selecting spectrogram cells
- **Model-Based Separation**  
Exploiting regularities in source signals

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